

# Top precision at the LHC

Tomáš Ježo

University of Zürich

Based on:

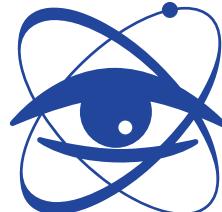
*TJ, Nason* [[arXiv:1509.09071](#)]

*TJ, Lindert, Nason, Oleari, Pozzorini* [[arXiv:1607.04538](#)]

14 December 2017



Universität  
Zürich<sup>UZH</sup>



Fyzikální ústav  
Akademie věd ČR, v. v. i.

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- Top = top quark
  - ▶ Third family quark, most massive particle of the SM



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- **precision**
  - ▶ Inclusion of higher order terms of the perturbative expansion



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  - ▶ The world's largest and most powerful particle collider, the most complex experimental facility ever built, and the largest single machine in the world<sup>†</sup>



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  - ▶ Most sofisticated calculations for top quark production at hadron colliders at NLO+PS accuracy



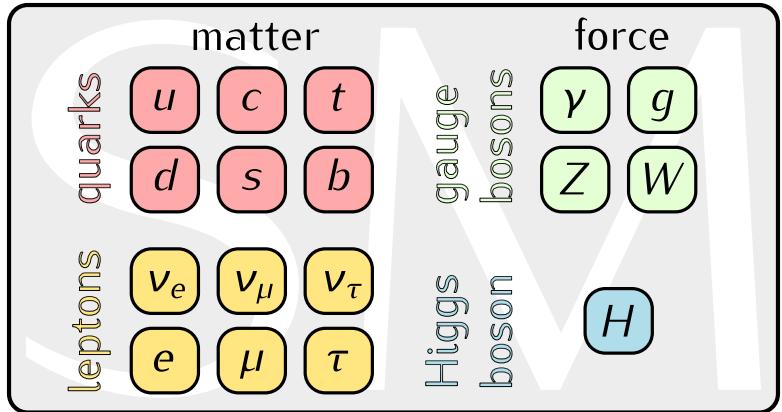
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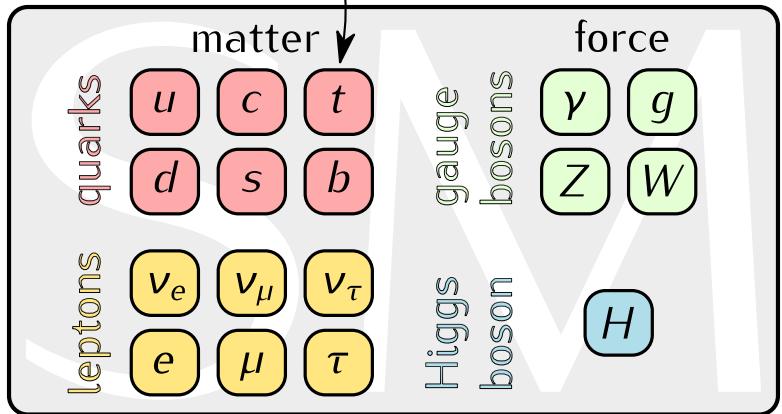
# Top quark trivia

- 3<sup>rd</sup> family up-type quark



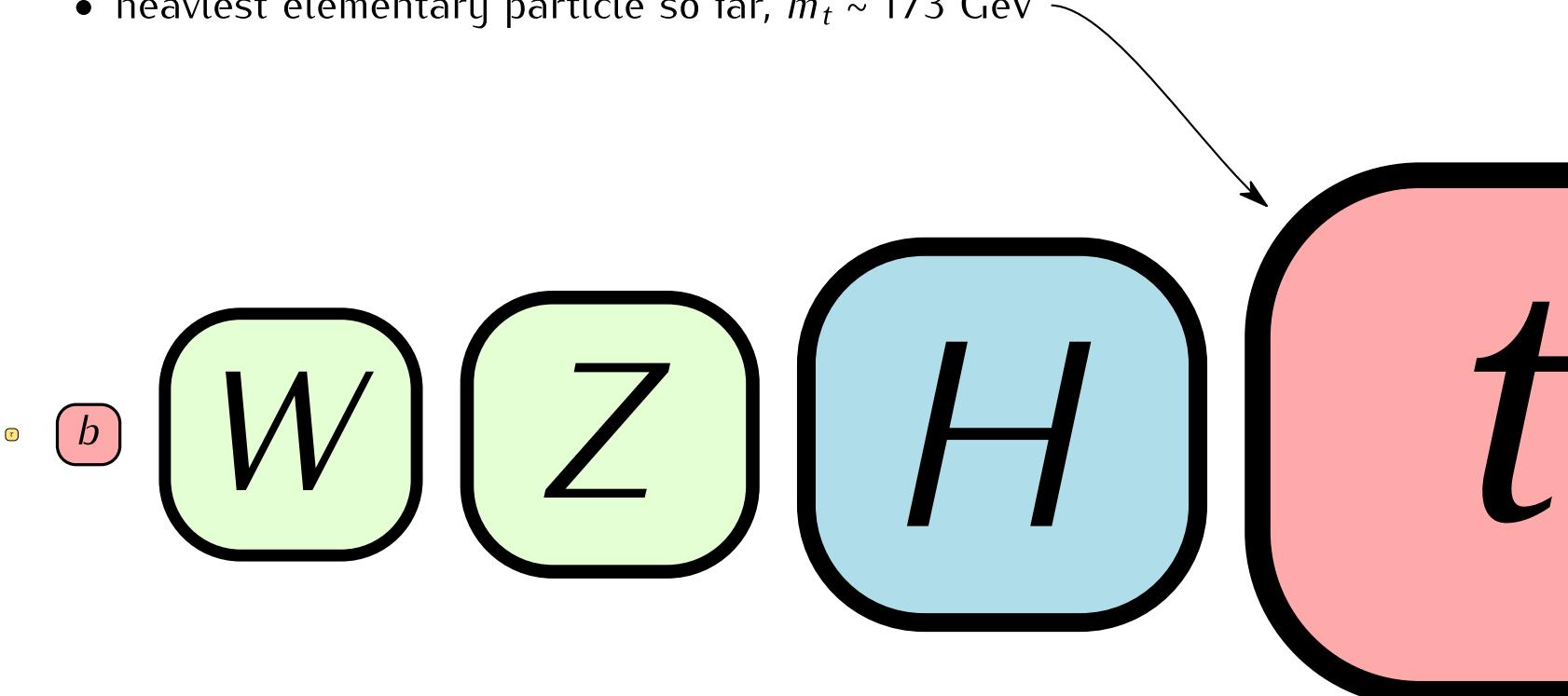
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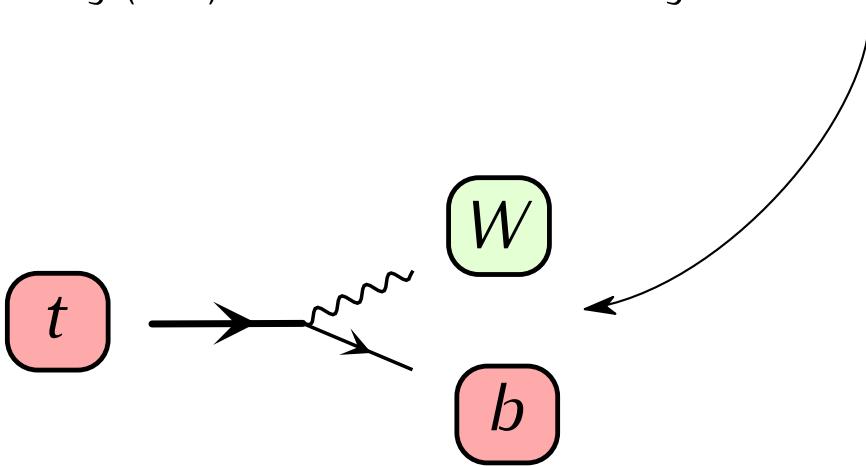
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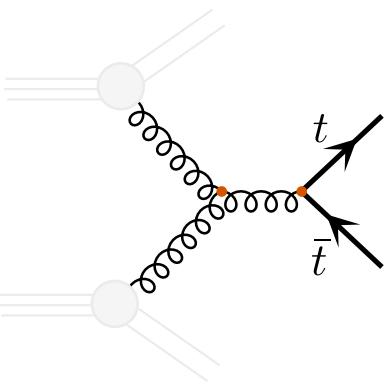
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- 3<sup>rd</sup> family up-type quark
- heaviest elementary particle so far,  $m_t \sim 173$  GeV
- is very short lived,  $\Gamma_t \sim 1.4$  GeV
  - ▶ relatively narrow **resonance**,  $\Gamma_t/m_t \sim 0.8\%$
  - ▶ **decays** before it gets a chance to hadronize, unlike any other quark
  - ▶ **decays** electroweakly (EW) and almost exclusively as  $t \rightarrow W + b$



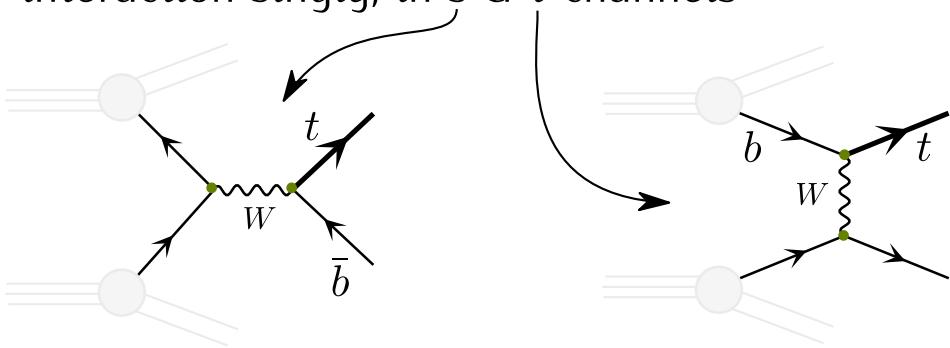
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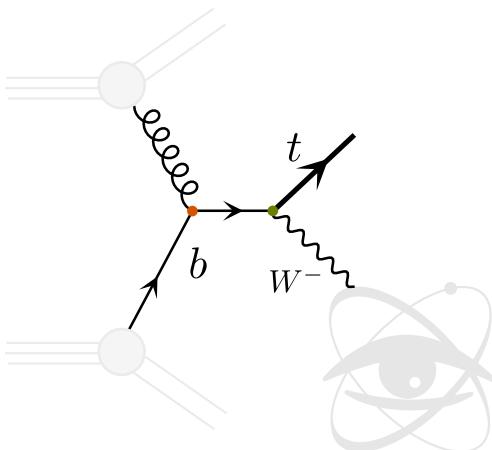
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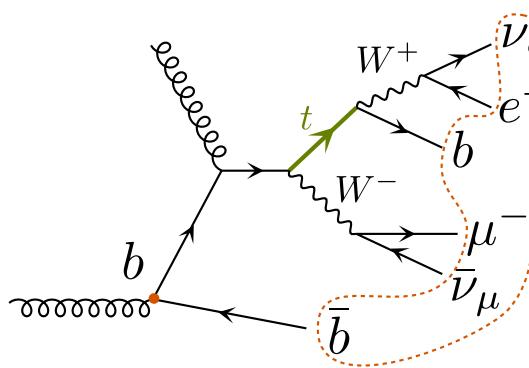
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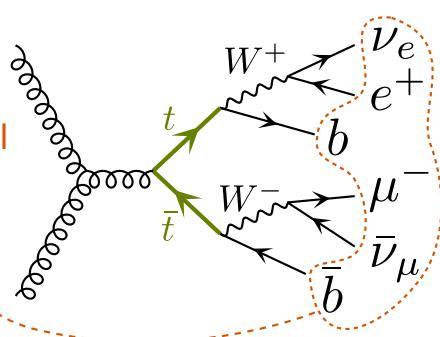


# Top quark trivia

$tW$  associated production @ NLO



$t\bar{t}$  production @ LO



same final state!

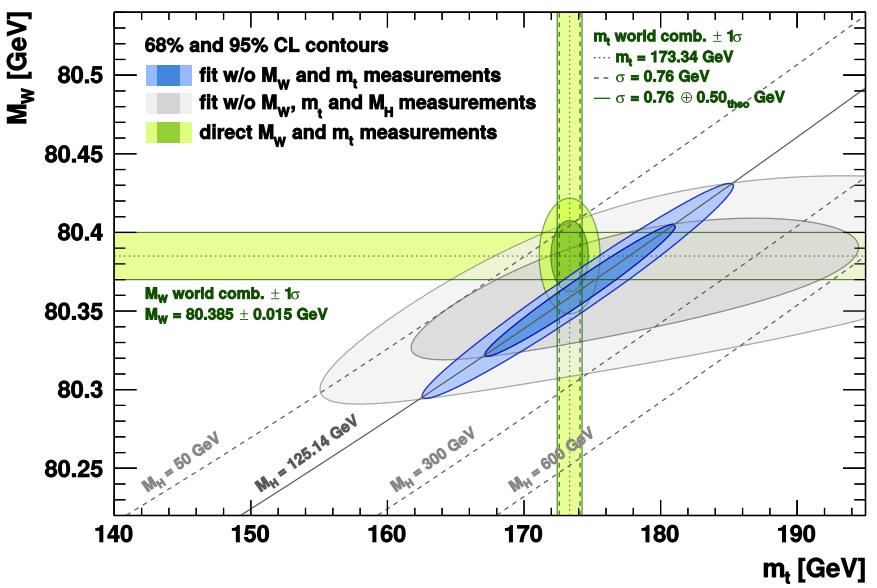
- at a hadron collider produced:
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goes out the window!



# Top quark mass

- $m_H$ ,  $m_W$  and  $m_T$  correlated in the SM
  - ▶ Accurate knowledge of  $m_T$  constitutes a precision test of the SM

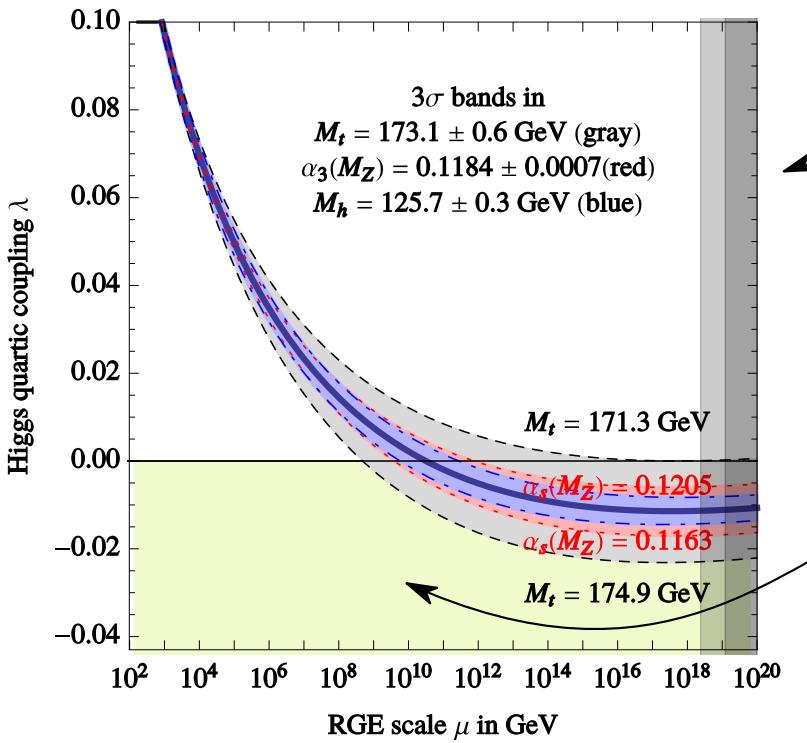


Global fit to electroweak precision observables  
[\[arXiv:1407.3792\]](https://arxiv.org/abs/1407.3792)



# Top quark mass

- Due to its large mass top couples to the Higgs boson rather strongly
  - ▶ RG flow of the Higgs quartic sensitive to the value of  $m_T$



RG flow of the Higgs quartic coupling for  $m_H = 125.7$  GeV  
[\[arXiv:1512.01222\]](https://arxiv.org/abs/1512.01222)

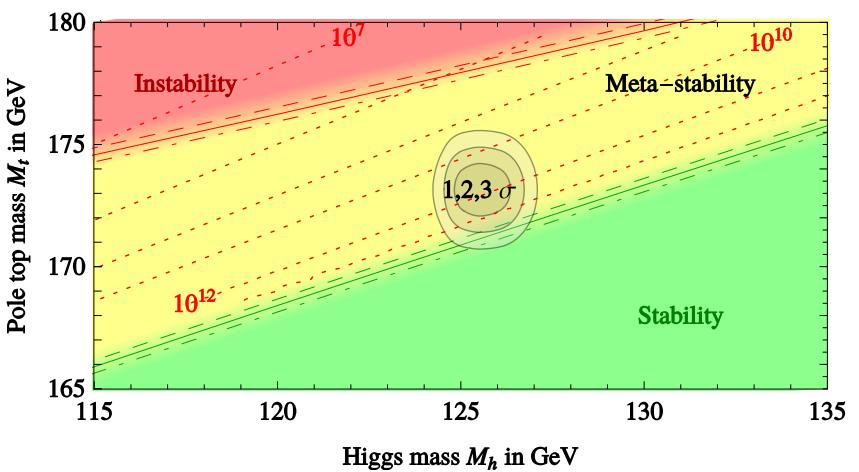
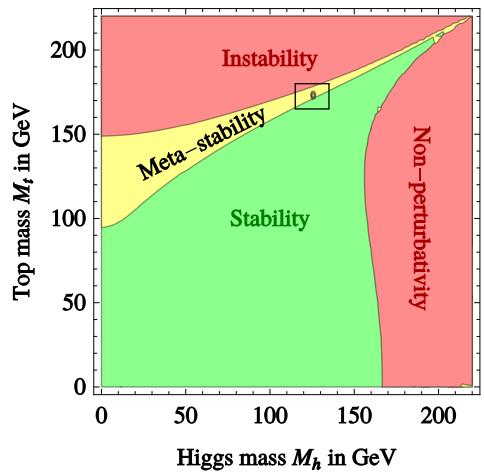
Higgs potential has no minimum for  $\lambda < 0$ !



# Top quark mass

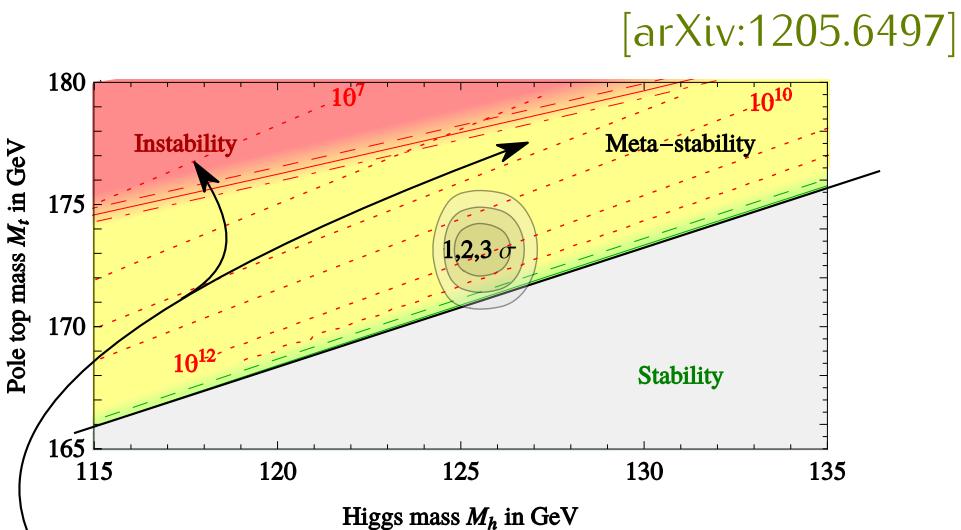
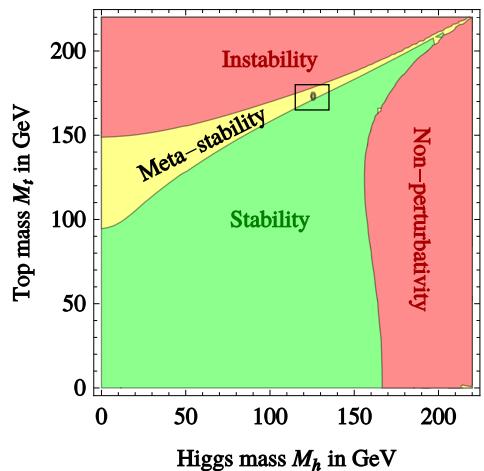
- Due to its large mass top couples to the Higgs boson rather strongly
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[arXiv:1205.6497]



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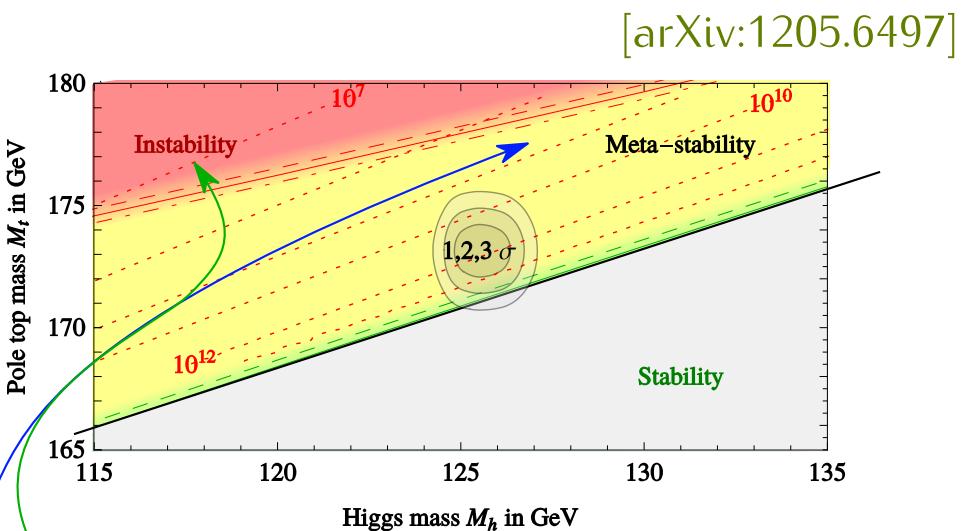
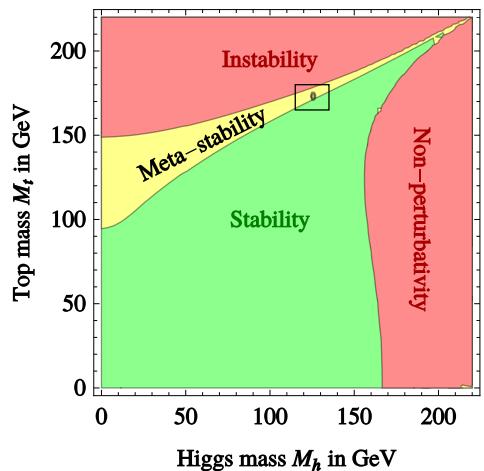


Higgs quartic coupling  $\lambda_H$  runs to negative values at Planck scale



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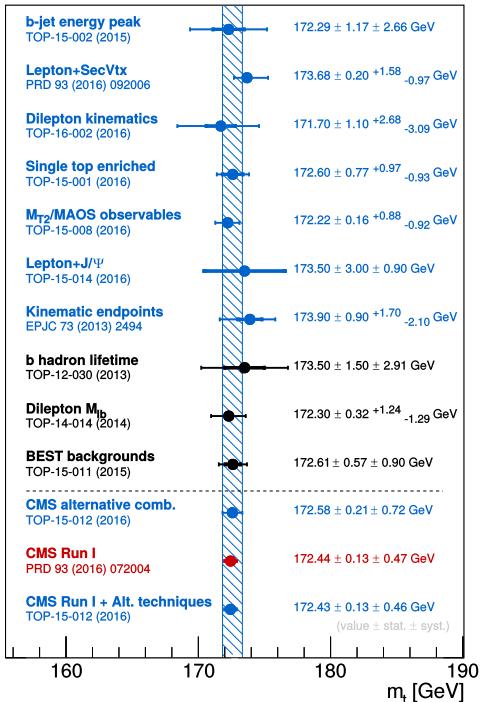
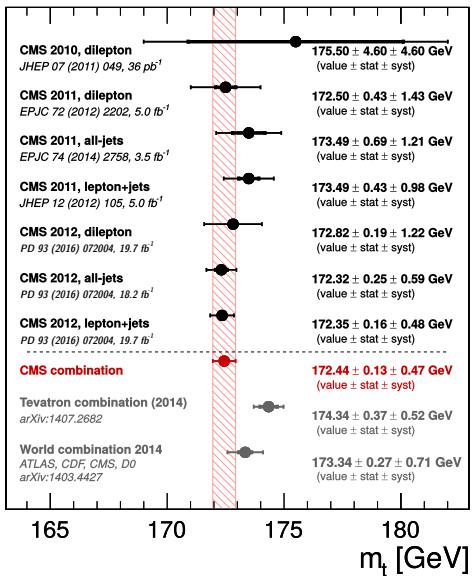
The vacuum life-time is long enough

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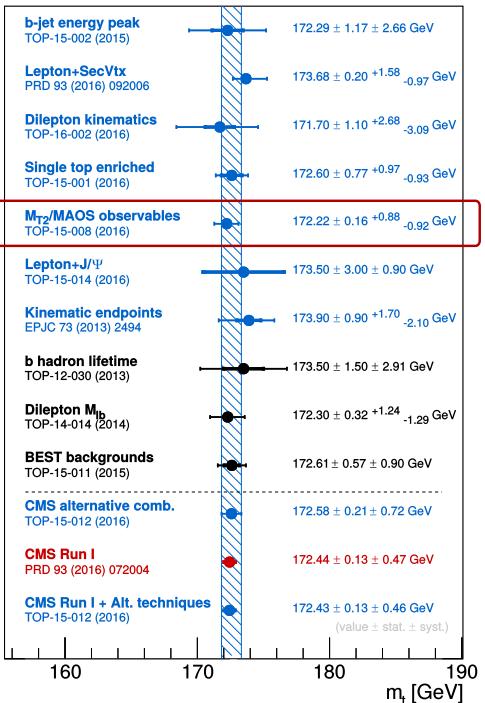
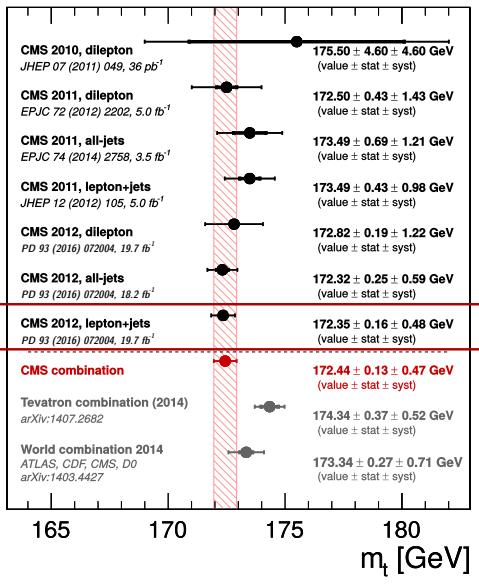
# Top quark mass

- $m_T$  measurement at the LHC
  - ▶ Plethora of methods for  $m_t$  determination
  - ▶ Most precise ones rely on top reconstruction from its decay products
  - ▶ Top-quarks abundantly produced at the LHC



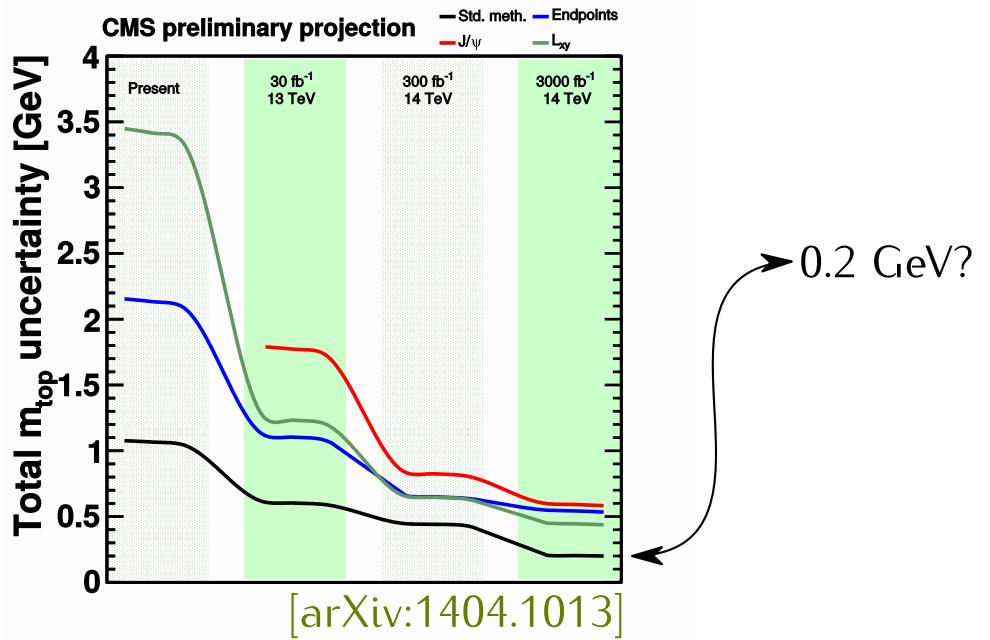
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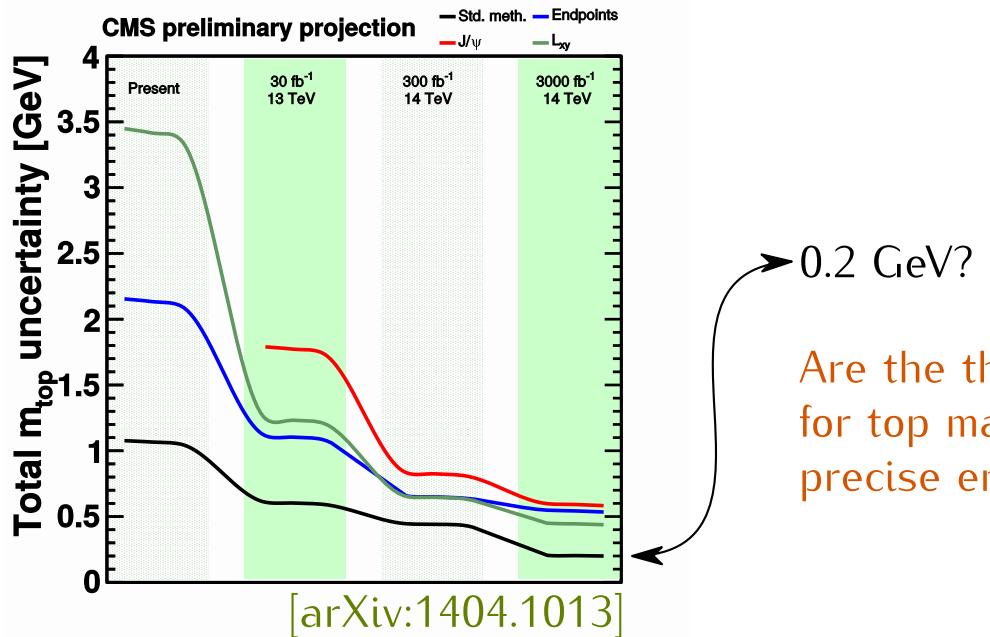
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# Top quark

arXiv id	observable	top backgrounds
<a href="#">1712.02758</a>	Higgs and $Z$ to $\varphi\gamma, \rho\gamma$	<hr/>
<a href="#">1712.02118</a>	long lived charginos	$t\bar{t}$
<a href="#">1712.02304</a>	$H \rightarrow ZZ^* \rightarrow 4l$	$t\bar{t}, t\bar{t} + Z, t\bar{t} + H$
<a href="#">1712.02332</a>	squarks and gluinos	$t\bar{t}, Wt, ST, t\bar{t} + W/Z/WW$
<a href="#">1712.01602</a>	$d\sigma_{tW}$	duh
<a href="#">1711.11520</a>	top-squark pair	$t\bar{t}, Wt, ST, t\bar{t} + Z$
<a href="#">1711.08341</a>	soft-drop jet mass	<hr/>
<a href="#">1711.03301</a>	dark matter, other NP	$t\bar{t}, ST$ (small contrs)
<a href="#">1711.03296</a>	$\sigma_{W^+}/\sigma_{W^-}$ and $d\sigma_W$	$t\bar{t}, ST$
<a href="#">1711.02692</a>	$\sigma_{(\text{di})\text{jet}}$	<hr/>
<a href="#">1711.01901</a>	Supersymmetry	$t\bar{t}, ST, Wt$
<a href="#">1710.11412</a>	dark matter + $b/t$ quarks	$t\bar{t}, ST, t\bar{t} + W/Z/\gamma/H, t\bar{t} + WW/t\bar{t}, \dots$
<a href="#">1710.09560</a>	$\sigma$ isolated- $\gamma$ + h.f. jet	<hr/>
<a href="#">1710.09748</a>	$H^{++}$	$t\bar{t}, ST, t\bar{t}W/Z/\gamma/H$
<a href="#">1710.07235</a>	$WW/WZ$ resonances	$t\bar{t}, ST$
<a href="#">1710.07171</a>	pair-produced resonances	$t\bar{t}$
...	...	...



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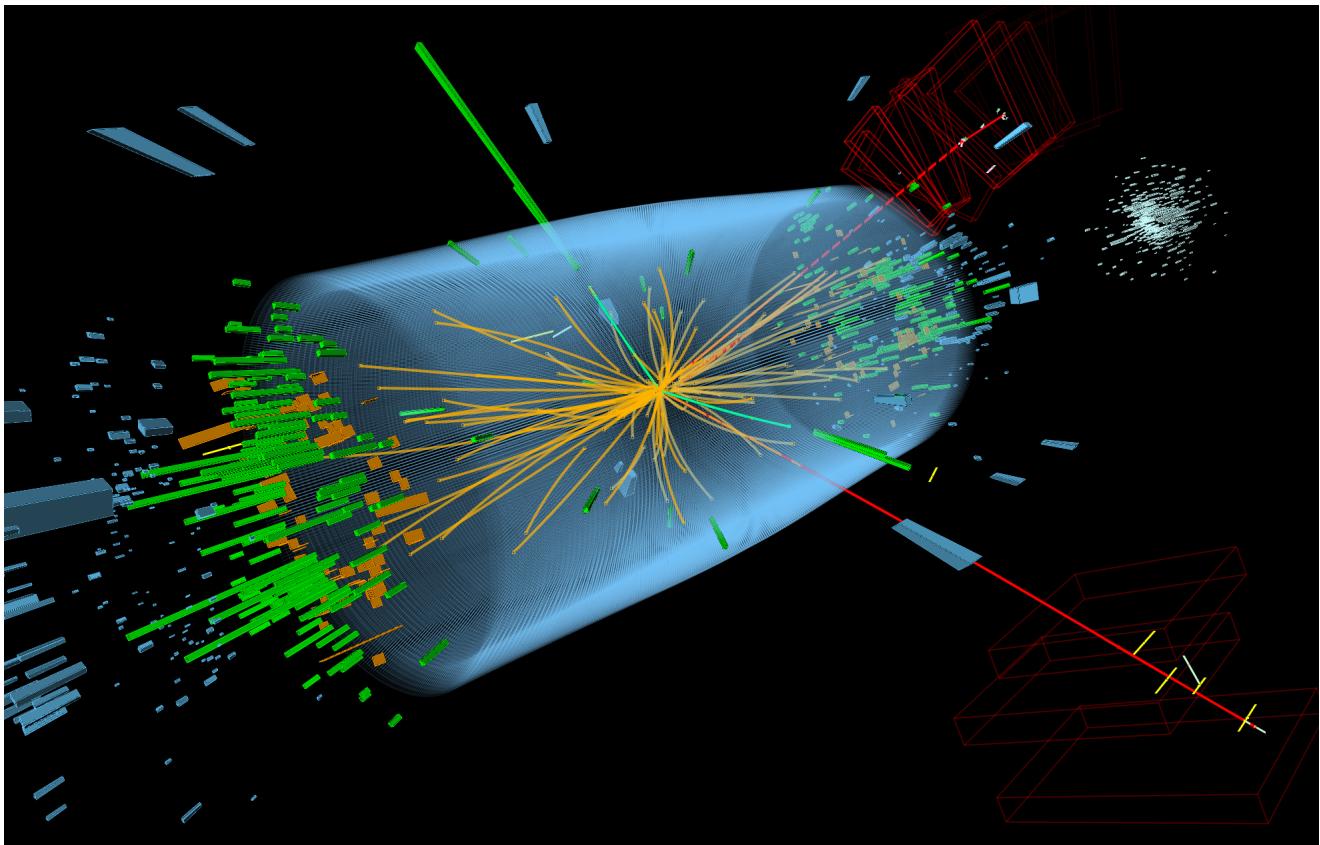
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1711.08341	sd	
1711.03301	da	
1711.03296	$\sigma_W$	
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...	...	...

12/16 require reliable simulation of  $t\bar{t}$ !



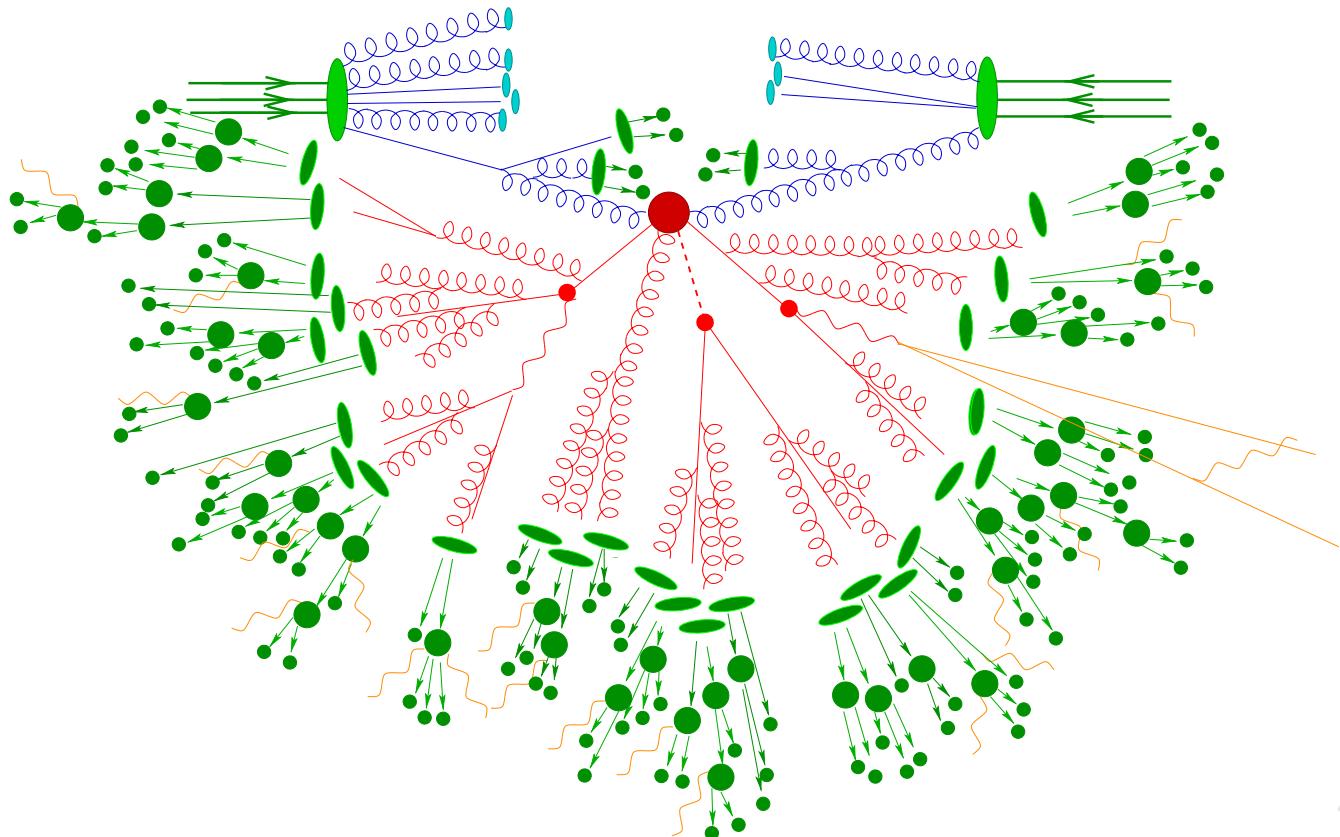
# Hadronic collisions

- An example of a proton-proton collision



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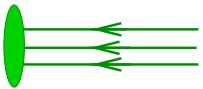
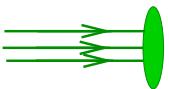


† drawing by Sherpa



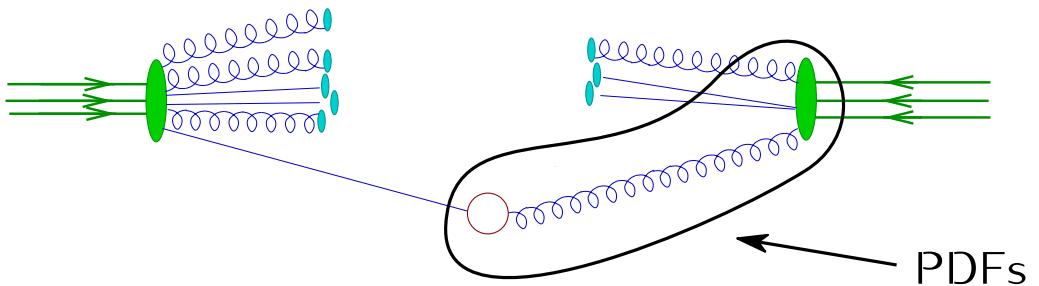
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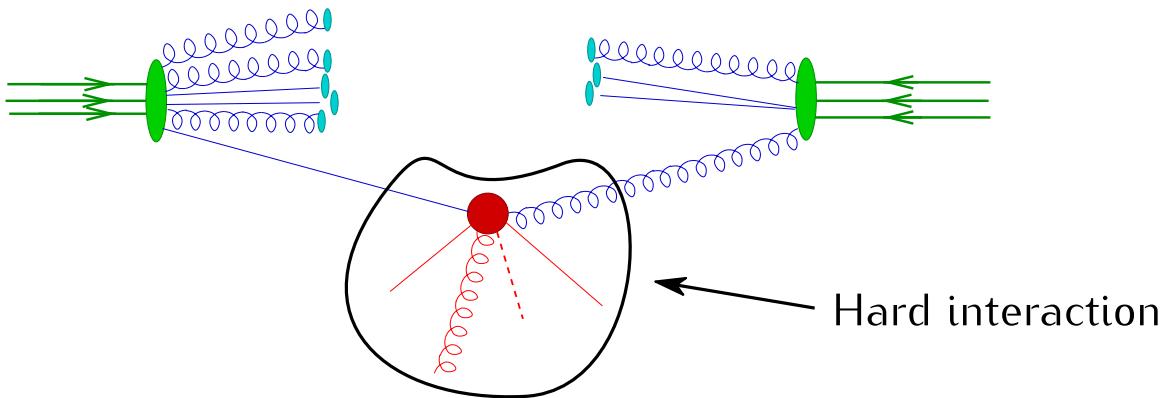
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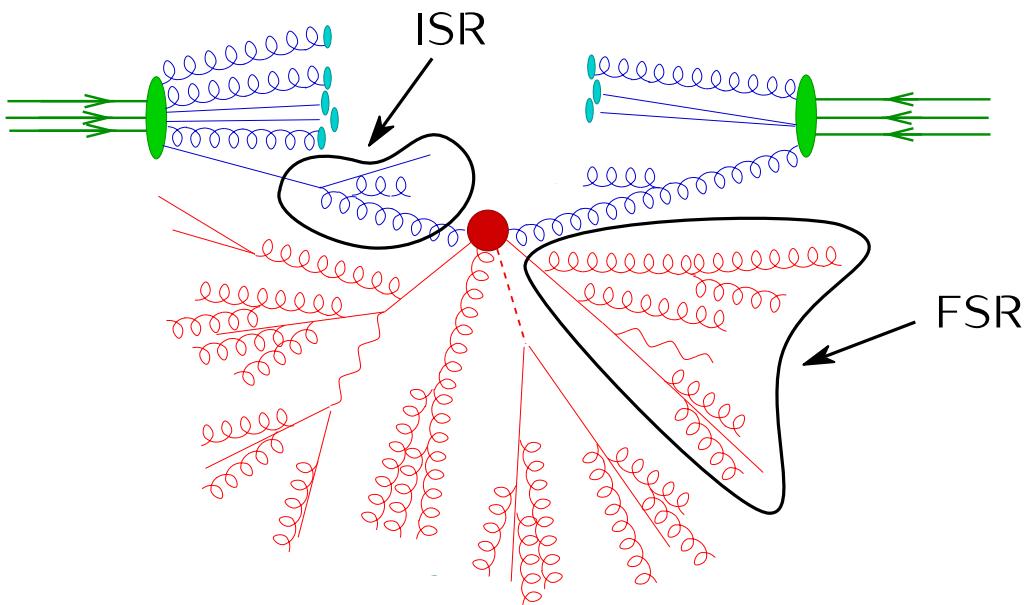
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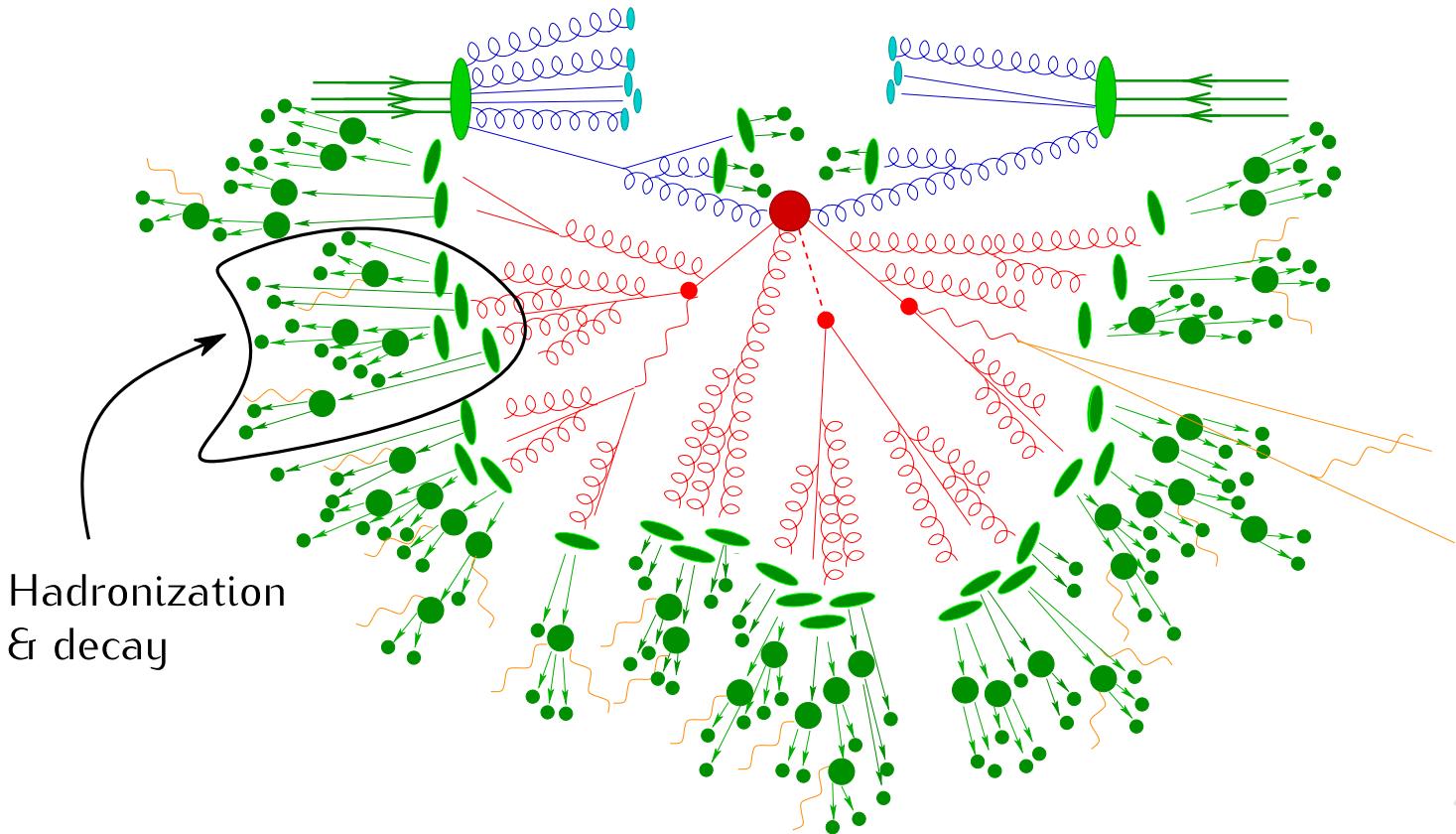
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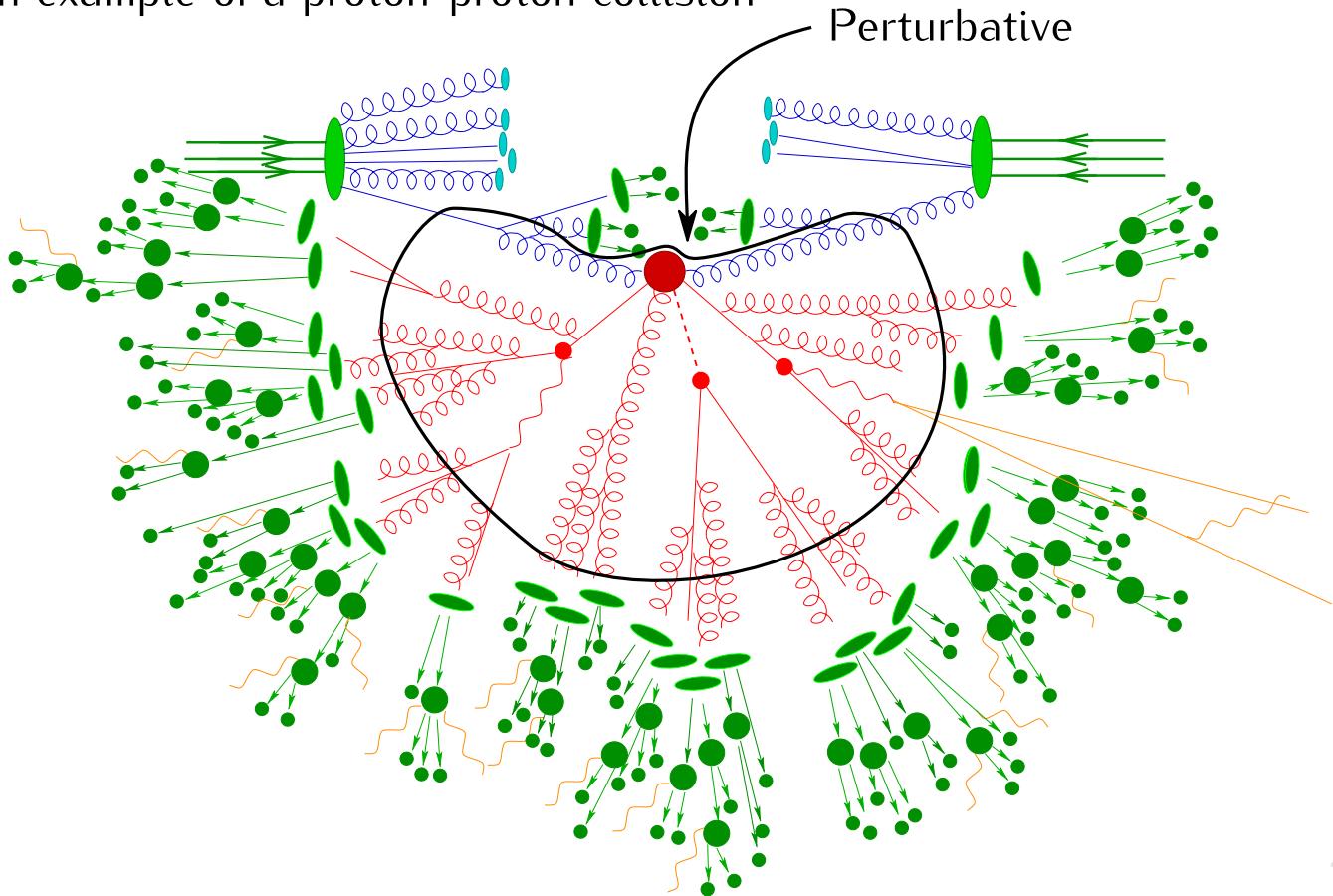
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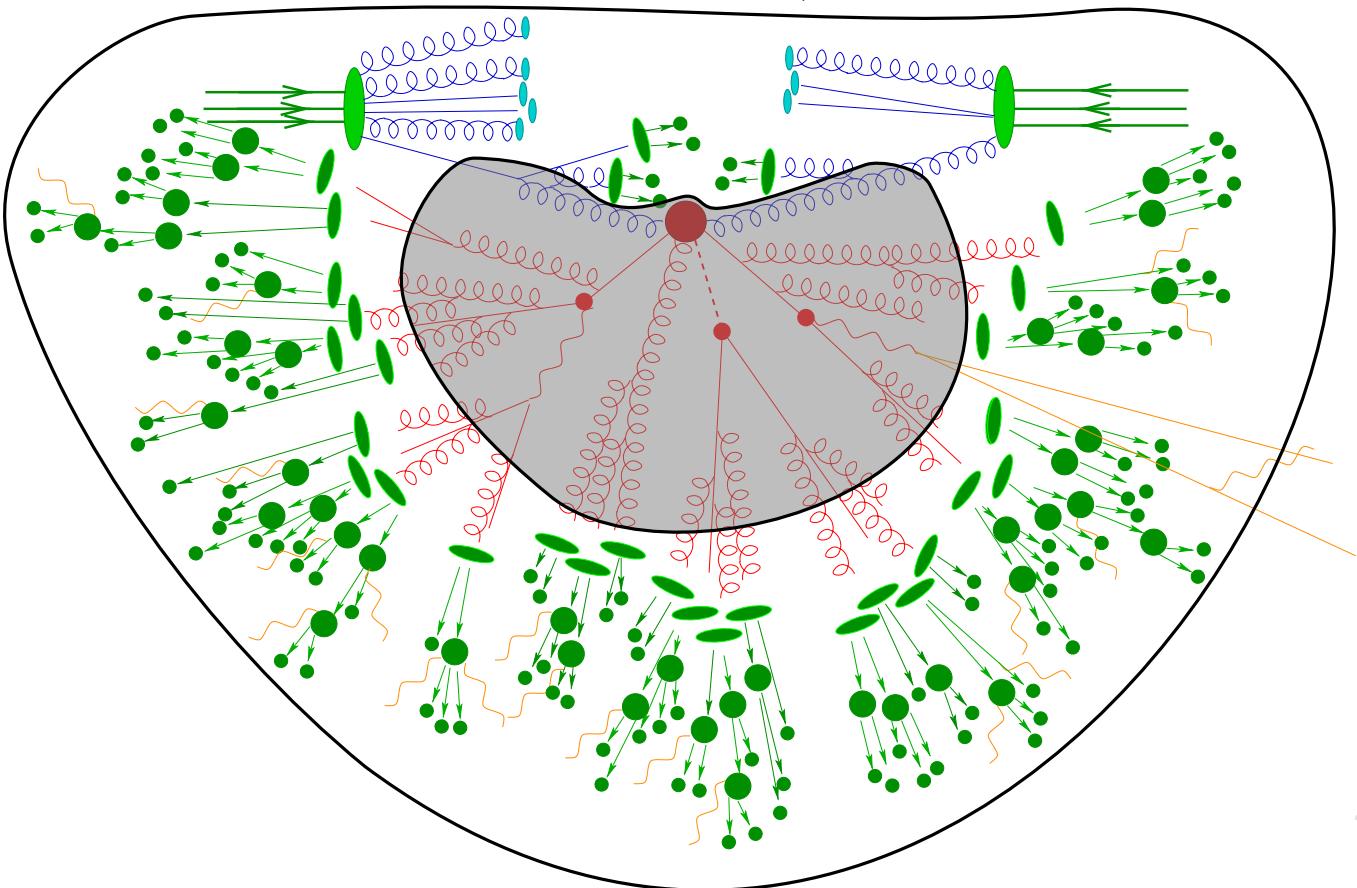
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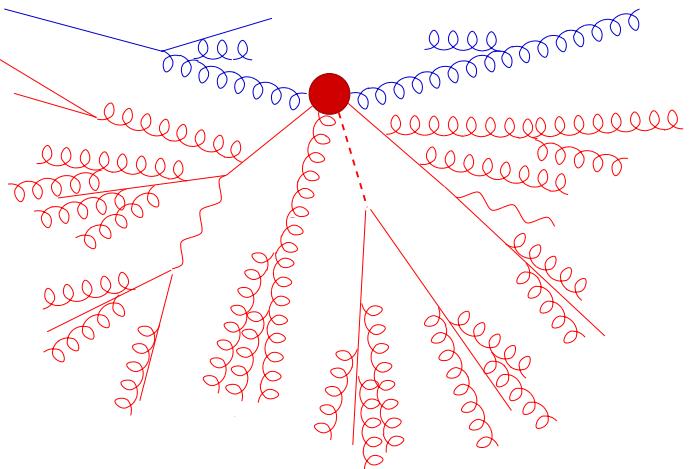
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Non perturbative



# Hadronic collisions

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  - ▶ I focus on the perturbative part
  - ▶ in particular: interplay of fixed order NLO calculations and PS



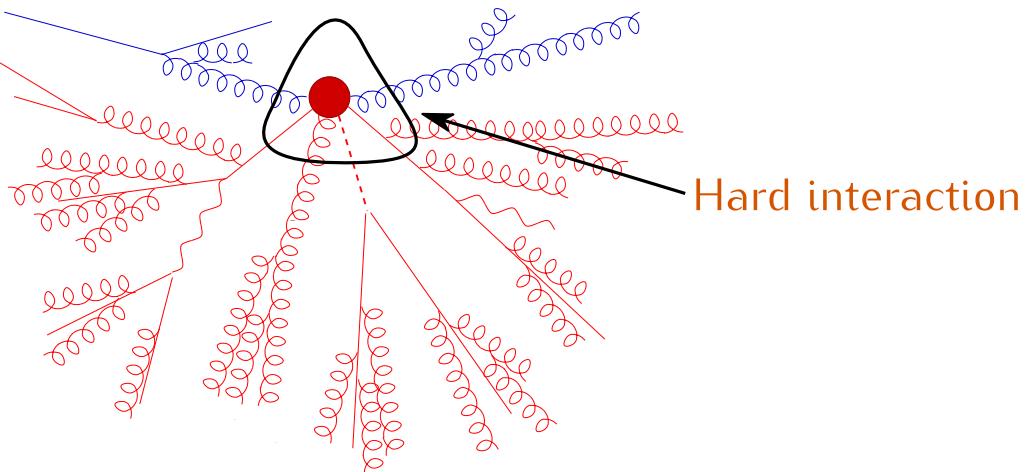
PS = Parton Shower

NLO = Next-to-Leading Order



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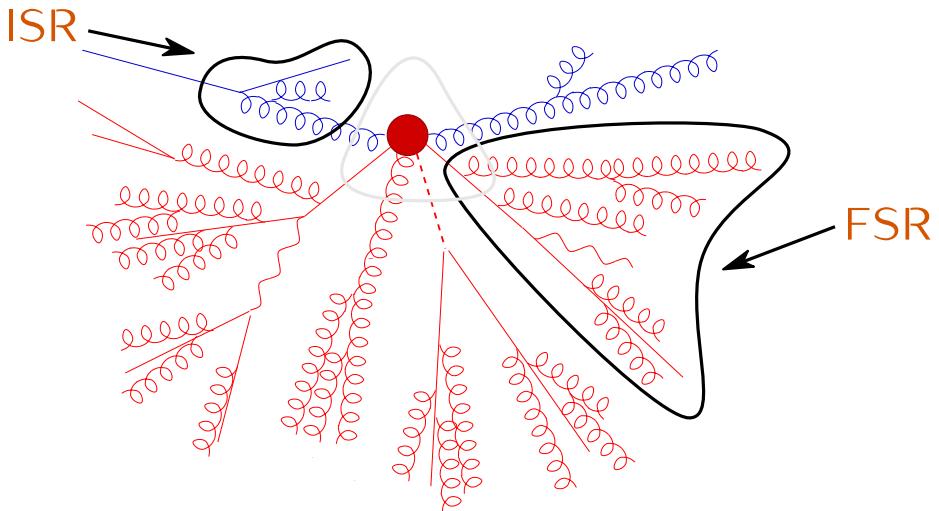
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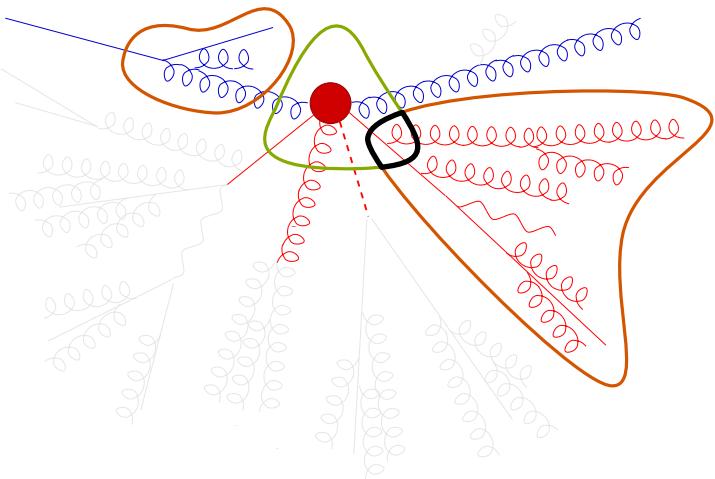
ISR = Initial State Radiation

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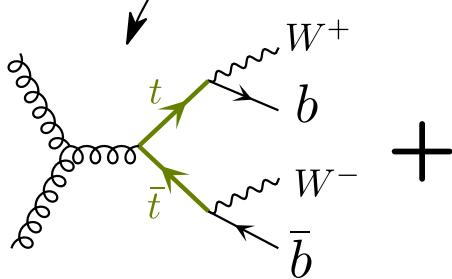
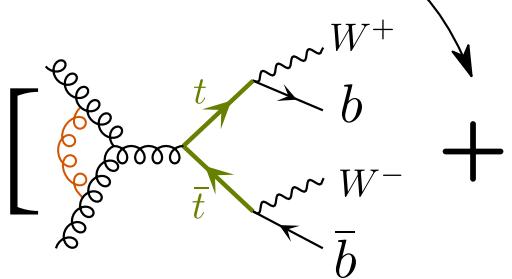
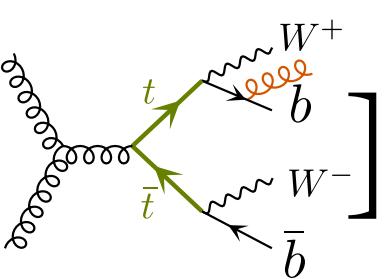
FSR = Final State Radiation



# Precise calculations for colliders

- Perturbative expansion in coupling constants:

$$\sigma(\mu_r) = \frac{\alpha(\mu_r)}{\pi} \hat{\sigma}_1 + \left( \frac{\alpha(\mu_r)}{\pi} \right)^2 \hat{\sigma}_2 + \left( \frac{\alpha(\mu_r)}{\pi} \right)^3 \hat{\sigma}_3 + \mathcal{O}\left[ \left( \frac{\alpha(\mu_r)}{\pi} \right)^4 \right]^{\dagger}$$

 +
  +
 

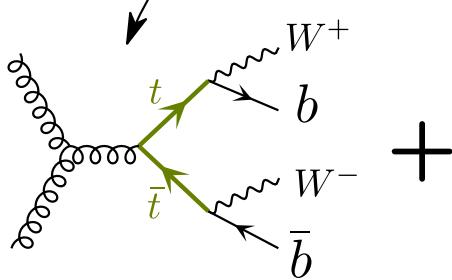
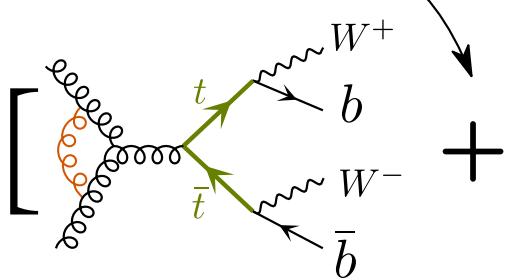
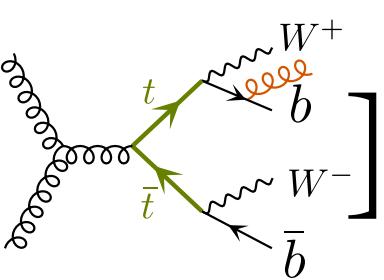
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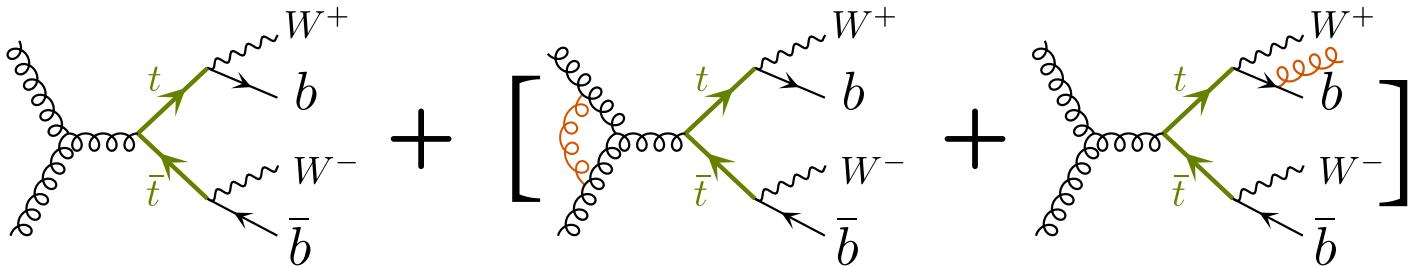
precise = including terms beyond the leading order

<sup>†</sup> keep in mind that there are multiple coupling constants in the SM



# Precise calculations for colliders

- Perturbative expansion in coupling constants:



- State of the art for top-pair and single top production:

- Single top, top pair NNLO QCD [[arXiv:1404.7116,1511.00549](#)]
- Top pair NNLO QCD + NLO EW [[arXiv:1511.00549](#)]
- Single top  $\times$  decay in NWA at approximate NNLO QCD [[arXiv:1708.09405](#)]
- Top pair  $\times$  decay in NWA at approximate NNLO QCD [[arXiv:1705.08903](#)]
- Single top full off-shell leptonic NLO QCD [[arXiv:1305.7088](#)]
- Top pair full off-shell leptonic NLO QCD [[arXiv:1312.0546](#)]
- Top pair full off-shell leptonic NLO EW [[arXiv:1607.05571](#)]
- Top pair full off-shell semileptonic NLO mixed [[arXiv:1711.10359](#)]



# Precise calculations for colliders

- Perturbative expansion in coupling constants:

$$\sigma(\mu_r) = \frac{\alpha(\mu_r)}{\pi} \hat{\sigma}_1 + \left( \frac{\alpha(\mu_r)}{\pi} \right)^2 \hat{\sigma}_2 + \left( \frac{\alpha(\mu_r)}{\pi} \right)^3 \hat{\sigma}_3 + \mathcal{O}\left[ \left( \frac{\alpha(\mu_r)}{\pi} \right)^4 \right]$$

- All order resummation:

- ▶ In most calculations logarithms of scale ratios appear
- ▶ When the scales are widely separated, the logs become large spoiling the convergence
- ▶ Resummation: "The art of constructing, from a subset of terms in a finite order perturbation series, an all-orders expression whose expansion gives at least those terms back."
- ▶ Universal numeric approach exists, known as Parton Shower, resuming leading logarithms
- ▶ Analytic process dependend calculations with higher accuracy available<sup>†</sup>

<sup>†</sup> heavily underrepresented in this talk

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- All orders

- Stacking PS on top of LO calculations trivial
- General framework for matching PS to NLO calculations known
- Some NNLO+PS calculations available

spoiling

“...rums in a finite order perturbation series, an all-orders expression whose expansion gives at least those terms back.”

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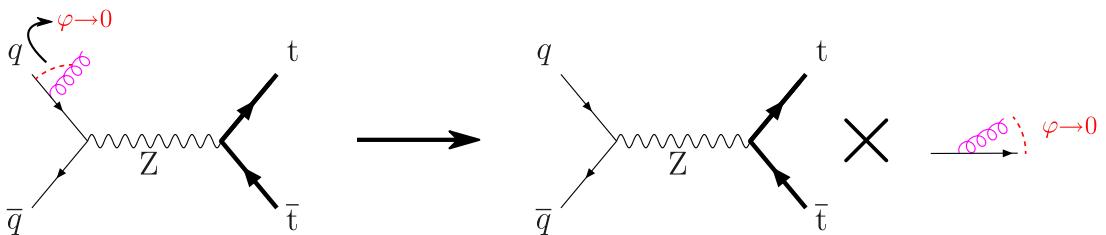
- All orders in coupling constant available
  - Stacking PS on top of LO calculations trivial
  - General framework for matching PS to NLO calculations known
  - Some NNLO+PS calculations available
- “The PS is a sum of terms in a finite order perturbation series, an all-orders expression whose expansion gives at least those terms back.”
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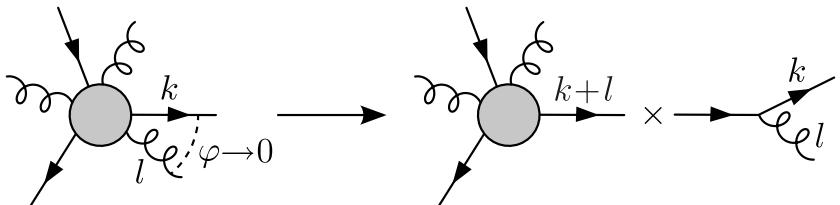
# Parton Shower

- In the collinear limit:



# Parton Shower

- In the collinear limit:



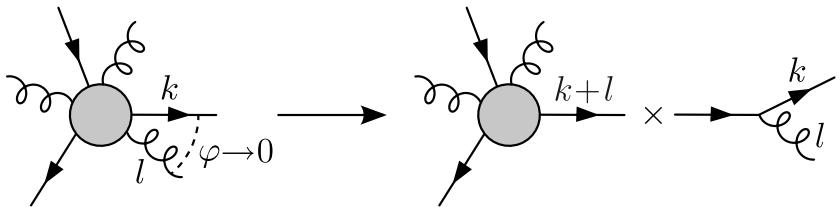
$$|\mathcal{M}_{n+1}|^2 d\Phi_{n+1} \rightarrow |\mathcal{M}_n|^2 d\Phi_n \times \frac{\alpha_S}{2\pi} \frac{dt}{t} P_{q,qg}(z) dz \frac{d\phi}{2\pi}$$

- $t$  hardness measure ( $\rightarrow 0$ ),  $z$  momentum fraction,  $\phi$  azimuthal angle
  - $P_{q,qg}(z)$  Altarelli-Parisi splitting for  $q \rightarrow qg$
- Can be applied recursively:  $n$  splittings naively correspond to real corrections at  $N^n$ NLO



# Parton Shower

- In the collinear limit:



$$|\mathcal{M}_{n+1}|^2 d\Phi_{n+1} \rightarrow |\mathcal{M}_n|^2 d\Phi_n \times \frac{\alpha_S}{2\pi} \frac{dt}{t} P_{q,qg}(z) dz \frac{d\phi}{2\pi}$$

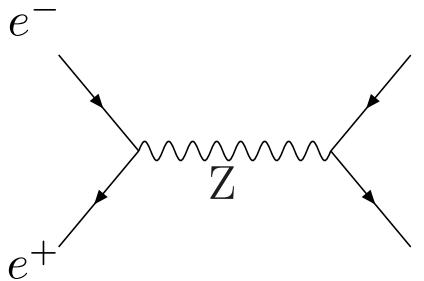
- Virtual corrections taken into account via Sudakov form factor

$$dP(t, t + dt) = \frac{\alpha_S}{2\pi} \frac{dt}{t} \int \frac{d\phi}{2\pi} \int P_{i,jl}(z) dz$$

- $dP$  probability of  $i \rightarrow jl$  splitting in  $[t, t + dt]$
- $1 - dP$  probability of no emission, equivalent of virtual correction



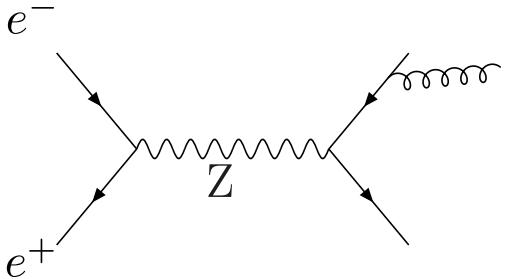
# Parton Shower



$$W = W_B$$

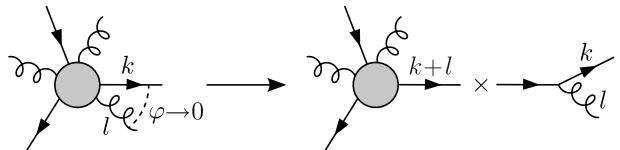


# Parton Shower



$$W = W_B \times V$$

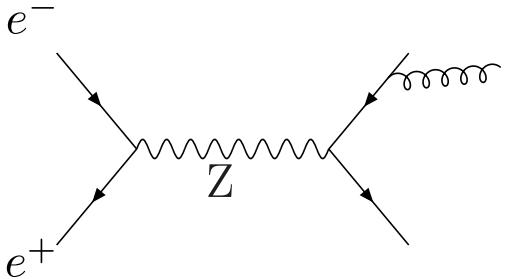
- Real corrections in collinear approximation:



$$|\mathcal{M}_{n+1}|^2 d\Phi_{n+1} \rightarrow |\mathcal{M}_n|^2 d\Phi_n \times \left( \frac{\alpha_s}{2\pi} \frac{dt}{t} P_{q,qg}(z) dz \right) d\phi$$

Diagram illustrating the evolution of a parton shower. A primary parton with momentum  $k$  and angle  $\theta_l$  emits a secondary parton with momentum  $l$  and angle  $\theta'_l$ . As  $\theta'_l \rightarrow 0$ , the emission becomes collinear. The emitted parton is labeled  $V$ .

# Parton Shower



$$W = W_B \times V \times \Delta$$

- Virtual corrections in collinear approximation:

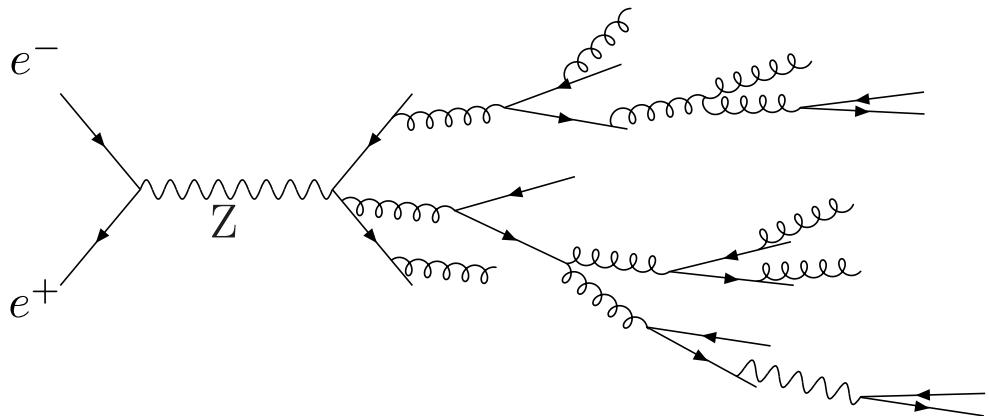
$$dP(\textcolor{red}{t}, \textcolor{red}{t} + dt) = \frac{\alpha_s}{2\pi} \frac{dt}{\textcolor{red}{t}} \int \frac{d\phi}{2\pi} \int P_{i,jl}(z) dz$$

- $dP$  probability of  $i \rightarrow jl$  splitting in  $[t, t + dt]$
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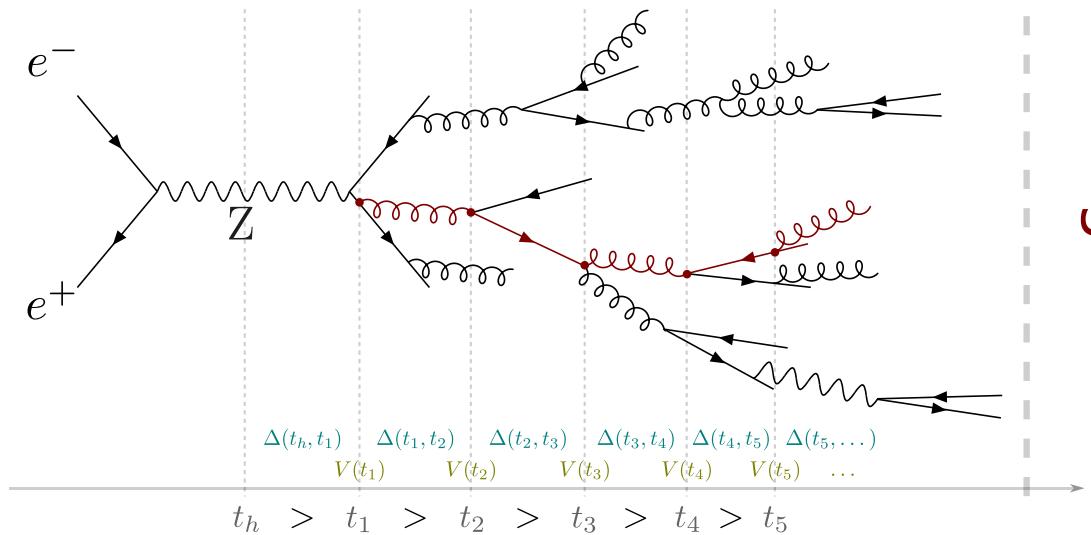
# Parton Shower

- Parton Shower can be automated



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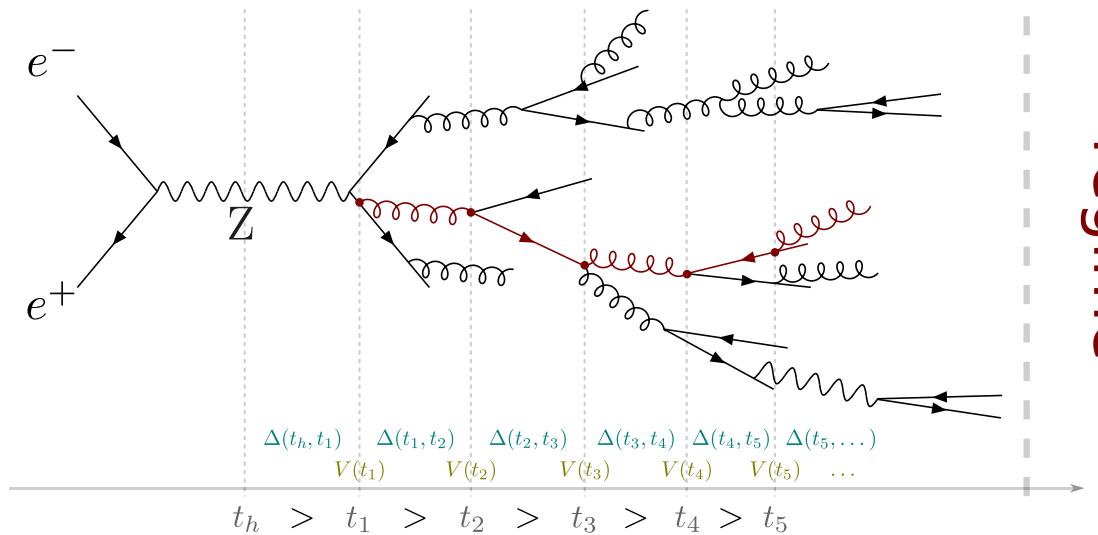


Non-perturbative regime

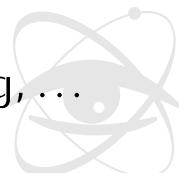
- Variable  $t$  measures hardness
  - Vanishes in the collinear limit
- Weight of the event is the Born weight times the splitting and Sudakov factors
- The ordering ensures equivalence to leading-logarithmic resummation

# Parton Shower

- Parton Shower can be automated

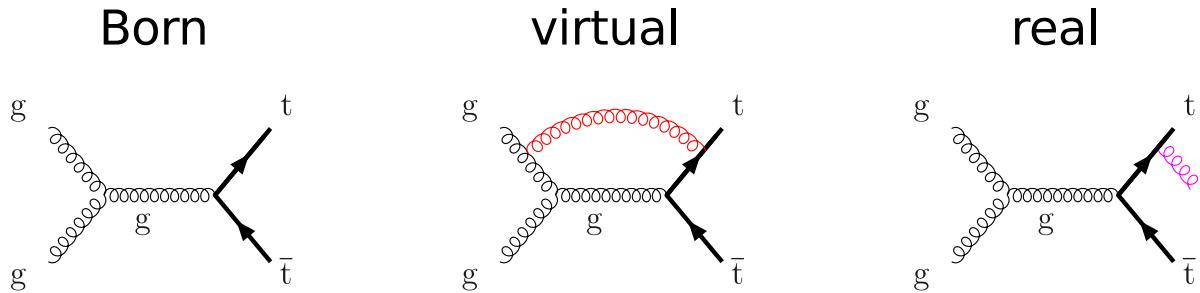


- With the purpose of:
  - Resumming leading-logarithms
  - Generating final state multiplicities unfeasible at FO
  - Modelling of clustering, hadronization, multi-parton scattering, ...
- Two well known Shower Monte Carlos (SMCs): Pythia, Herwig



# NLO & PS

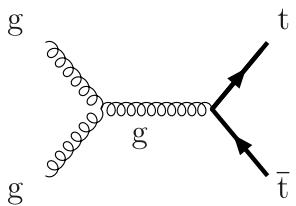
- Fixed order calculation @ NLO



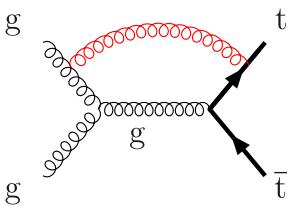
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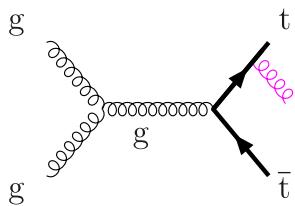
Born



virtual

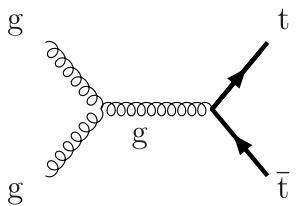


real

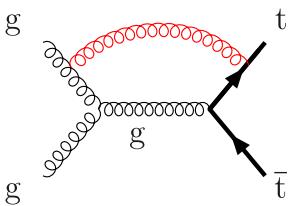


- Parton Shower

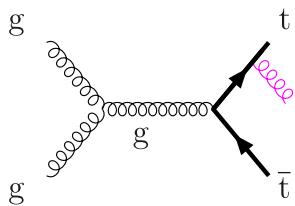
Born



$\Delta$

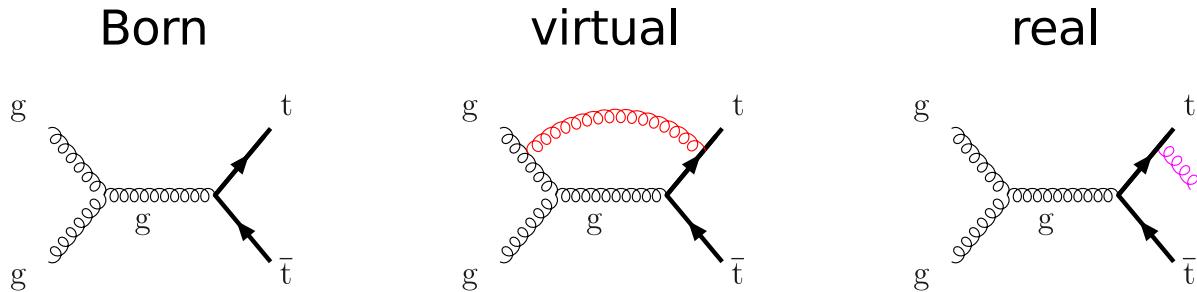


$V$

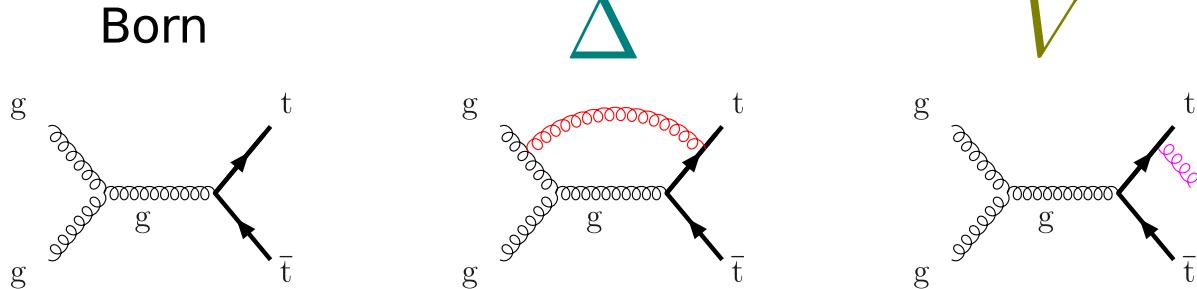


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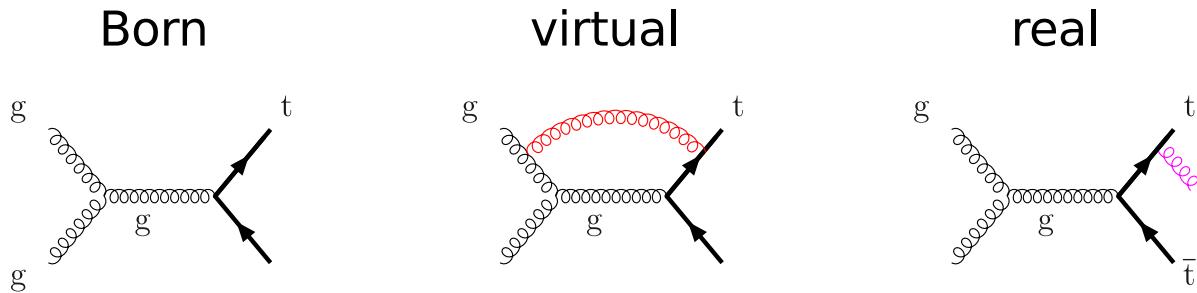


- Parton Shower

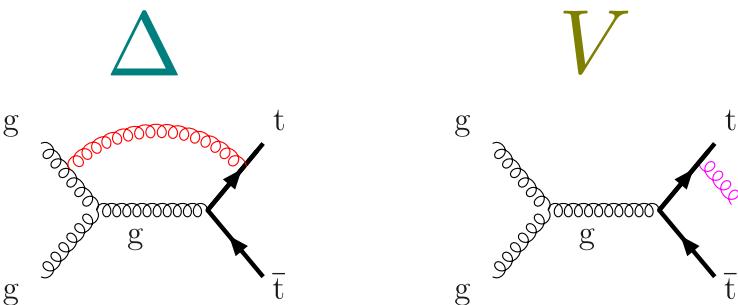


# NLO+PS

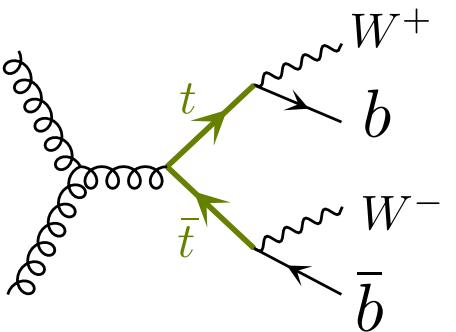
- NLO matched with PS



Leads to overcounting!  
 $\Delta$  and  $V$  counted twice!



# NLO+PS à la POWHEG

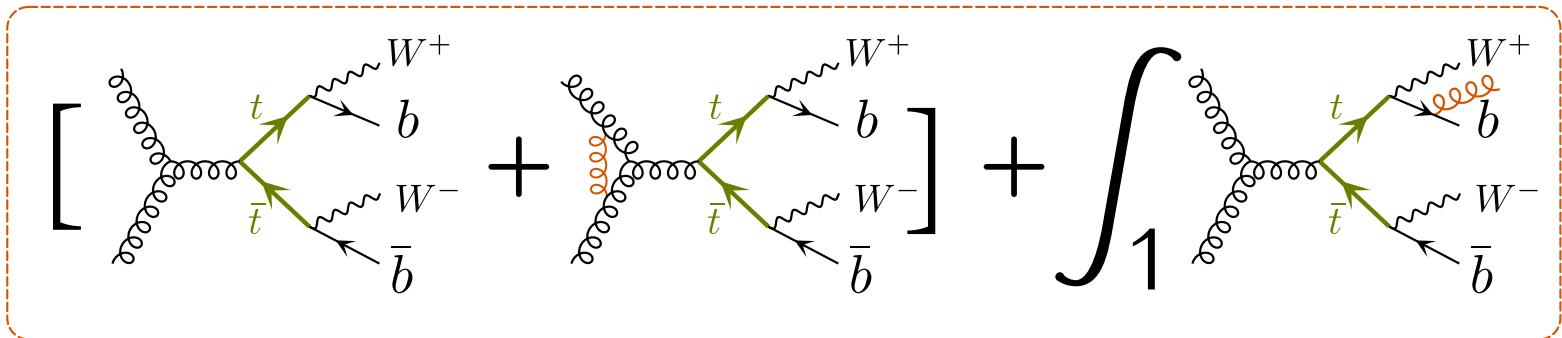


$$d\sigma = \overline{B}(\Phi_B) d\Phi_B \left[ \Delta(q_{\text{cut}}) + \sum_{\alpha} \Delta(k_T^{\alpha}) \frac{R_{\alpha}(\Phi_{\alpha}(\Phi_B, \Phi_{\text{rad}}))}{B(\Phi_B)} d\Phi_{\text{rad}} \right]$$

with  $\Delta(k_T^{\alpha}) = \exp \left[ - \int_{k_T^{\alpha} > q_{\text{cut}}} \frac{R_{\alpha}(\Phi_{\alpha}(\Phi_B, \Phi_{\text{rad}}))}{B(\Phi_B)} d\Phi_{\text{rad}} \right]$



# NLO+PS à la POWHEG

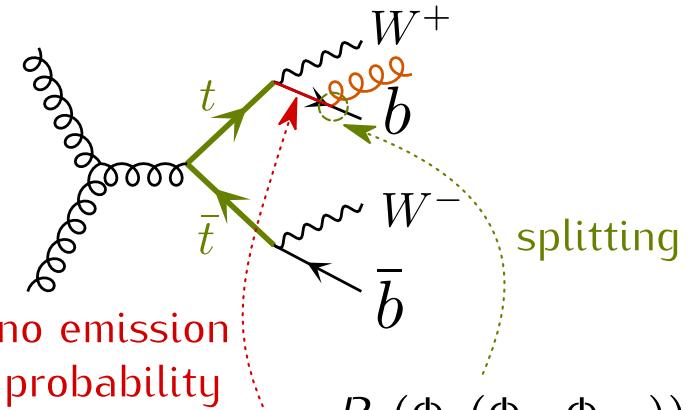


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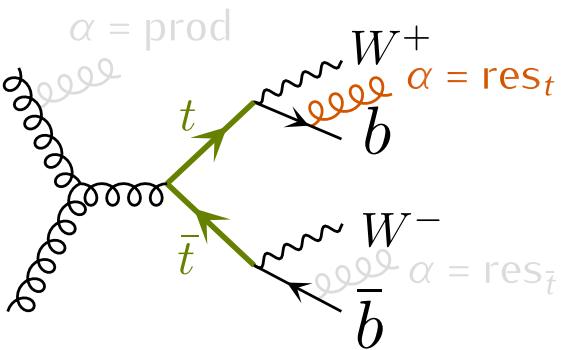


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- Such a NLO calculation can be resummed using the standard formulation of the Parton Shower supplemented by a  $p_T$  veto

# NLO+PS à la POWHEG

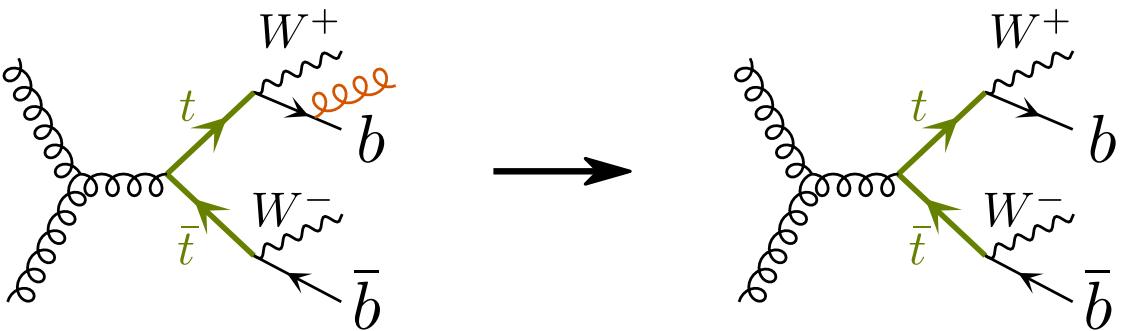


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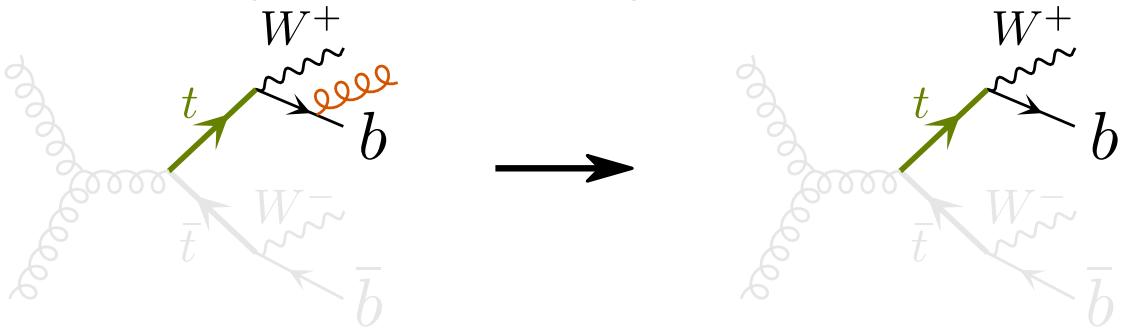
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- In standard formulation of the POWHEG method:
  - ▶  $n + 1 \leftrightarrow n$  mapping **doesn't preserve** top virtuality
  - ▶ Leading to **unphysical suppression** away from collinear singularities
  - ▶ Only **one hardest emission** is kept



# NLO+PS à la POWHEG

Only radiation in decay is concerned!



$$d\sigma = \bar{B}(\Phi_B) d\Phi_B \left[ \Delta(q_{\text{cut}}) + \sum_{\alpha} \Delta(k_T^{\alpha}) \frac{R_{\alpha}(\Phi_{\alpha}(\Phi_B, \Phi_{\text{rad}}))}{B(\Phi_B)} d\Phi_{\text{rad}} \right]$$

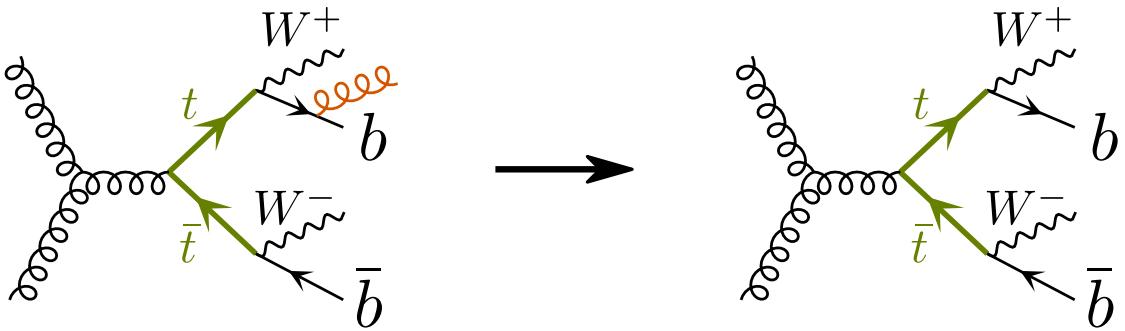
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# NLO+PS à la POWHEG RES

[TJ, P. Nason 2015]



$$d\sigma = \overline{B}(\Phi_B) d\Phi_B \left[ \Delta(q_{\text{cut}}) + \sum_{\alpha} \Delta(k_T^{\alpha}) \frac{R_{\alpha}(\Phi_{\alpha}(\Phi_B, \Phi_{\text{rad}}))}{B(\Phi_B)} d\Phi_{\text{rad}} \right]$$

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- In new “resonance-aware” formulation of the POWHEG method:
  - ▶  $n + 1 \leftrightarrow n$  mapping preserves top virtuality
  - ▶ No unphysical distortions of the top line shape
  - ▶ Keeps multiple emissions: from production and each resonance

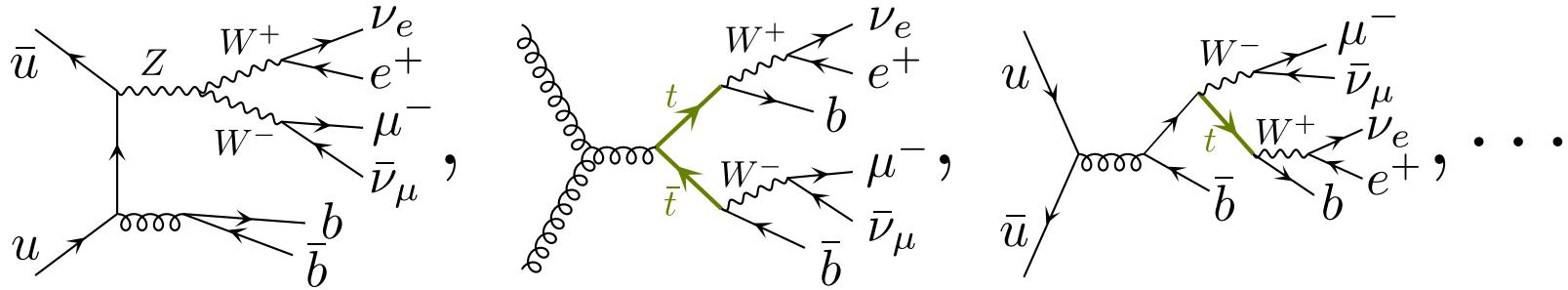


# bb41

[TJ, Lindert, Nason, Pozzorini, Oleari 2016]

- Process

- ▶  $pp \rightarrow \ell^+ \nu_\ell l^- \bar{\nu}_l b \bar{b}$  @ NLO QCD ( $pp \rightarrow W^+ b W^- \bar{b}$ ,  $W \rightarrow \text{leptons}$ )



- ▶ Born, real and virtual matrix elements by [OpenLoops](#)
- ▶ 4 flavour number scheme
  - ▷ Unified description of  $t\bar{t}$  and  $Wt$  production
  - ▷ Effects of  $b$ -quark mass included
  - ▷ Phase space with unresolved  $b$ -quarks accessible



# bb4l

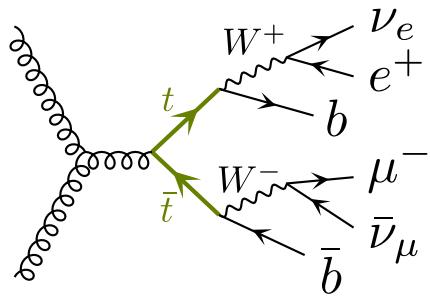
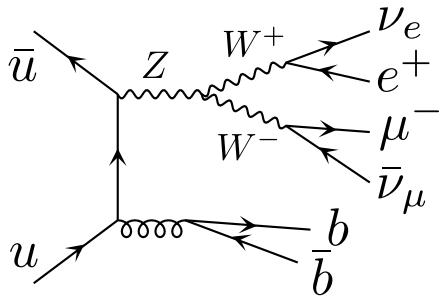
[T.J. Lindert, Nason, Pozzorini, Oleari 2016]

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- NLO+PS generator

- ▶ Implements resonance aware POWHEG method
- ▶ Employs 2 resonance histories



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- NLO+PS generator
  - ▶ Implements resonance aware POWHEG method
  - ▶ Employs 2 resonance histories ( $t(W^+ b)\bar{t}(W^- \bar{b})$ ,  $Z(W^+ W^-)b\bar{b}$ )
- Shower Monte Carlo
  - ▶ Standard LHE interface not sufficient (separate scalup required for production and each resonance)
  - ▶ Pythia8: PowhegHooksBB4L class publicly available (compatible with PowhegHooks)
  - ▶ Herwig7: coming soon



# bb4l

[TJ, Lindert, Nason, Pozzorini, Oleari 2016]

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  - ▶  $pp \rightarrow \ell^+ \nu_\ell l^- \bar{\nu}_l b \bar{b}$  @ NLO QCD ( $pp \rightarrow W^+ b W^- \bar{b}$ ,  $W \rightarrow \text{leptons}$ )
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- Shower Monte Carlo
  - ▶ Pythia8 interface available, Herwig7 coming soon
- Implementation
  - ▶ Resonance aware POWHEG method: **POWHEG BOX RES**
  - ▶ Process implementation: **b\_bbar\_4l** or **bbar4l**
  - ▶ Publicly available <http://powhegbox.mib.infn.it/>



# Results

- Compare  $t\bar{t}$  &  $tW$  generators
  - ▶ Generators:
    - ▷ hvq + ST\_wtch\_DR and hvq + ST\_wtch\_DS
    - ▷ ttb\_NLO\_dec ( $tW$  contribution only at LO)
    - ▷ bb4l
  - ▶ Observables:
    - ▷ Shapes of  $m_{Wj_B}$  and  $m_{lj_B}$
  - ▶ Setup:
    - ▷ LHC 8TeV
    - ▷ Anti- $k_T$  jets,  $R = 0.5$
    - ▷ The  $b/\bar{b}$  jet is the jet with the hardest  $b/\bar{b}$  flavoured hadron
    - ▷  $W$ 's fully reconstructed
    - ▷ Shower with Pythia 8.2



# $t\bar{t}$ & $tW$ generators in POWHEG BOX



- `hvq` [Frixione, Nason, Ridolfi, 2007], `ST_wtch_DR(S)` [Re, 2010]
  - ▶ Production at NLO
  - ▶ Decays at LO
  - ▶ Radiation from FS  $b$ 's only with PS
  - ▶ Includes hadronic  $W$  decays
- `ttb_NLO_dec` [Campbell, Ellis, Nason, Re, 2014]
  - ▶ Production at NLO
  - ▶ Decays at NLO
  - ▶ Radiation from FS  $b$ 's with ME (thanks to `allrad`)
  - ▶ Includes hadronic  $W$  decays,  $Wt$  contribution at LO
- `bb4l` [TJ, Lindert, Nason, Oleari, Pozzorini, 2016]
  - ▶  $pp \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b}$  production at NLO (production and decay at NLO)
  - ▶ Radiation from FS  $b$ 's with ME (thanks to `allrad`)
  - ▶ No hadronic  $W$  decays, Includes  $Wt$  contribution



# $t\bar{t}$ & $tW$ generators in POWHEG BOX



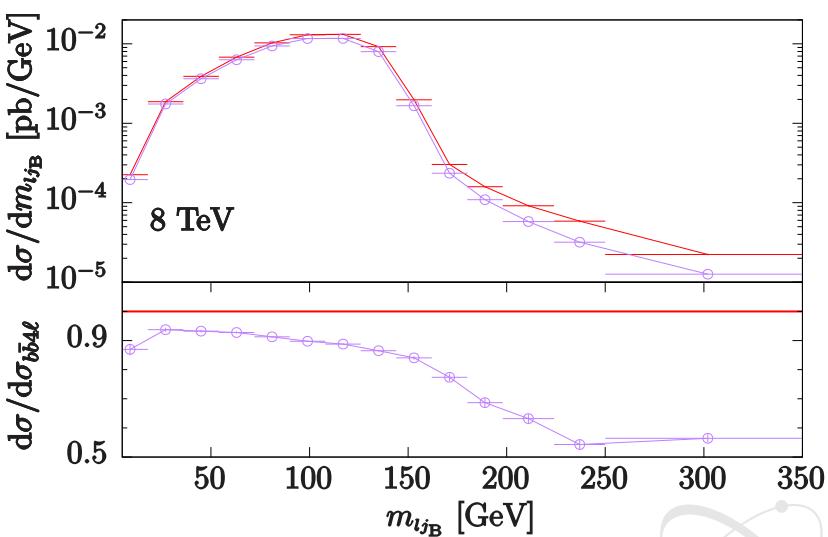
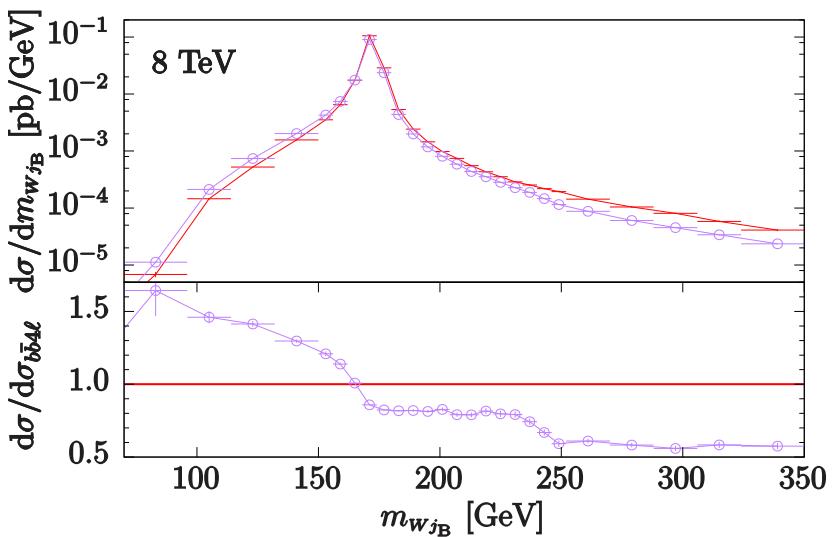
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  - ▶  $pp \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b}$  production at NLO (production and decay at NLO)
  - ▶ Radiation from FS  $b$ 's with ME (thanks to allrad)
  - ▶ No hadronic  $W$  decays, Includes  $Wt$  contribution

POWHEG-BOX-V2



# Impact of radiative corrections in top decays

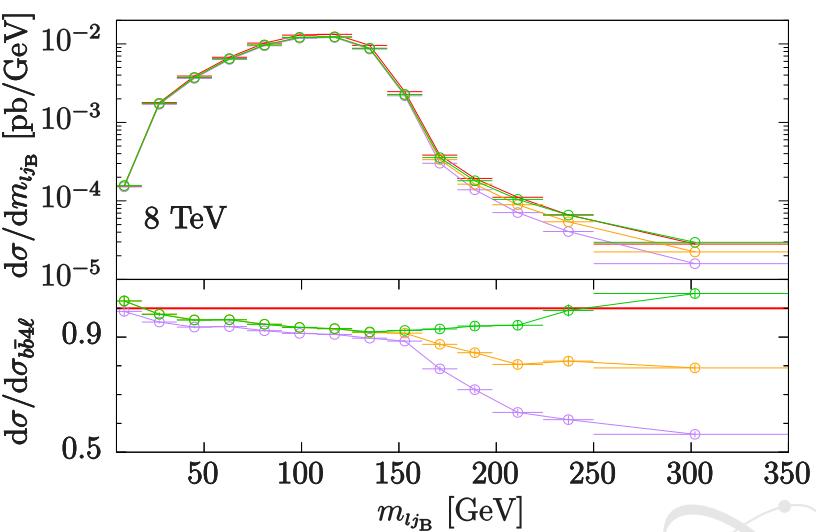
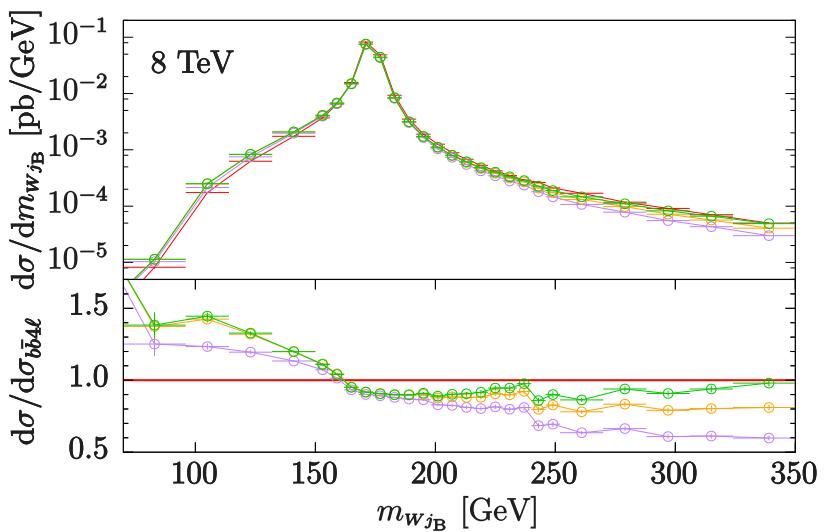
- $Wj_B$  and  $lj_B$  mass
  -  b\_bbar\_4l:  $pp \rightarrow \ell^+ \nu_\ell l^- \bar{\nu}_l b \bar{b}$ @NLO, allrad scheme
  -  hvq:  $t\bar{t}$  @NLO, decay @LO, no  $Wt$  contribution



we observe a dramatic difference, even a shift in the reconstructed top mass peak

# Impact of radiative corrections in top decays

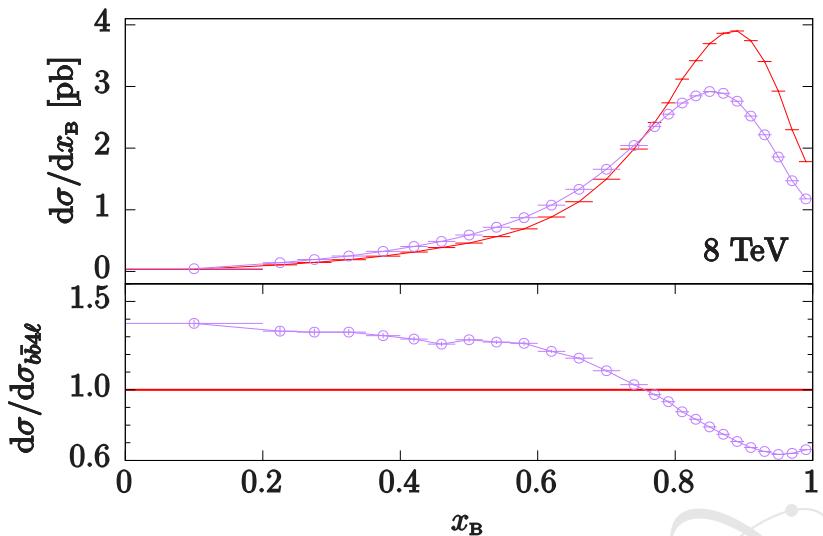
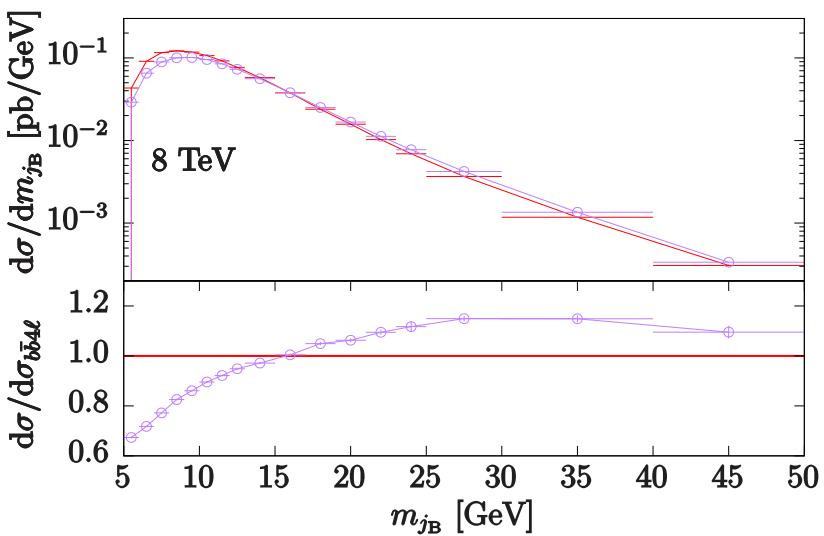
- $W j_B$  and  $l j_B$  mass
  -  b\_bbar\_4l:  $pp \rightarrow \ell^+ \nu_\ell l^- \bar{\nu}_l b \bar{b}$ @NLO, allrad scheme
  -  hvq:  $t\bar{t}$  @NLO, decay @LO, no  $Wt$  contribution
  -  hvq + ST\_wtch\_DS:  $tt$  &  $Wt$  @NLO,  $t$  decay @LO
  -  hvq + ST\_wtch\_DR:  $tt$  &  $Wt$  @NLO,  $t$  decay @LO



adding ST\_wtch to hvq improves the agreement,  
most notably in the tails

# Impact of radiative corrections in top decays

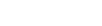
- $j_B$  mass and  $B$  fragmentation function
  -  b\_bbar\_4l:  $pp \rightarrow \ell^+ \nu_\ell l^- \bar{\nu}_l b \bar{b}$  @NLO, allrad scheme
  -  hvq:  $t\bar{t}$  @NLO, decay @LO, no  $Wt$  contribution

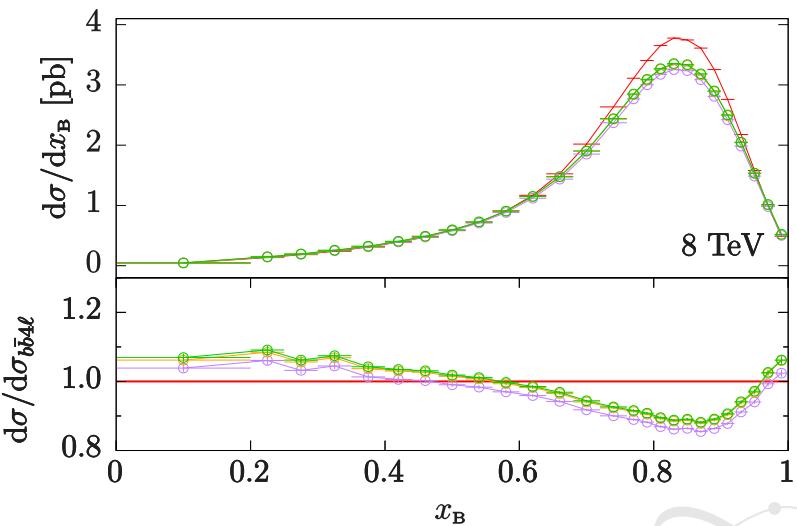
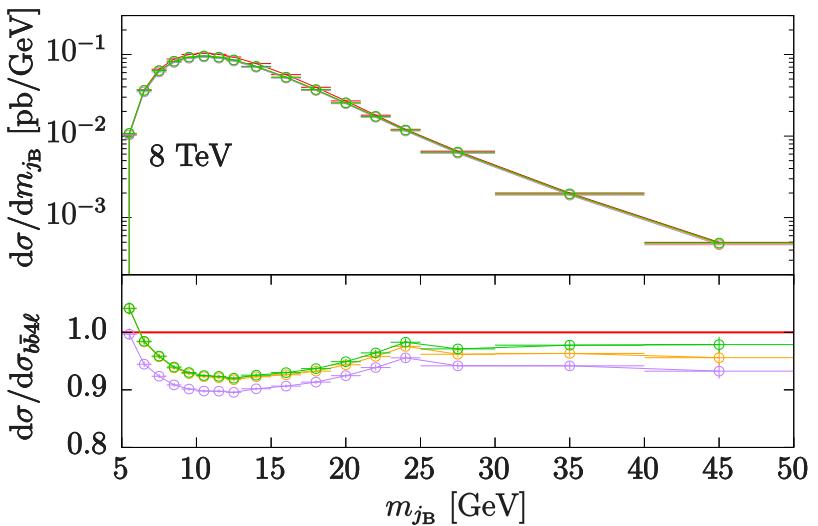


hvq predicts narrower  $b$ -jets and softer  $B$  fragmentation function

# Impact of radiative corrections in top decays

- $j_B$  mass and  $B$  fragmentation function

- ▶  b\_bbar\_4l:  $pp \rightarrow \ell^+ \nu_\ell l^- \bar{\nu}_l b \bar{b}$ @NLO, allrad scheme
- ▶  hvq:  $t\bar{t}$  @NLO, decay @LO, no  $Wt$  contribution
- ▶  hvq + ST\_wtch\_DS:  $tt$  &  $Wt$  @NLO,  $t$  decay @LO
- ▶  hvq + ST\_wtch\_DR:  $tt$  &  $Wt$  @NLO,  $t$  decay @LO

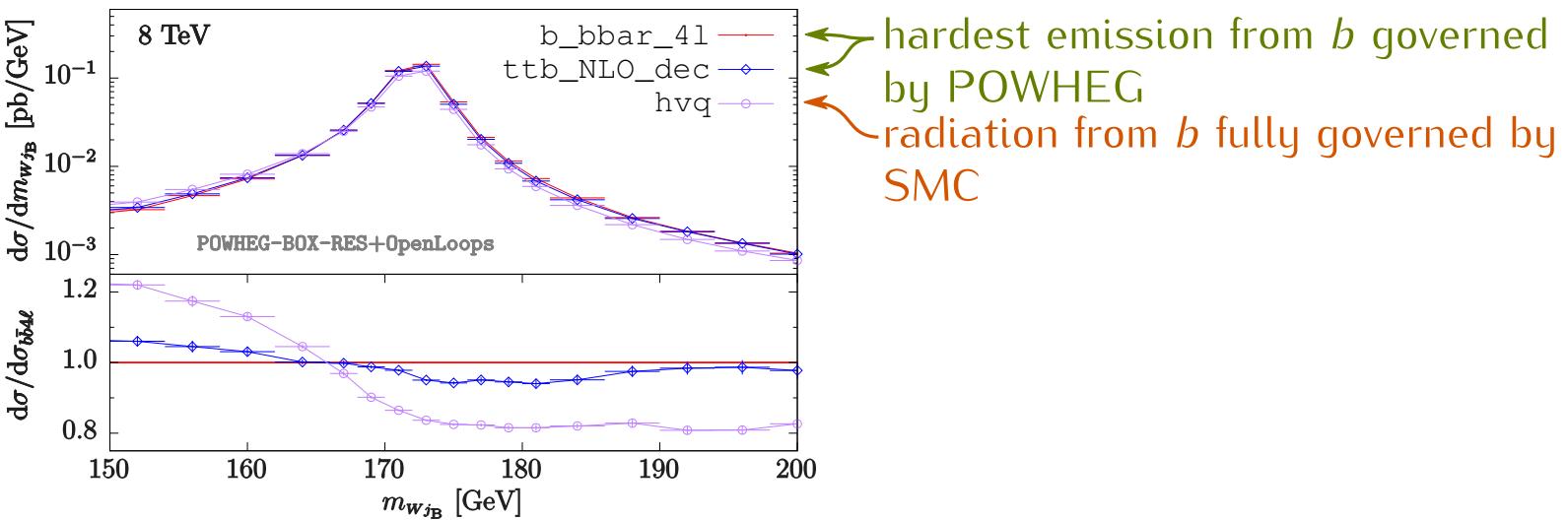


adding ST\_wtch to hvq does not affect the shape

† difference with respect to previous slide due to MPI

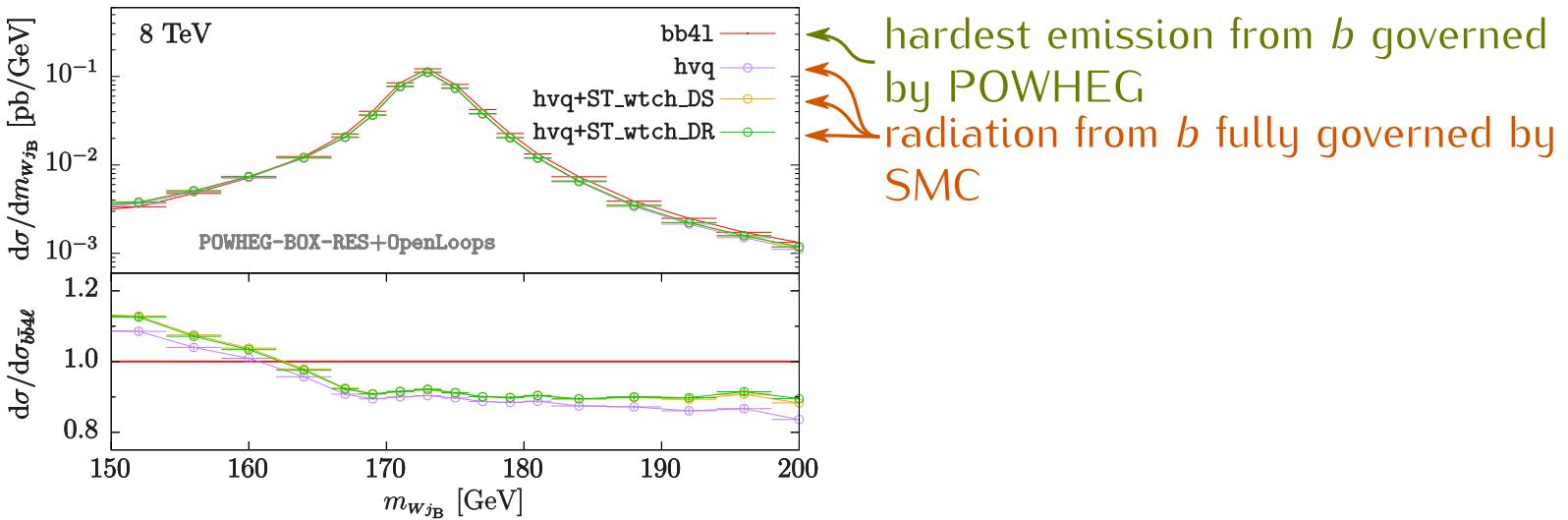
# Impact of radiative corrections in top decays

- In conclusion:
  - ▶ Radiative corrections in top decays have dramatic impact on  $b$ -jet description



# Impact of radiative corrections in top decays

- In conclusion:
  - ▶ Radiative corrections in top decays have dramatic impact on  $b$ -jet description



the difference in the shape around the peak due to treatment of hardest emission off  $b$ 's (adding ST\_wtch to hvq does not help)



# Summary and outlook

- Top quark plays a prominent part in the LHC physics program
  - ▶ Heaviest particle of the SM, playing crucial role in EWSB
  - ▶ Precise knowledge of  $m_T$  important for SM precision tests
  - ▶ Accurate Monte Carlos for top quark simulation indispensable
- Recent years saw tremendous progress:
  - ▶ In FO calculations reaching NNLO QCD + NLO EW precision in production, NNLO QCD in decay in NWA
  - ▶ First NLO QCD full off-shell calculations with top decay now also available
  - ▶ This culminated in NLO+PS matched Monte Carlo for top-pair and  $tW$  production including leptonic decay
- Comparisons with previous generation show:
  - ▶ Considerable differences in  $b$ -jet description
  - ▶ May this have an impact on top mass determination?

