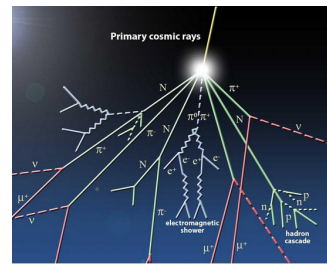
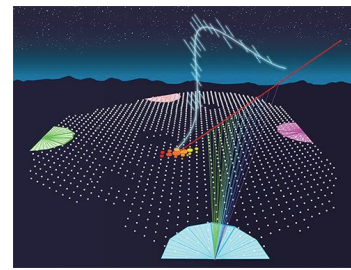


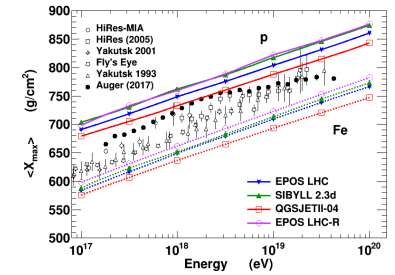
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+



=



# Decreasing systematic uncertainty of cosmic-ray mass through testing of models of hadronic interactions beyond LHC energies

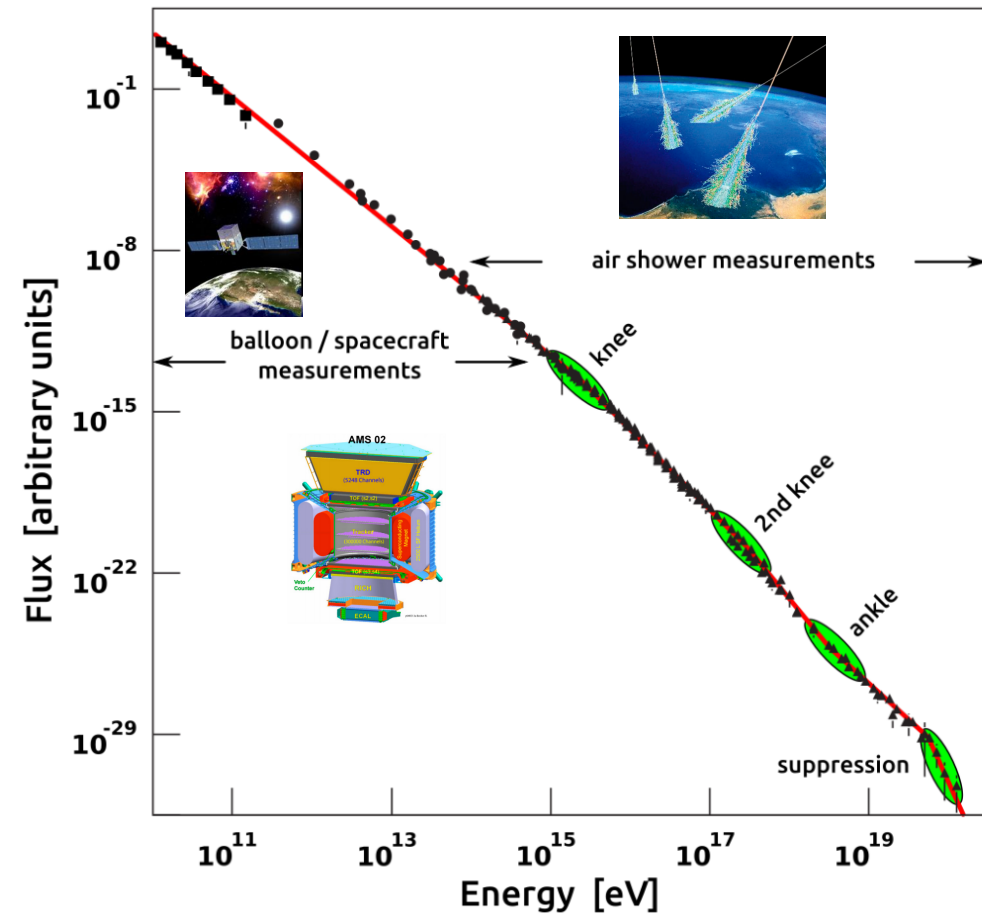
Jakub Vicha

vicha@fzu.cz

# Outline of the talk

- very brief introduction into cosmic rays and air showers
- review of tests of models of hadronic interactions using air-shower data
  - muon problem in air-shower simulations
- recent reveal of a new problem in air-shower modelling regarding the depth of shower maximum ( $X_{\max}$ )
- consequences of this new phenomenon
  - air-shower modelling
  - cosmic-ray physics

# Cosmic rays

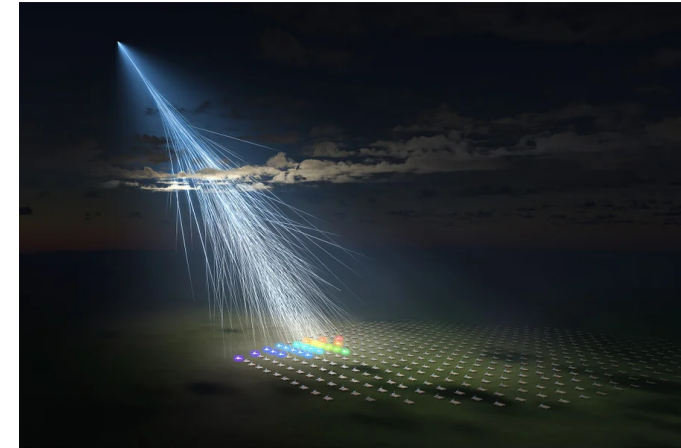


1 particle/m<sup>2</sup>/second

1 particle/m<sup>2</sup>/year

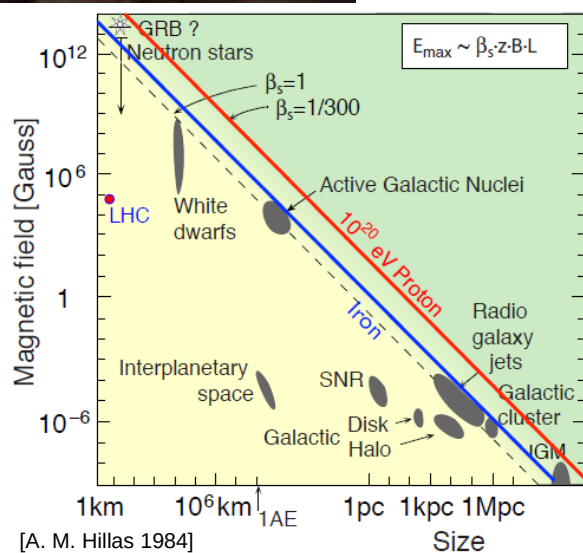
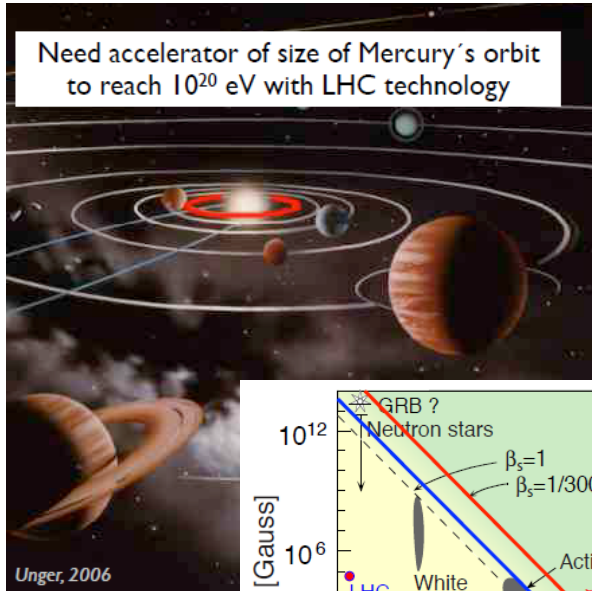
1 particle/km<sup>2</sup>/century

- above  $\sim 1$  PeV, only indirect measurements using air showers
  - energy (spectral features)
  - mass (H...Fe... nuclei)
  - direction (anisotropies)

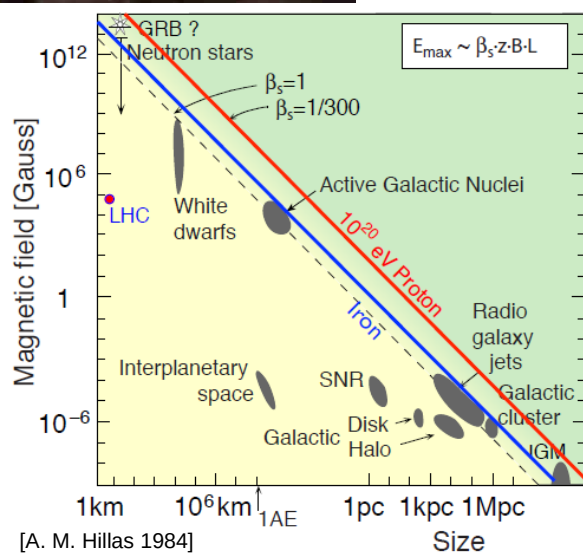
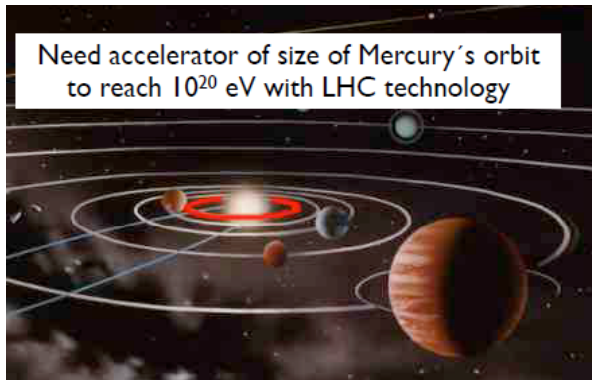


# Persisting mystery beyond $10^{20}$ eV

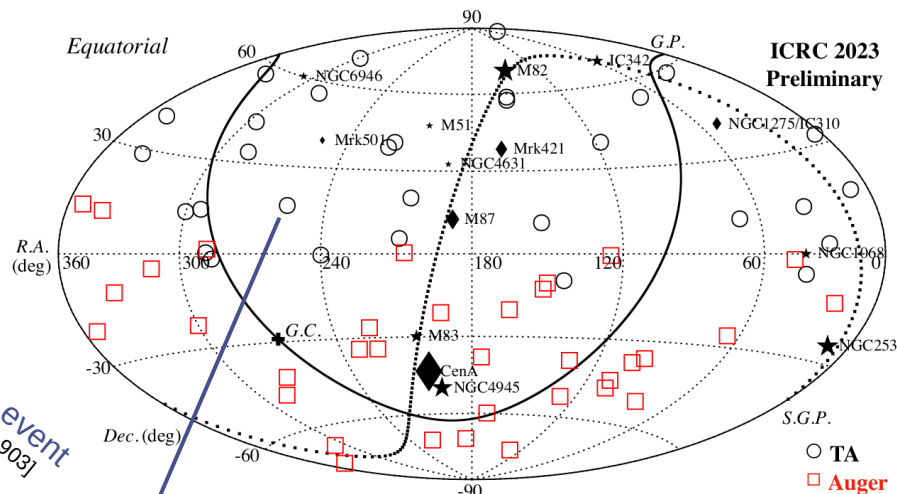
Need accelerator of size of Mercury's orbit to reach  $10^{20}$  eV with LHC technology



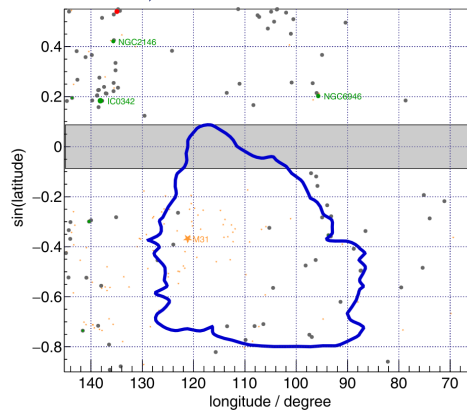
# Persisting mystery beyond $10^{20}$ eV



The most energetic event  
[TA Coll., Science 382 (2023) 903]



[T. Fujii, PoS(ICRC2023)031]



Backtracking even as Fe in the Galactic magnetic field does not point to any obvious source candidate

[M. Unger, G. Farrar, ApJL 962 (2024) L5]

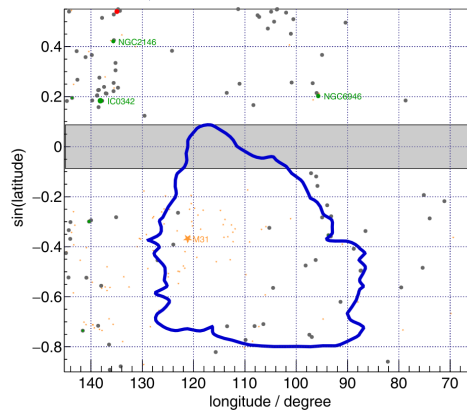
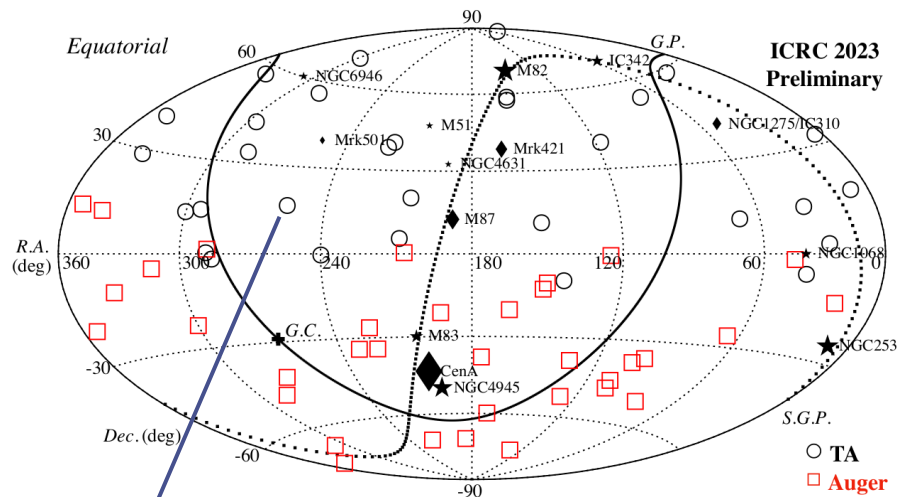
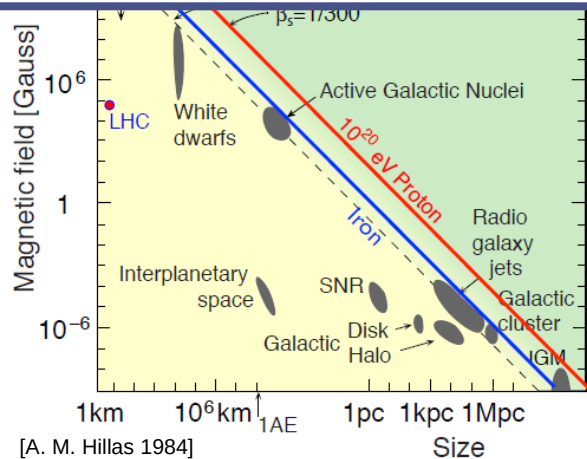
Are UHECR transients ???

● 2MASS galaxies    ★ local galaxies    ● Swift-BAT AGNs    ● radio galaxies    ● starburst galaxies    ■ Amaterasu localization

# Persisting mystery beyond $10^{20}$ eV

Need accelerator of size of Mercury's orbit to reach  $10^{20}$  eV with LHC technology

**Cosmic-ray mass is the key to understand !**



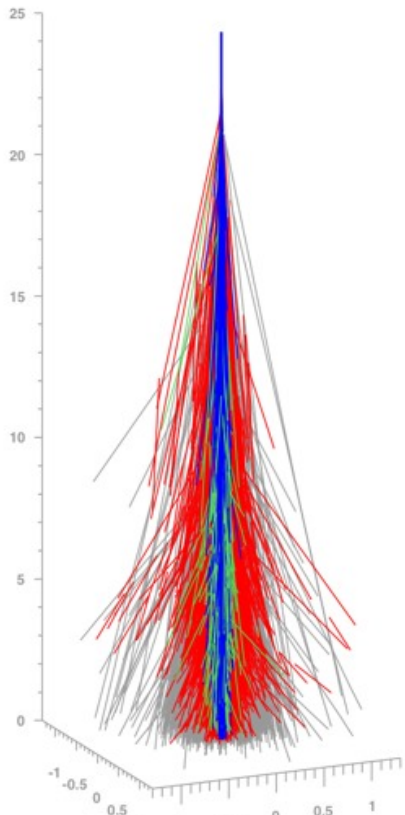
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[M. Unger, G. Farrar, ApJL 962 (2024) L5]

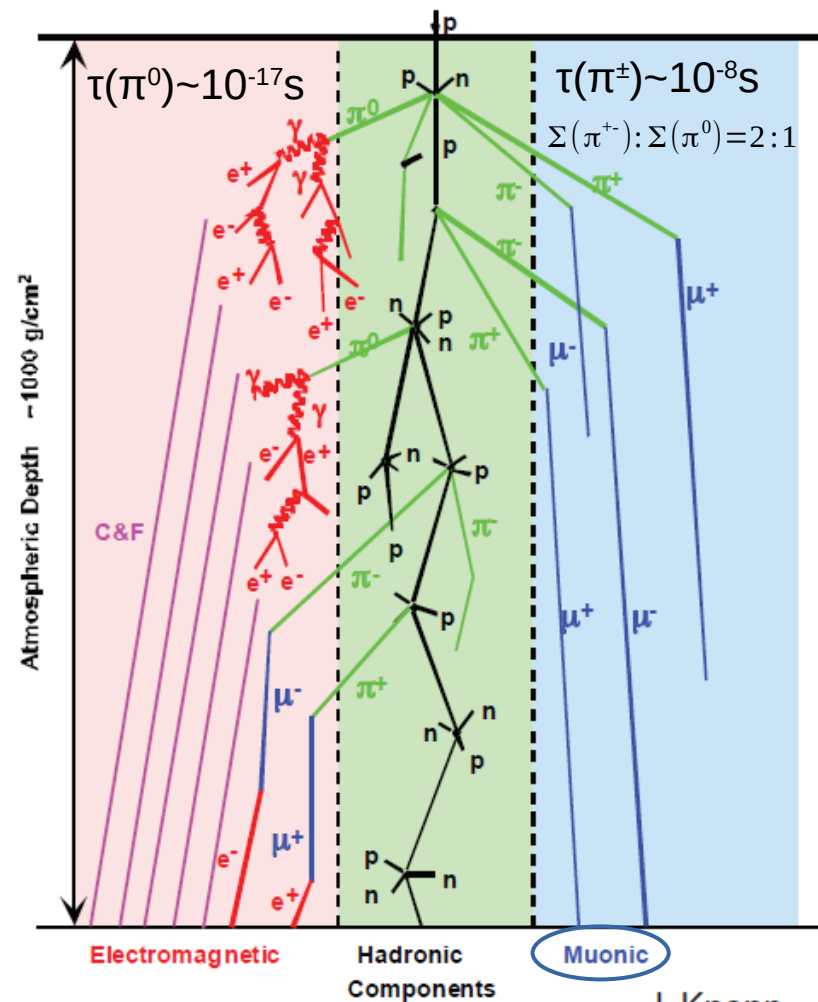
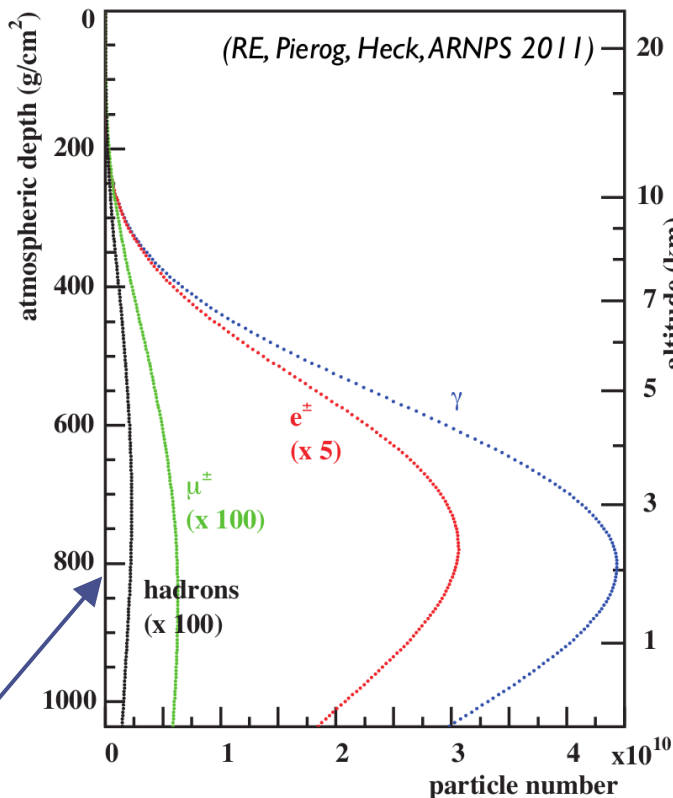
Are UHECR transients ???

● 2MASS galaxies    ★ local galaxies    ● Swift-BAT AGNs    ● radio galaxies    ● starburst galaxies    ■ Amaterasu localization

# Air shower development



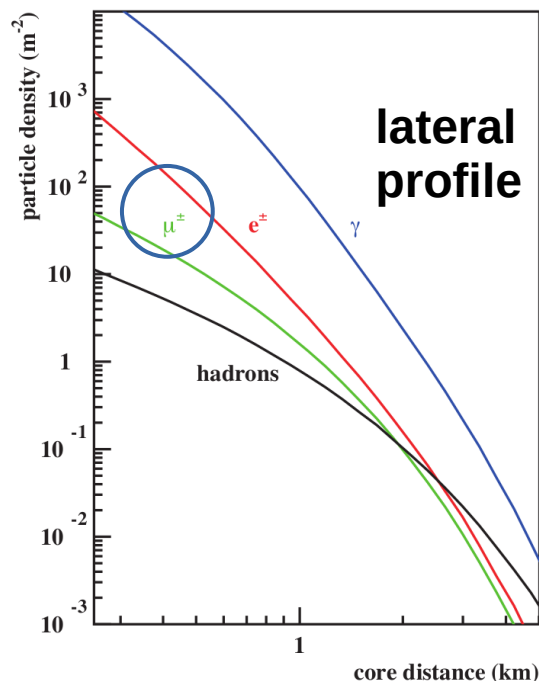
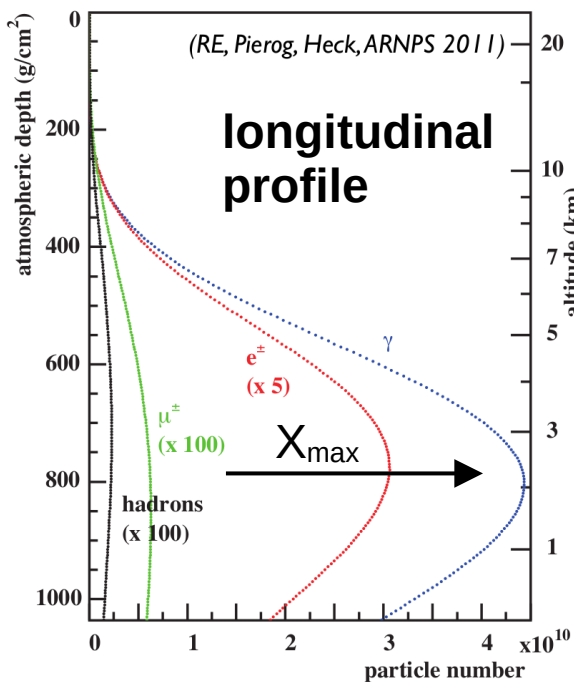
$X_{\max}$



J. Knapp

# Hadronic interactions in air showers

- depth of shower maximum ( $X_{\max}$ )
  - number of muons  $N_{\mu}$  (decays of  $\pi^{\pm}$ )
- } sensitive to primary mass **A**
- extrapolated to higher energies and different kinematic regions than accessible
- large systematic uncertainty on interpreted *mass composition*



$$X_{\max}(A) \approx X_0(E_0/A) + \lambda_r \ln[\xi_c^e E_0/A] - \lambda_r \ln[3 N_{ch}(E_0/A)]$$

$$N_{\mu}(A) \approx [\xi_c^{\pi} E_0/A]^{\beta}, \quad \beta \approx 0.9$$

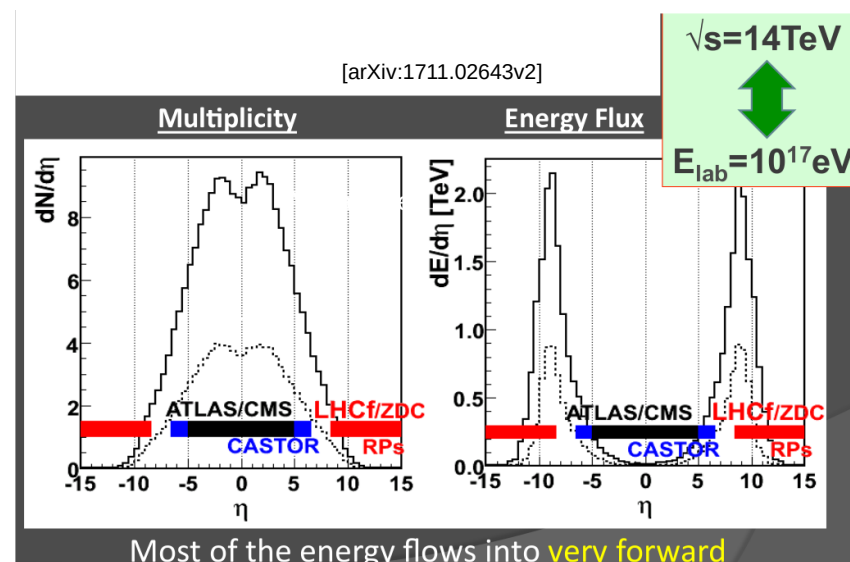
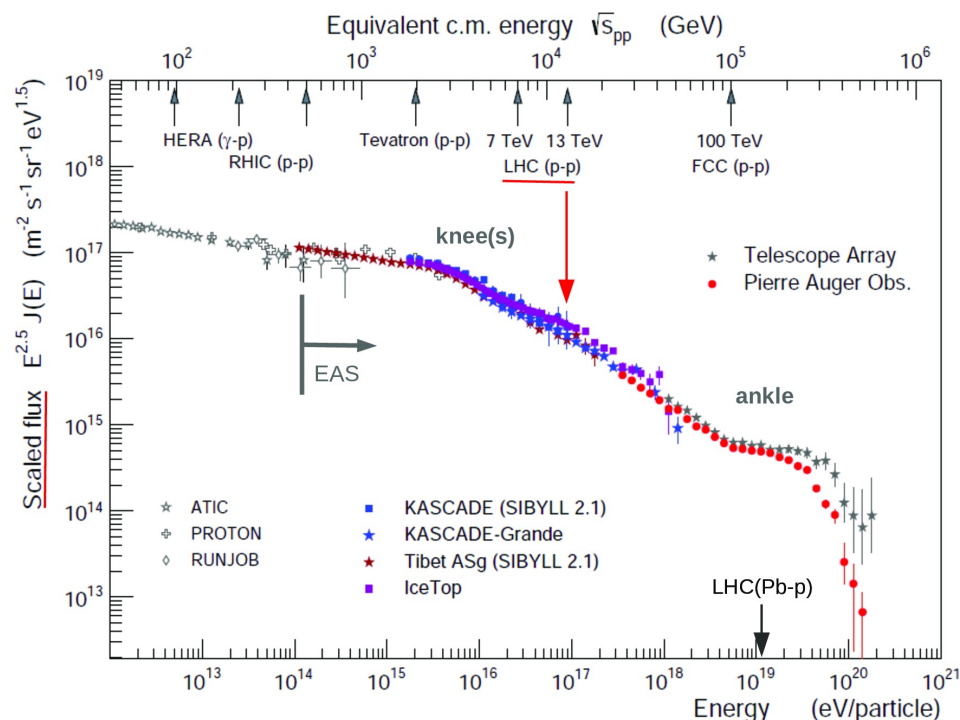
[Astropart. Phys. 22 (2005) 387]

- **$X_{\max}$**  measurable in fluorescence telescopes
  - precise, low duty cycle
- **Muons** measurable in surface detectors
  - em contamination, full duty cycle



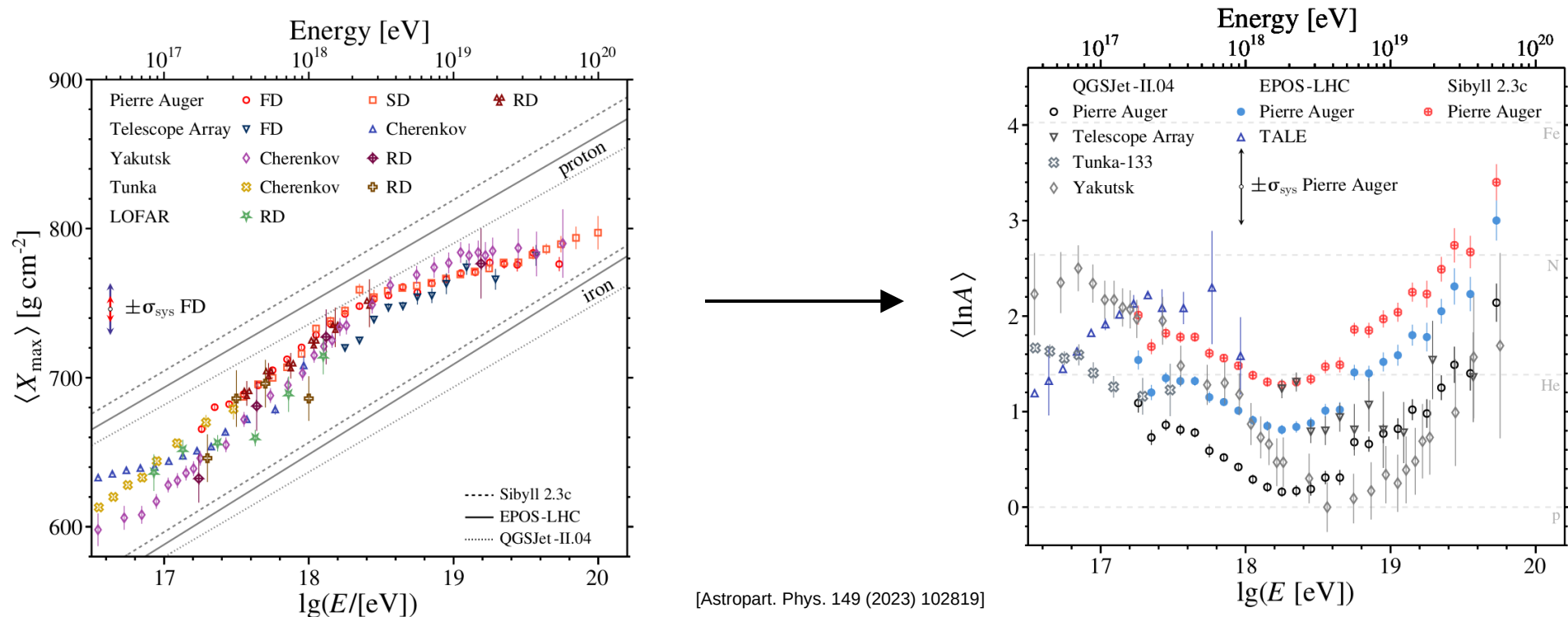
# Hadronic interactions in air showers

- depth of shower maximum ( $X_{\max}$ )
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- } sensitive to primary mass  $A$
- extrapolated to higher energies and different kinematic regions than accessible
- ➔ large systematic uncertainty on interpreted *mass composition*



# Mass composition of cosmic rays

- our knowledge is dominated by unknown systematic uncertainty of  $X_{\max}$  predicted from air-shower modelling ( $> 20 \text{ g/cm}^2$ ), compared to experimental systematics ( $\sim 10 \text{ g/cm}^2$ )

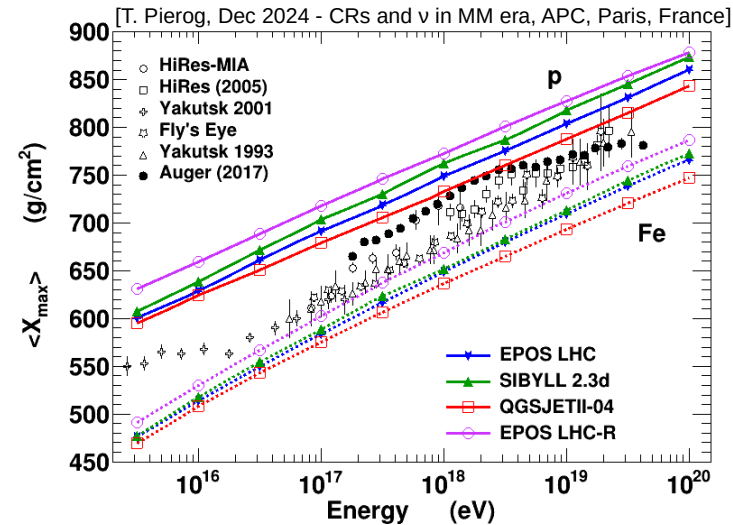
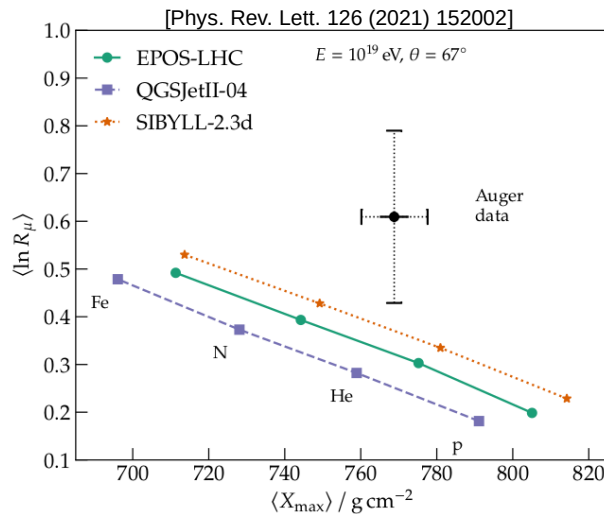


[Astropart. Phys. 149 (2023) 102819]

# Testing models of hadronic interactions

Are measured data bracketed by model predictions for protons and iron nuclei ?

The key is the consistency of observables in the interpreted mass composition at given reconstructed energy (!)

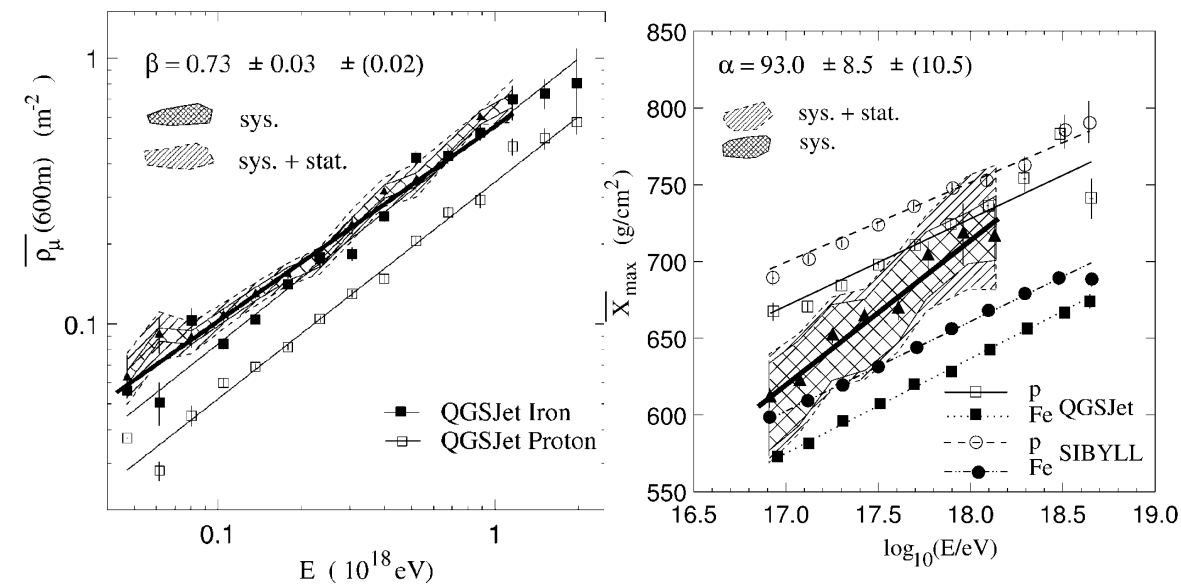


**Current models of hadronic interactions available for tests:**  
*EPOS-LHC (LHCR), QGSJet II-04 (III), Sibyll 2.3d (\*)*

# First indications of a problem to consistently describe data

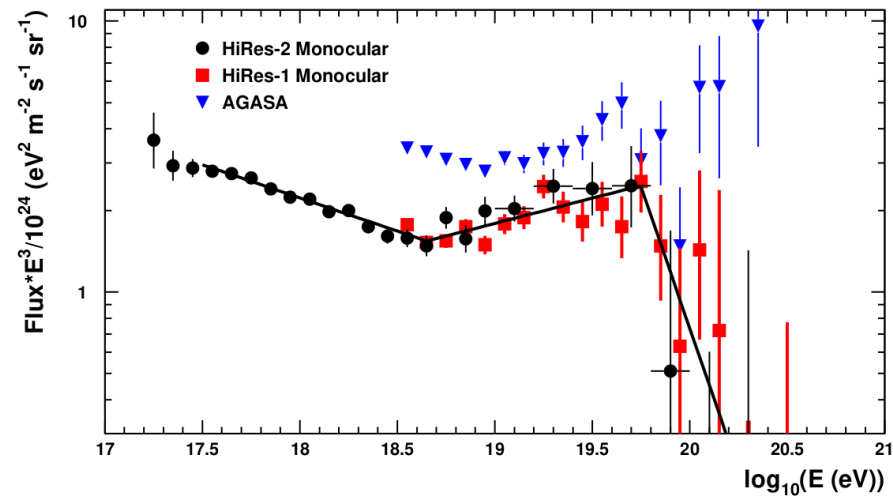
## HiRes-MIA experiment

[Phys. Rev. Lett. 84 (2000) 4276]

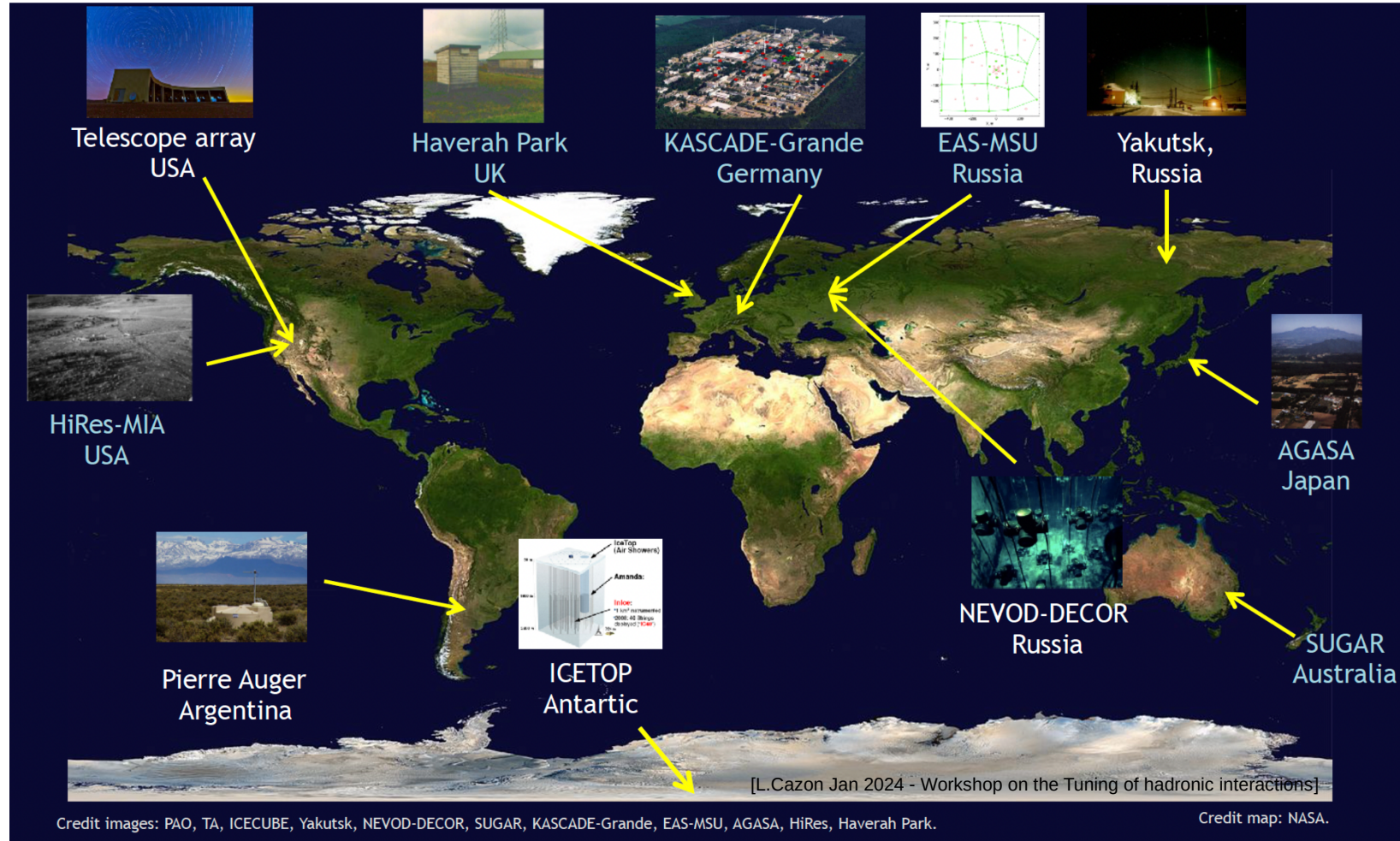


## Energy estimation from muon content at AGASA

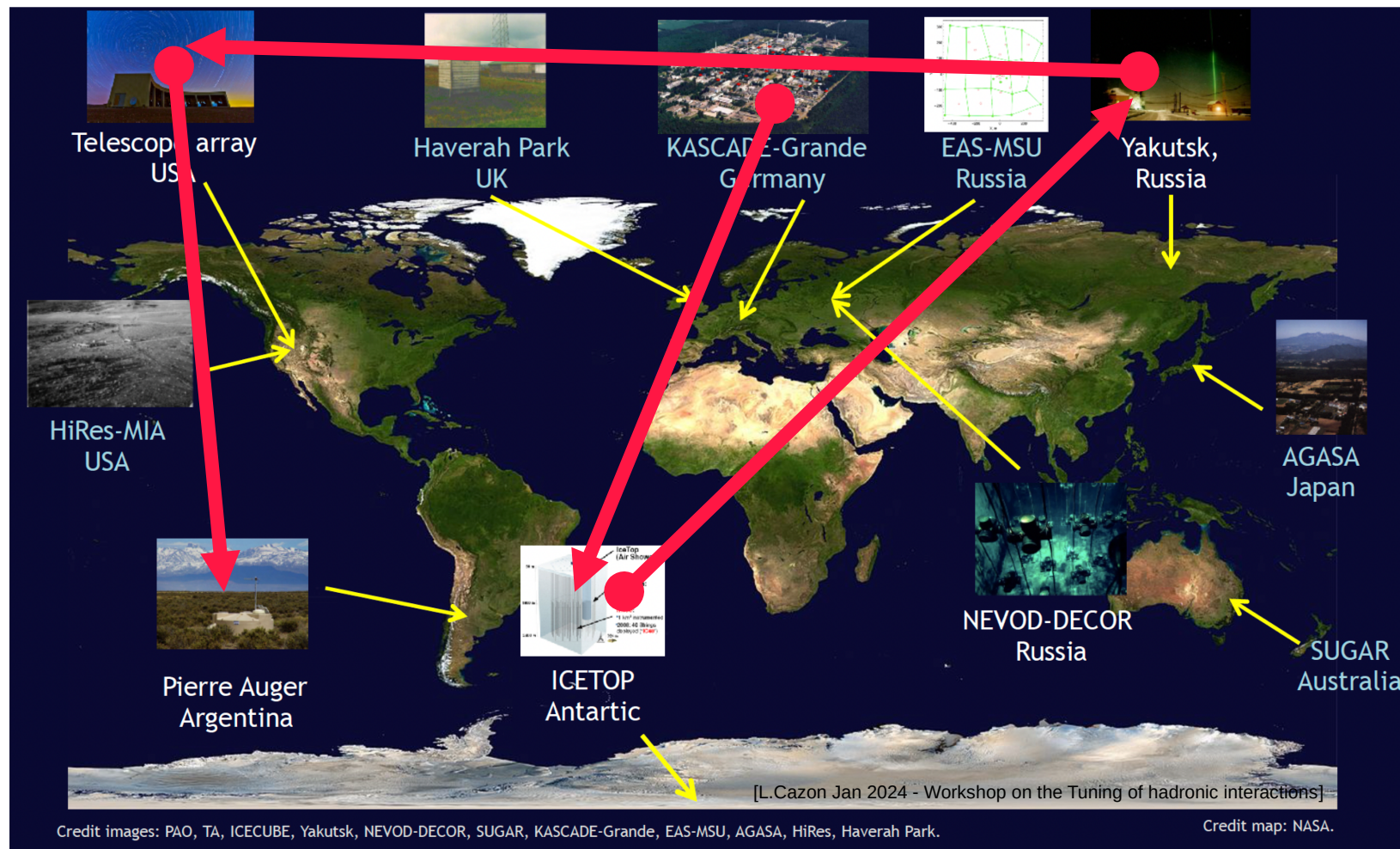
[Phys. Rev. Lett. 100 (2008) 101101]



# Selected past and current air-shower experiments

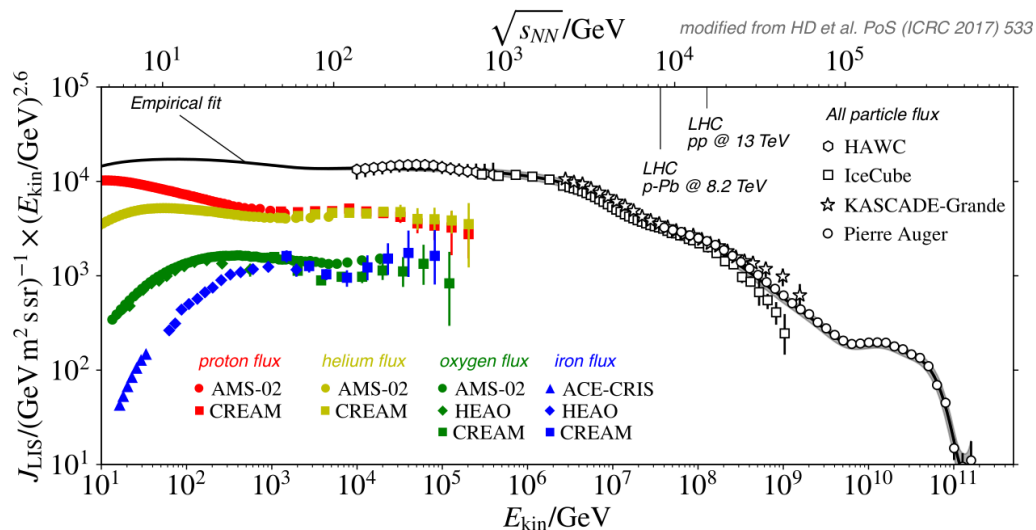
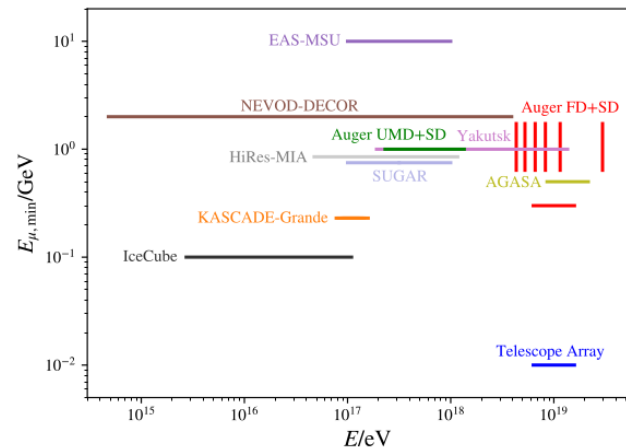
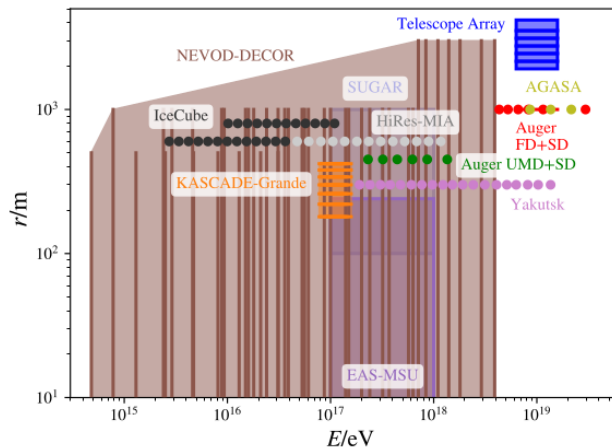
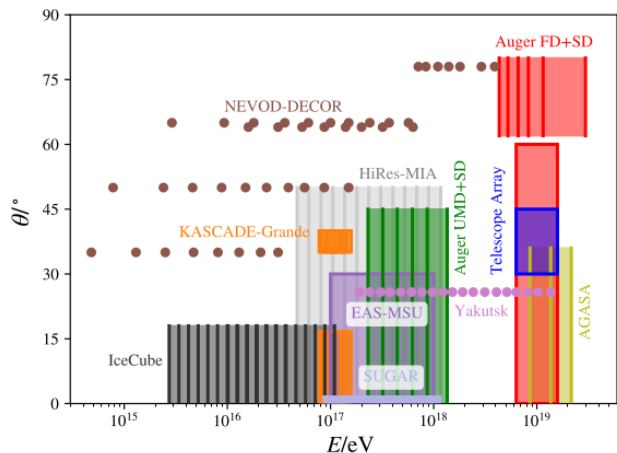


# This talk: “Short tour towards higher energies“



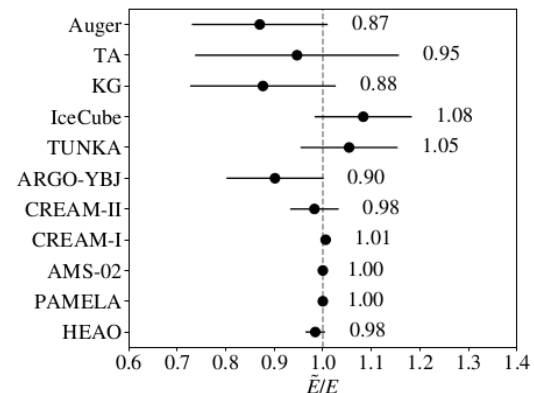
# Differences in measurements

[Astrophys. Space Sci. 367 (2022) 3]



[PoS(ICRC2017)533]

## Global Spline Fit (GSF)

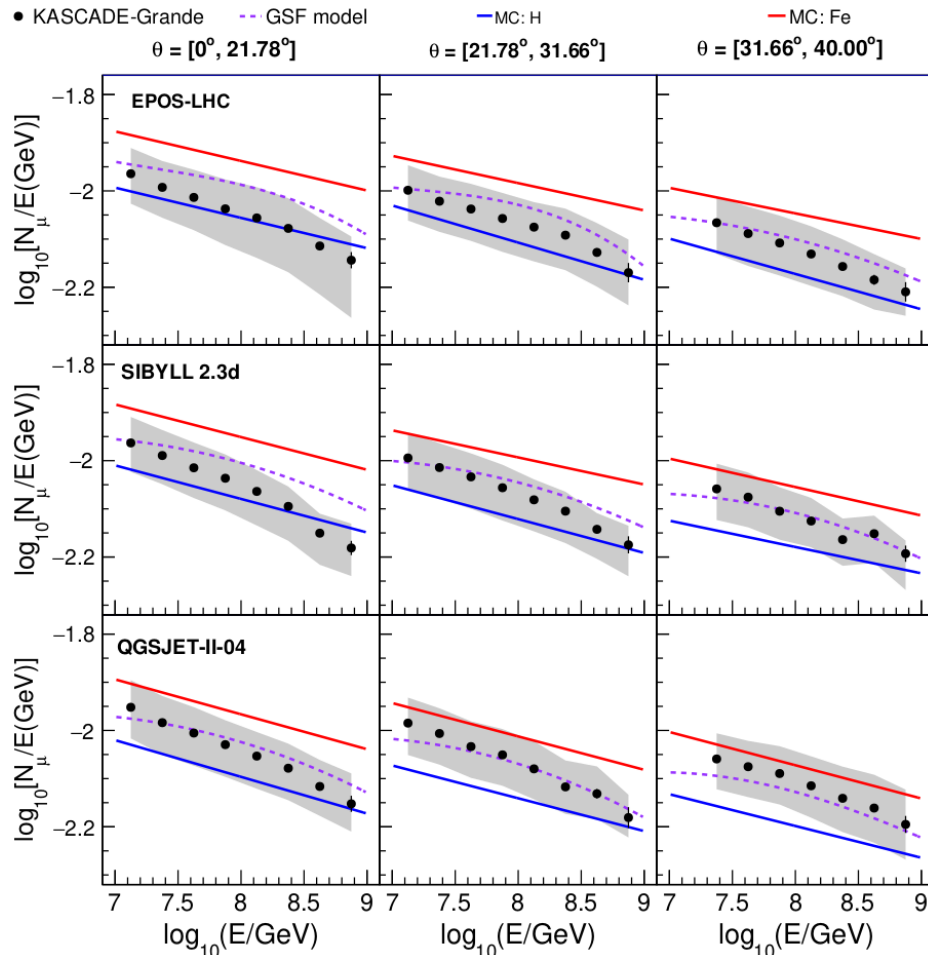
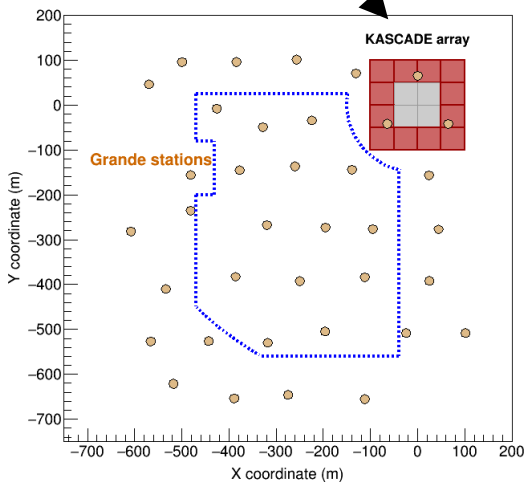


# Muons at KASCADE-Grande

[PoS(ICRC2023)376]



$E_\mu > 230$  MeV



Better consistency at larger zenith angles (higher muon energy)  
 → too steep muon spectra in models?

Caveat: energy scale of the Pierre Auger Observatory, GSF mass-composition model



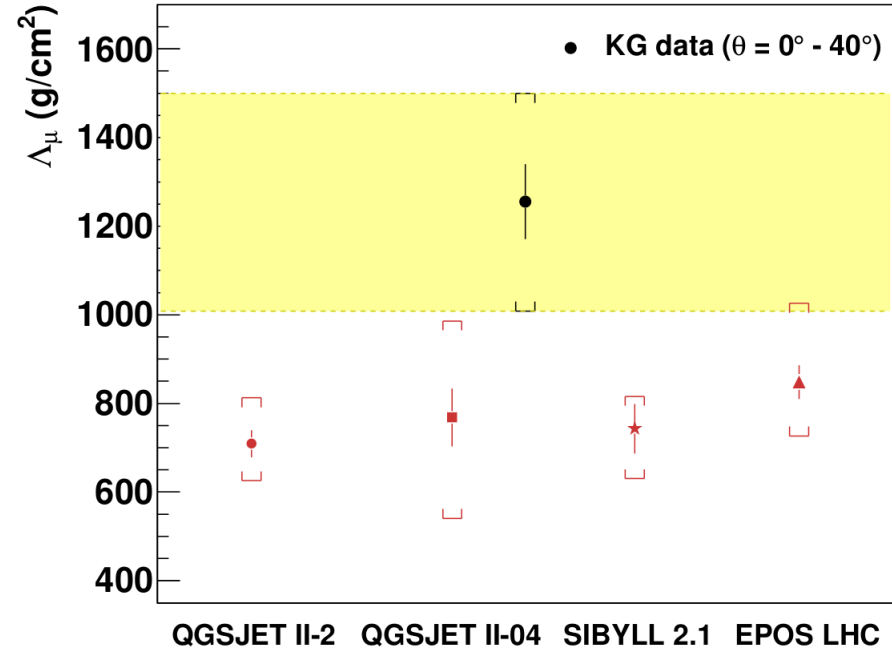
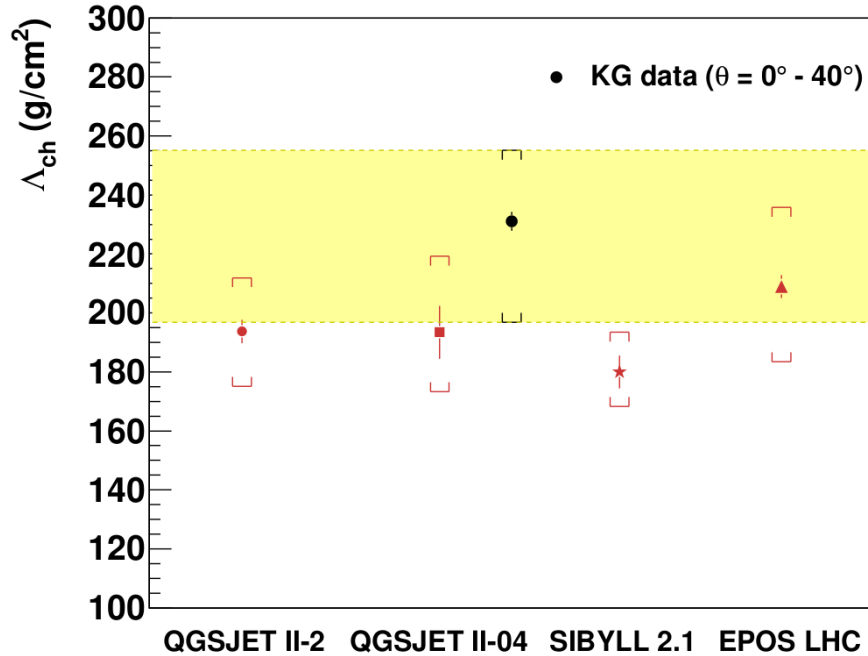
# Signal attenuation at KASCADE-Grande

$10^{16.3-17.0}$  eV

$E_\mu > 230$  MeV

[Astropart. Phys. 95 (2017) 25]

$$N_\mu(\theta) = N_\mu^0 e^{-X_0 \sec \theta / \Lambda_\mu}$$



Attenuation of all charged particles consistent between data and models

Attenuation of muons in  $1-2\sigma$  tension between data and models

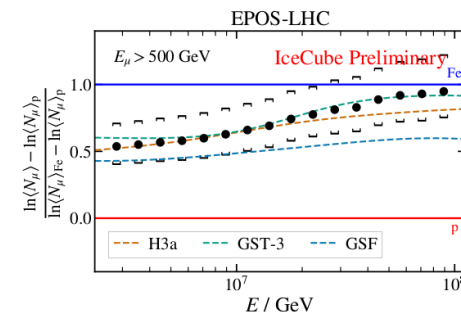
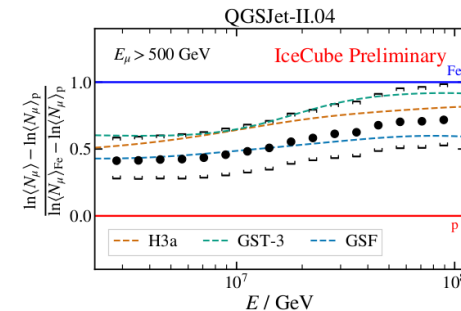
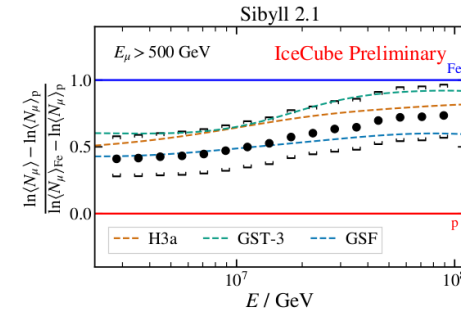
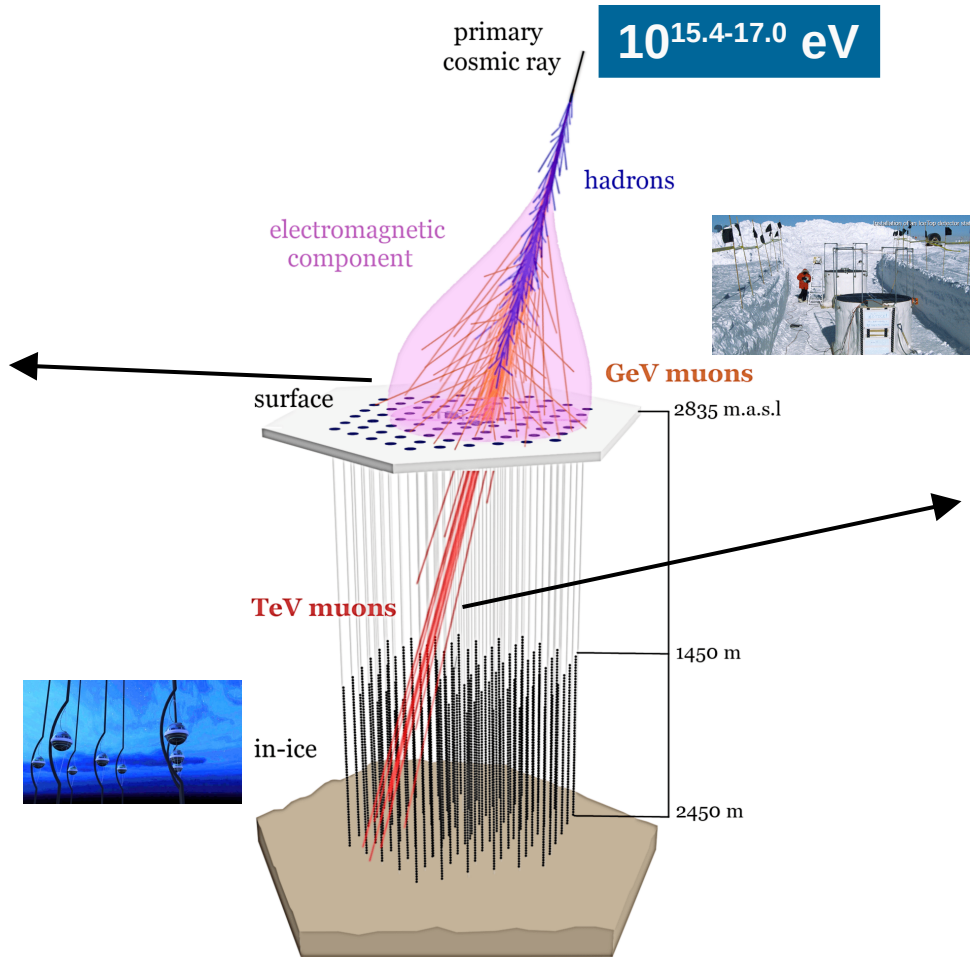
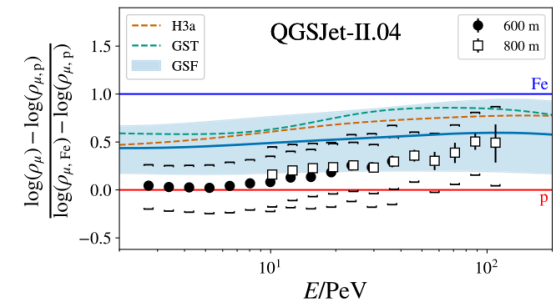
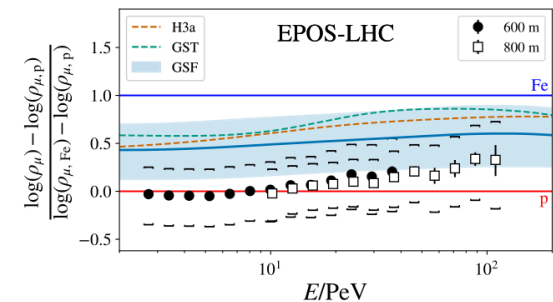
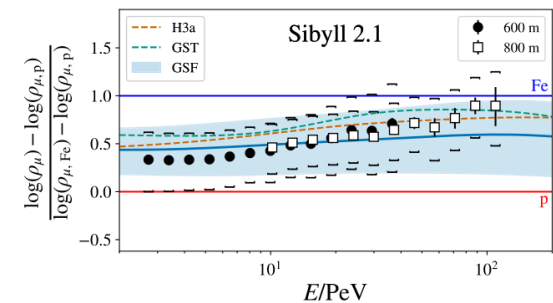
→ harder muon spectra in data

# IceCube + IceTop: measurements of GeV and TeV muons

[Phys. Rev. D 106 (2022) 032010]

**10<sup>15.4-17.0</sup> eV**

[PoS(ICRC2023)207]



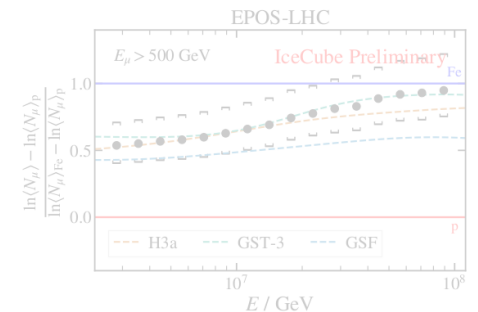
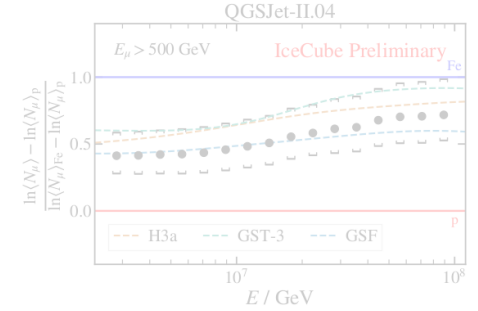
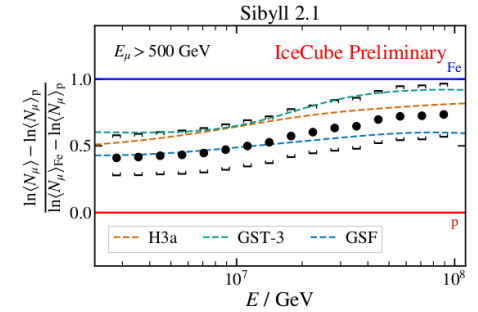
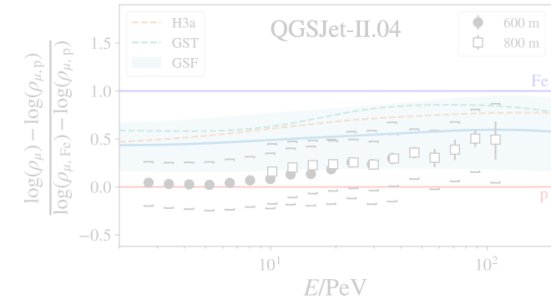
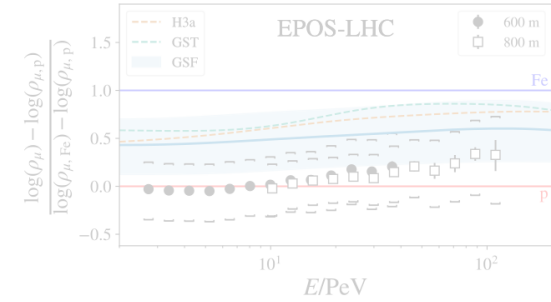
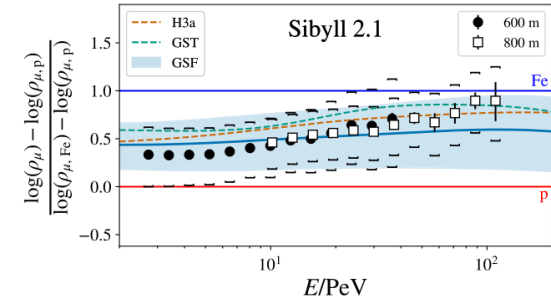
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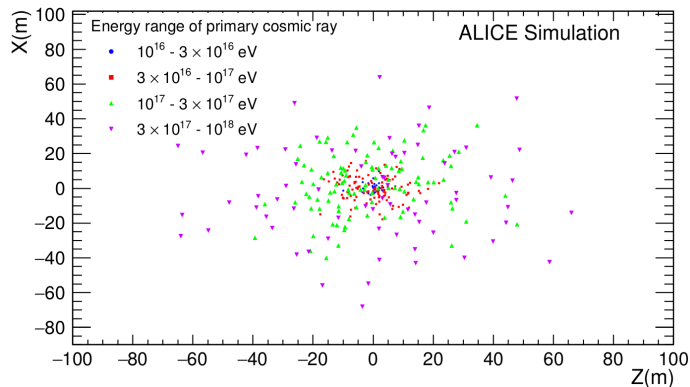
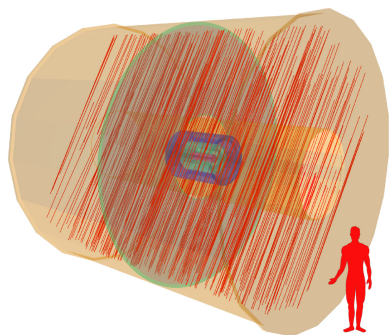
The most consistent description using pre-LHC model !



# Muon bundles

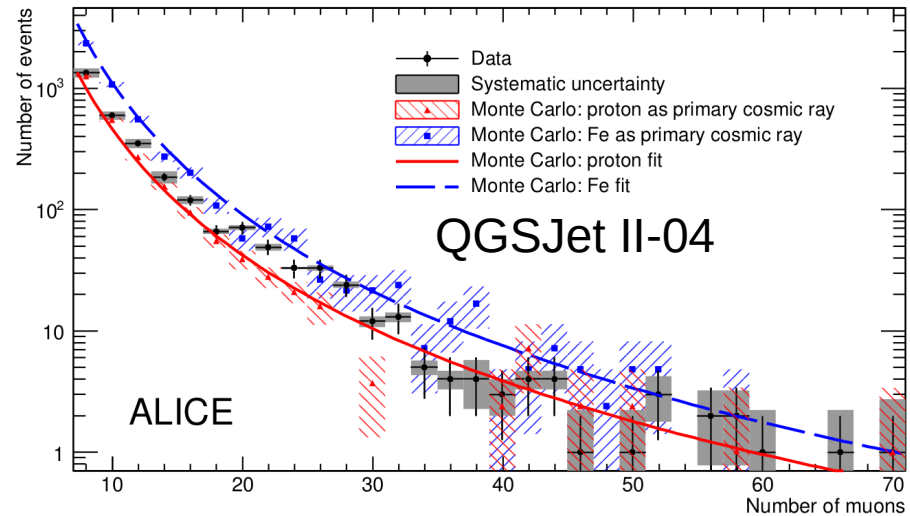
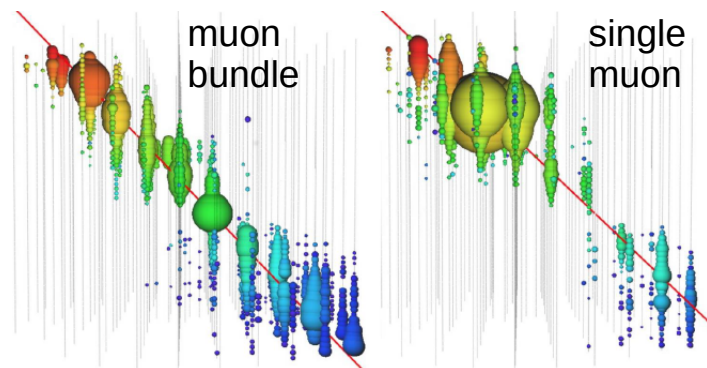
ALICE

[JCAP 01 (2016) 032]



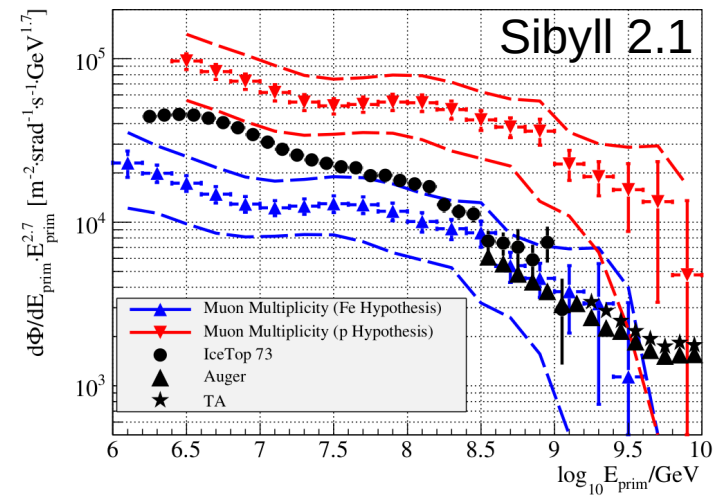
IceCube

[Astropart. Phys. 78 (2016) 1]



• no tension observed so far

• what about all new models and more statistics?

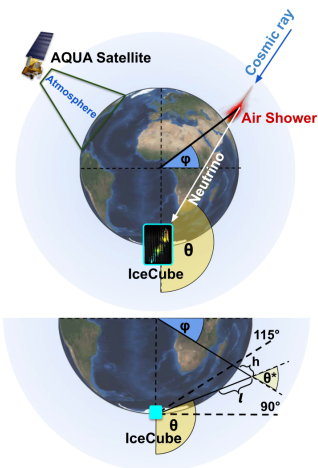


# Correlation of IceCube neutrino flux with $\Delta T$

$< 10^{15}$  eV

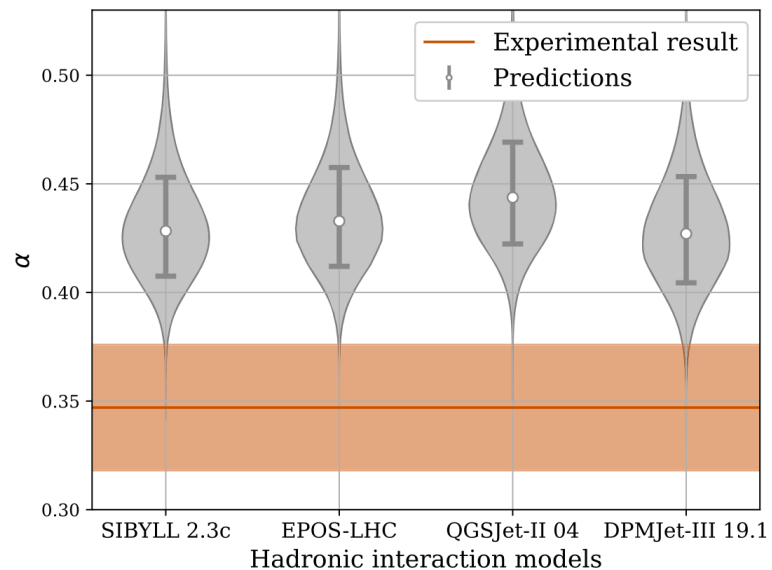
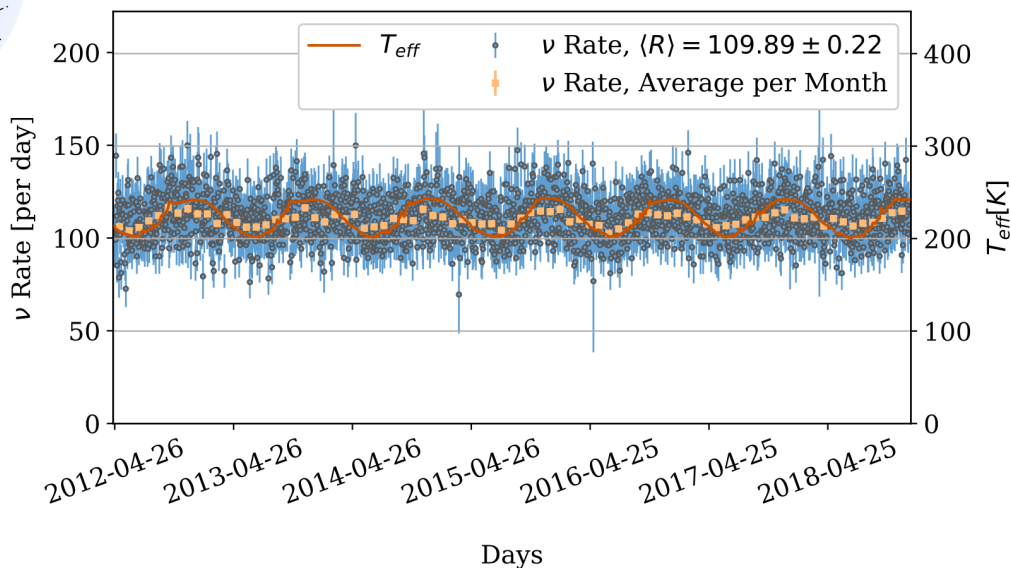
$E_\mu \approx \text{TeV}$

[Eur. Phys. J. C 83 (2023) 777]



- effective air temperature ( $T_{\text{eff}}$ ) measured by AQUA satellite
- 262,846  $\nu_\mu$  track events  $\sim 200\text{-}7700$  GeV

$$\frac{R(t) - \bar{R}}{\bar{R}} = \alpha \frac{T_{\text{eff}}(t) - \bar{T}_{\text{eff}}}{\bar{T}_{\text{eff}}}$$

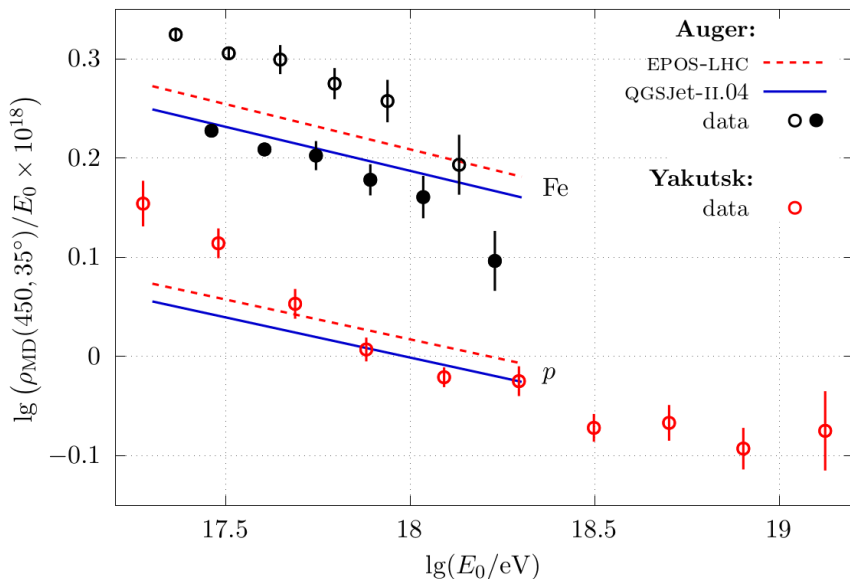


$\alpha$	LLH	$\chi^2$
Exp. result	$0.347 \pm 0.029$	$0.357 \pm 0.030$
MCEq	$0.424 \pm 0.038$	$0.424 \pm 0.039$
Analytic Appr.	$0.429 \pm 0.038$	$0.439 \pm 0.039$
Kaons only	$0.278 \pm 0.076$	
Pions only	$0.637 \pm 0.099$	

$\sim 2\text{-}3\sigma$  tension  $\rightarrow$  larger kaon contribution to the neutrino flux ?

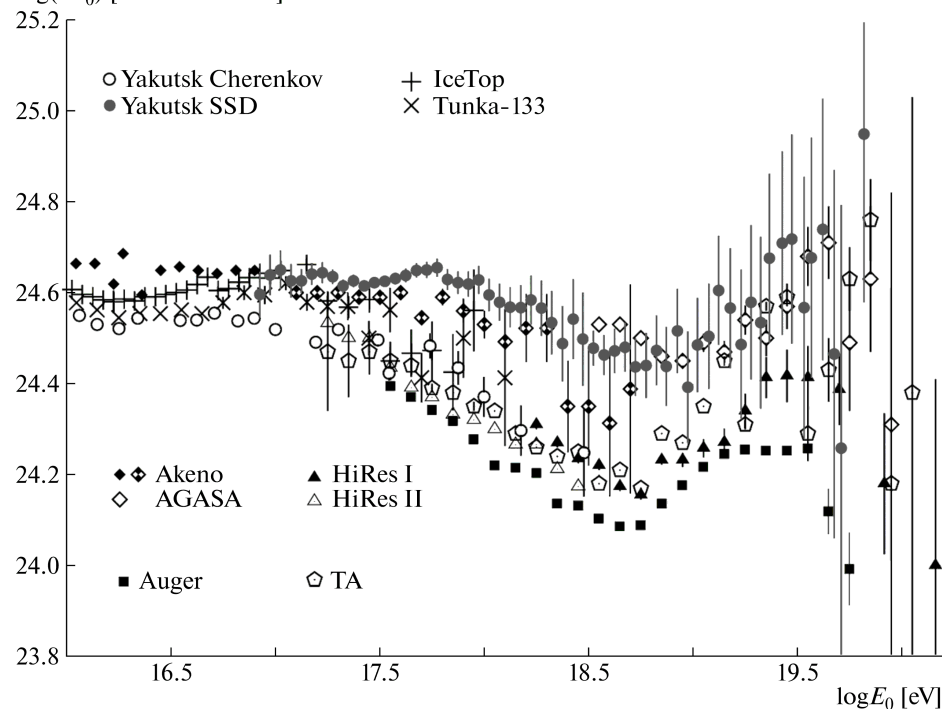
# Muon density at Yakutsk

[JETP Lett. 117 (2023) 645]



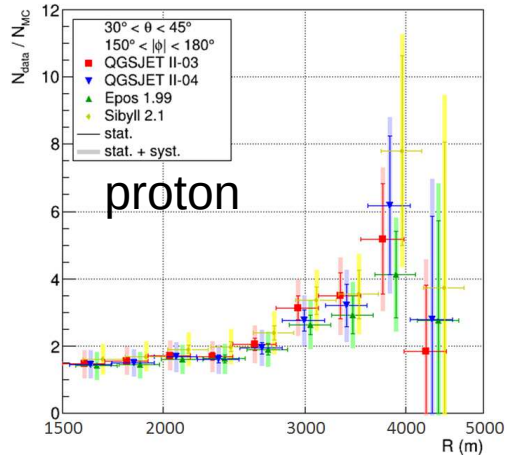
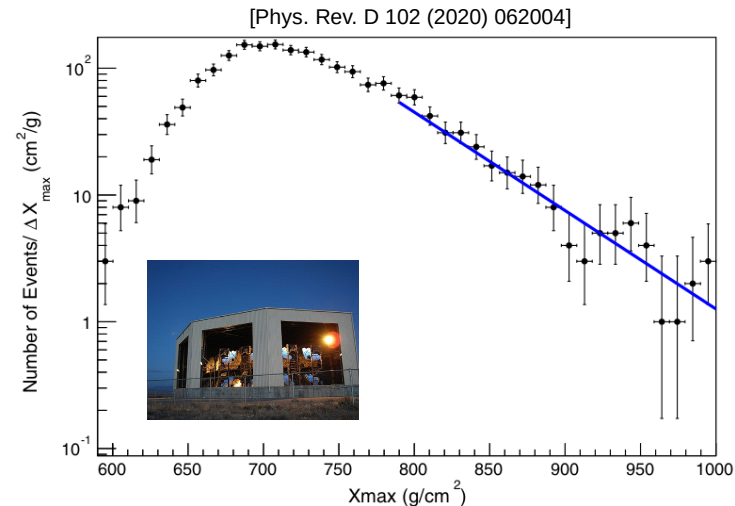
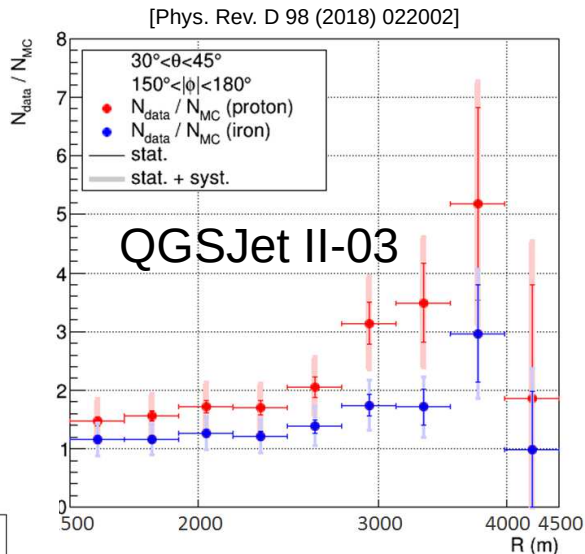
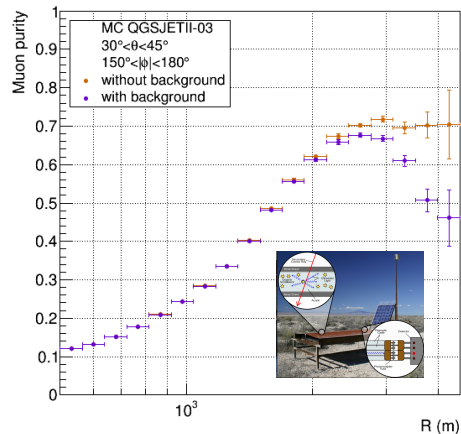
$\log(JE_0^3)$  [ $\text{m}^{-2} \text{s}^{-1} \text{sr}^{-1} \text{eV}^2$ ]

[Physics of Atomic Nuclei, 81 (2018) 575]

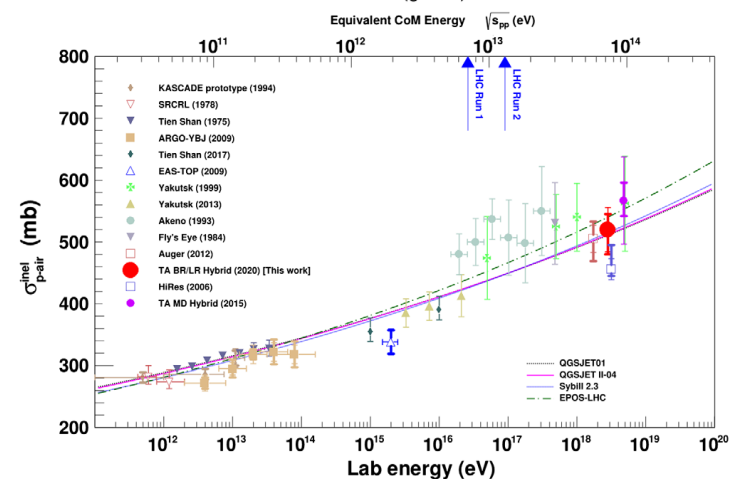


- no muon deficit and compatible with protons (excluded by Auger)
  - consequence of a difference in the energy scale ?

# Tests at Telescope Array



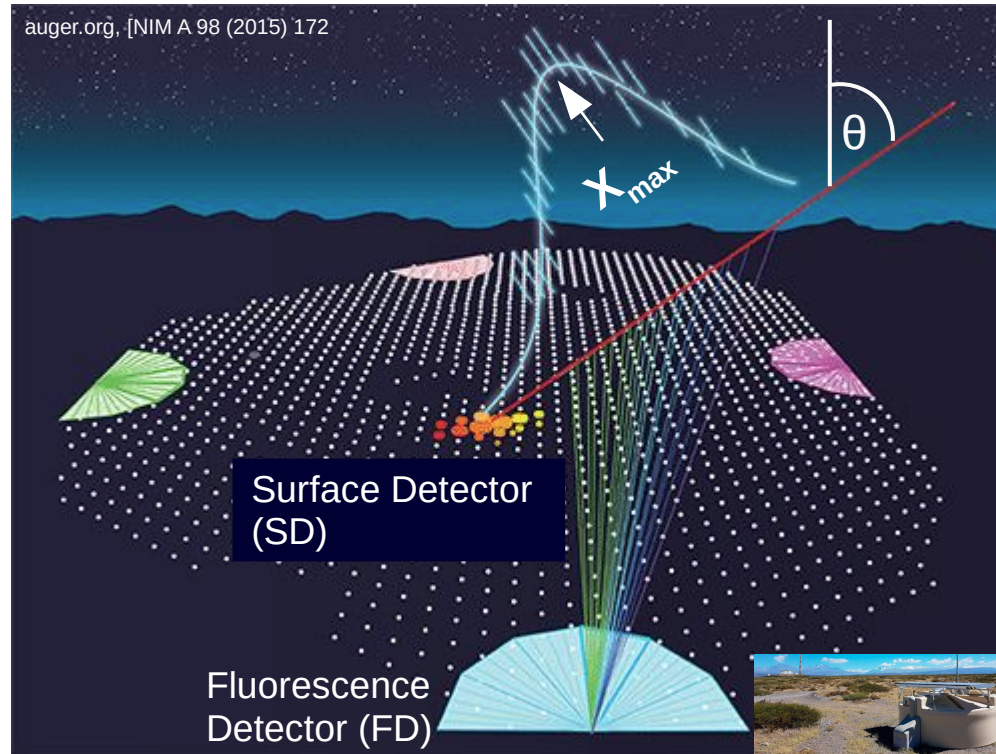
- tension with data in muons
- p-air cross-section consistent with models



# The Pierre Auger Observatory - *the best instrument to study hadronic interactions above $\sqrt{s} \approx 50$ TeV*

## SD signal

- **muon content**
  - from buried scintillators,  $\theta < 45^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$
- **muon production depth**
  - for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$
- **muon energy spectrum**
  - from attenuation with  $\theta$  and  $r$
- **rise time** of signal vs.  $r$



## FD longitudinal profile

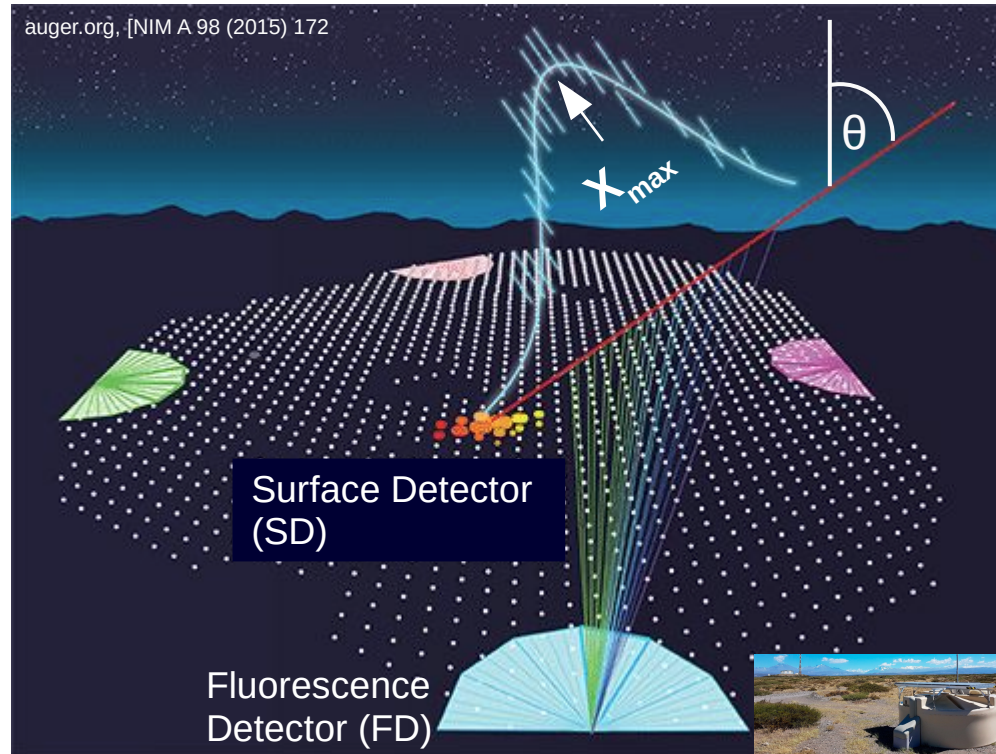
- estimation of **primary masses** from  $X_{\text{max}}$  fits
- interpretation of  $X_{\text{max}}$  moments using  $\ln A$
- **p-air cross-section** from tail of  $X_{\text{max}}$  distribution
- **average shape** of longitudinal profiles
- frequency of **anomalous showers**



# The Pierre Auger Observatory - *the best instrument to study hadronic interactions above $\sqrt{s} \approx 50$ TeV*

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  - [Phys. Rev. D 90 (2014) 012012]
- muon energy spectrum
  - from attenuation with  $\theta$  and  $r$
- **rise time** of signal vs.  $r$ 
  - [Phys. Rev. D 96 (2017) 122003]

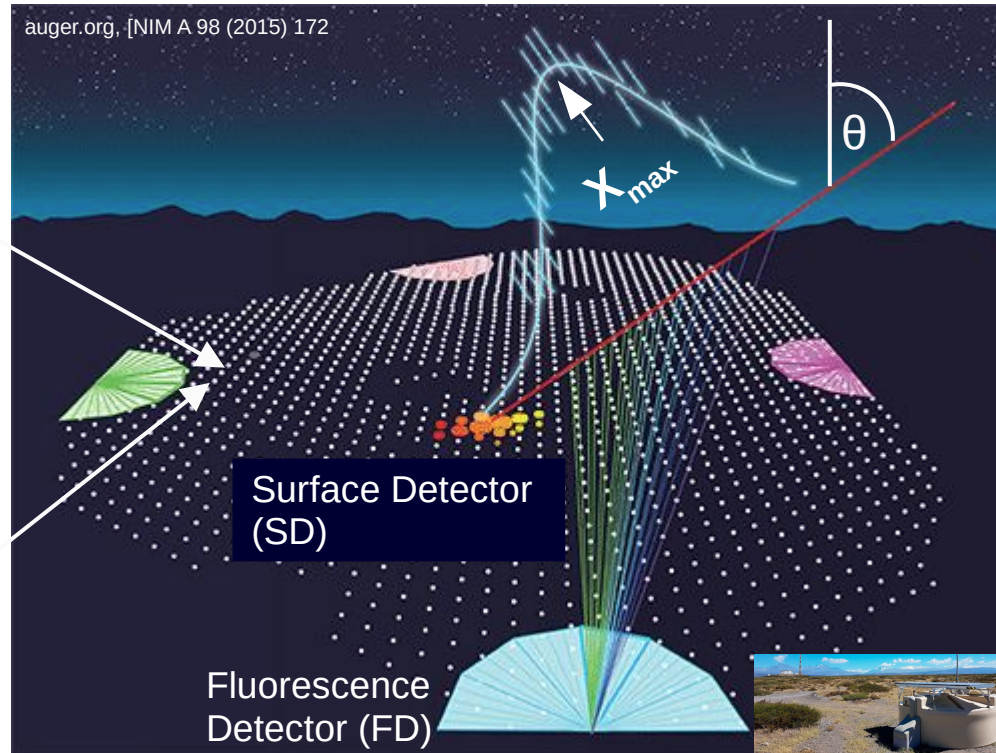
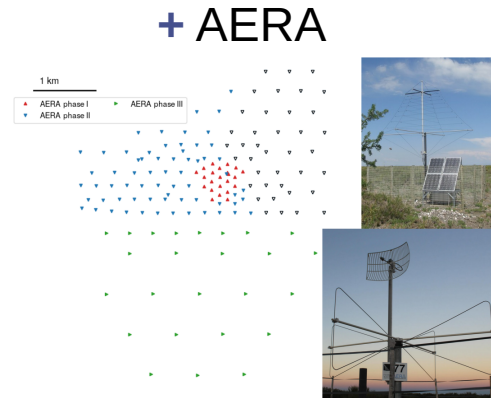
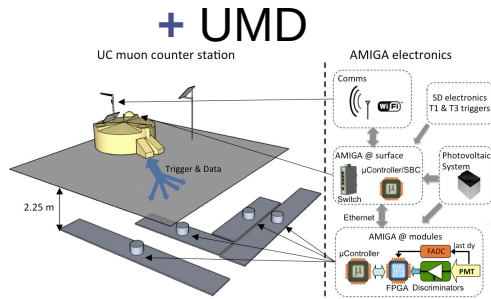


*not covered here,  
see references and backup slides*

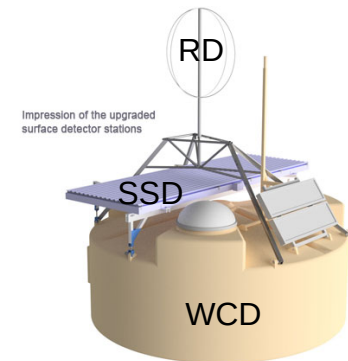
## FD longitudinal profile

- estimation of primary masses from  $X_{\text{max}}$  fits
- interpretation of  $X_{\text{max}}$  moments using  $\ln A$
- $p$ -air cross-section from tail of  $X_{\text{max}}$  distribution
- **average shape** of longitudinal profiles
  - [JCAP 03 (2019) 018]
- frequency of **anomalous showers**
  - [EPJ Web of Conferences 144 (2017) 01009]

# The Pierre Auger Observatory - *the best instrument to study hadronic interactions above $\sqrt{s} \approx 50$ TeV*



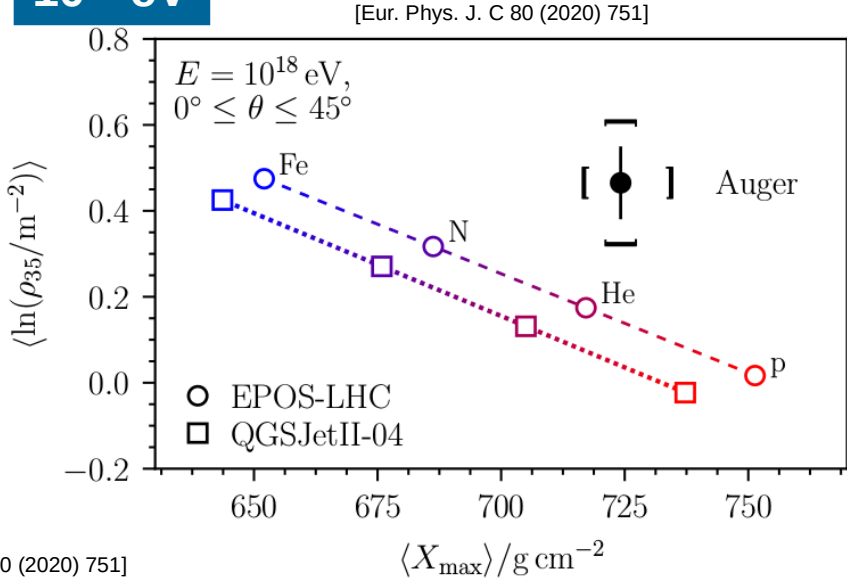
**+ AugerPrime**



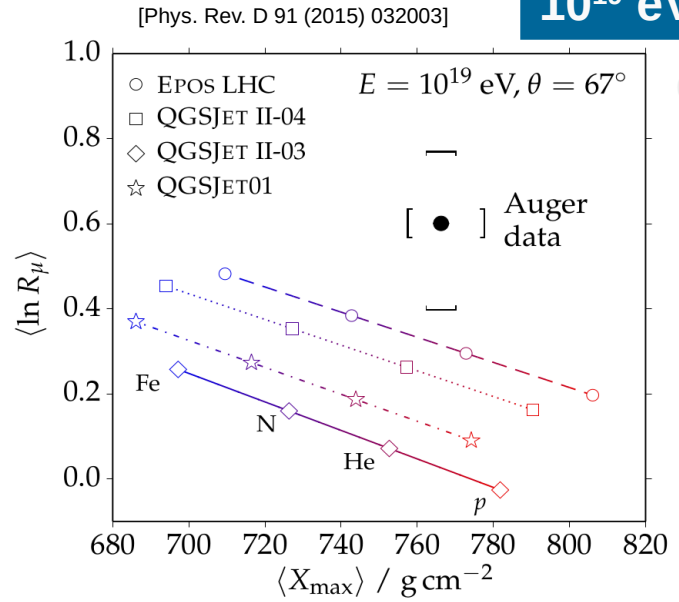
**Especially for combination of SD and FD observables !  
+ more to come in near future**

# Observables relevant to hadronic interaction models

**10<sup>18</sup> eV**



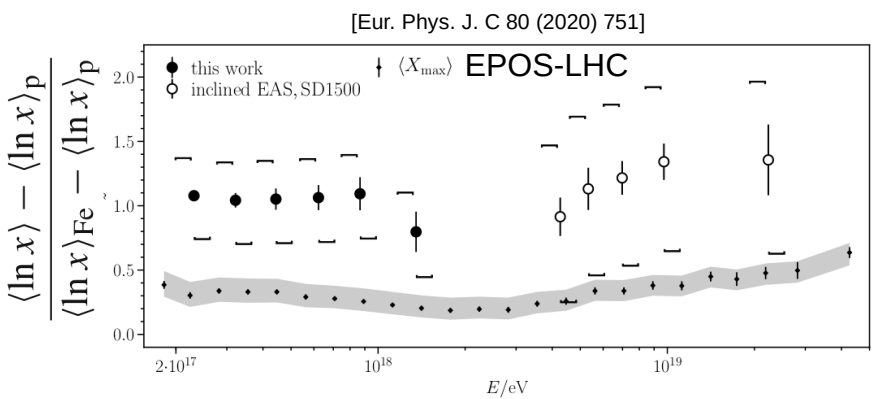
**10<sup>19</sup> eV**



## SD signal

- muon content
  - from buried scintillators,  $\theta < 45^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$

• muon production depth  
→ for core distance  $r > 1500\text{m}, \theta > 65^\circ$



• **~1.5-3 $\sigma$**  problem to describe the size of the muon content:  
**factor ~1.3-1.6 !**

• problem seen at various energies and zenith angles

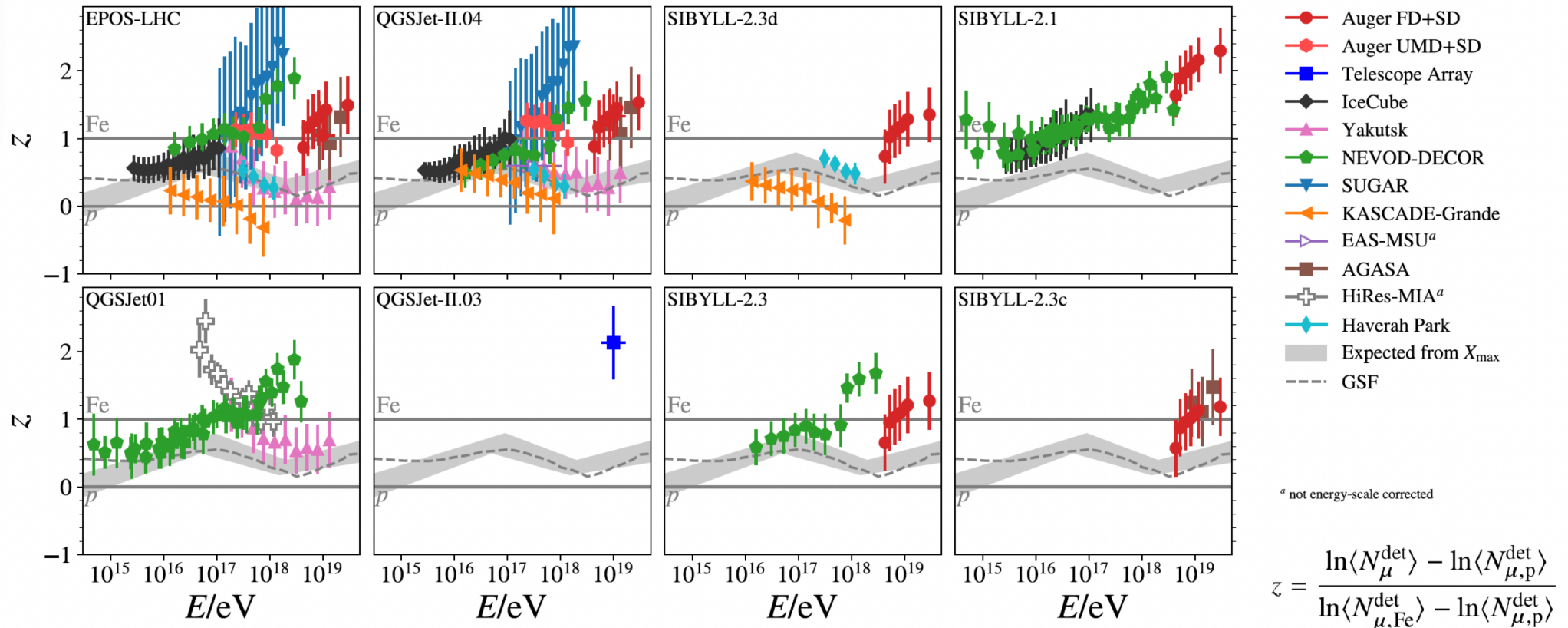
• range shape of longitudinal profiles  
• frequency of anomalous showers

# WHISP - energy evolution of the muon problem

[PoS(ICRC2023)466, L.Cazon Jan 2024 - Workshop on the Tuning of hadronic interactions]

► The z-scale after applying the energy shifts for common energy calibration.

Preliminary



## SD signal

- muon content
  - from buried scintillators,  $\theta < 45^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$
- muon production depth
  - for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$
- **muon energy spectrum**
  - from attenuation with  $\theta$  and  $r$
- rise time of signal vs.  $r$

- very hard in general with SD only
  - large systematics from energy scale
  - multi-detector approach necessary:
    - **SD+FD at different zenith angles**
    - WCD+RPC+SSD+UMD+RD
- @ AugerPrime**

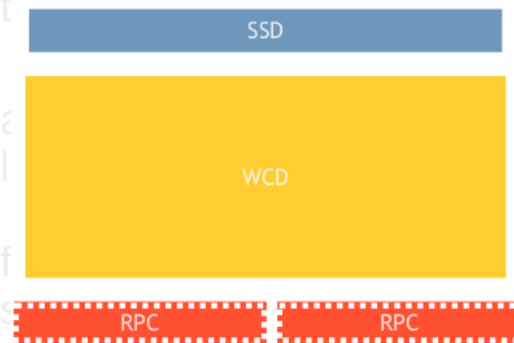
+ Underground Muon Detector

FD longitudinal profile

estimation of primary masses from  $X_{\text{max}}$  fits

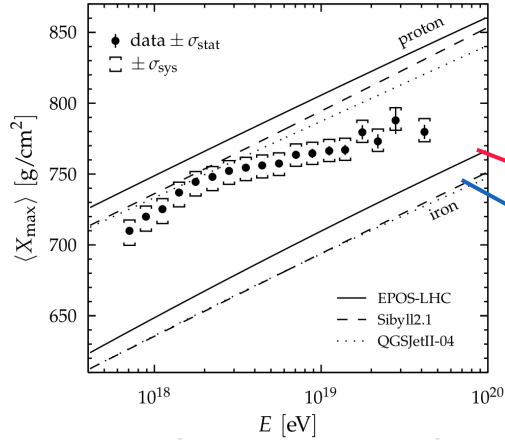
interpretation of  $X_{\text{max}}$  moments using  $\ln A$

+ Radio Detector

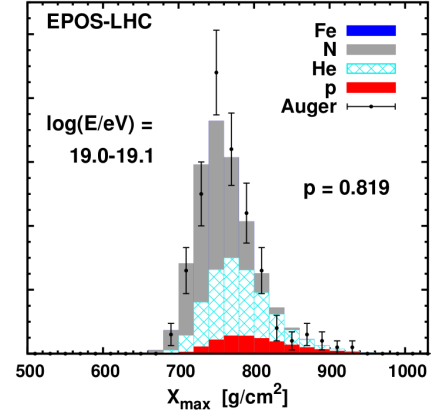


# Observables relevant to hadronic interaction models

[Phys. Rev. D 90 (2014) 122005]

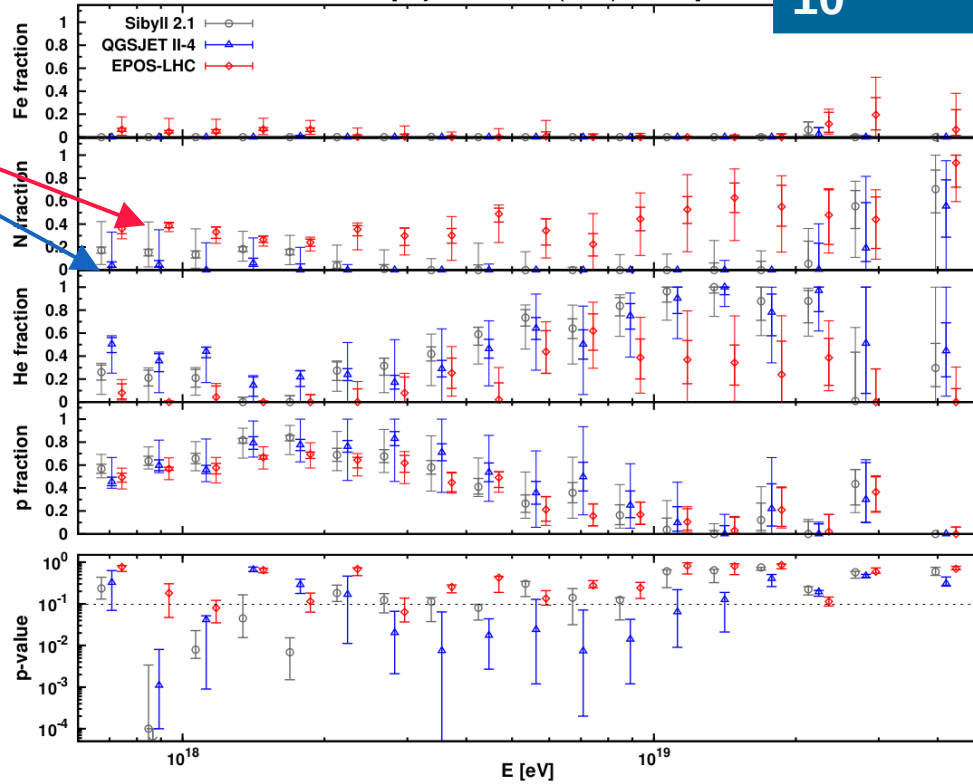


→ for core distance



[Phys. Rev. D 90 (2014) 122006]

**10<sup>17.8-19.6</sup> eV**



## FD longitudinal profile

- estimation of primary masses from  $X_{\max}$  fits

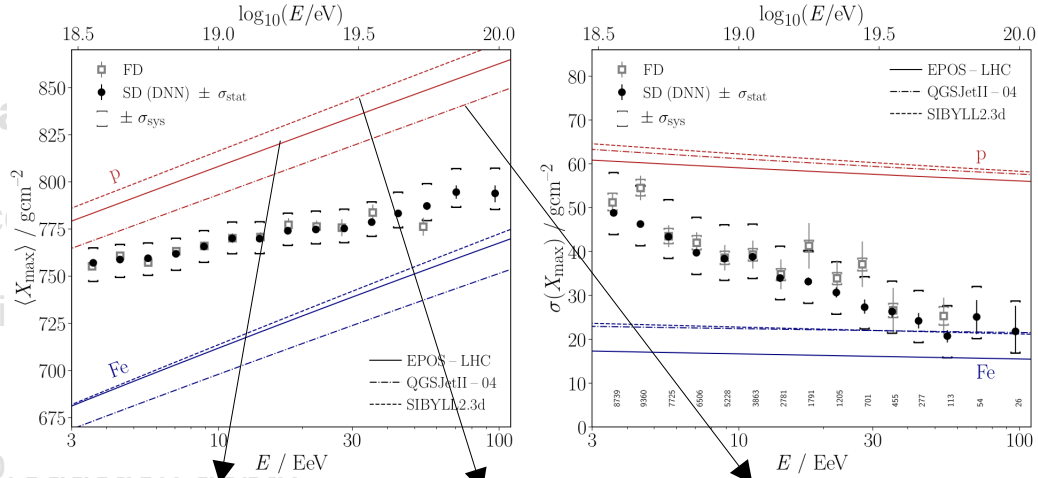
dependent on MC  $X_{\max}$  scale  
 - input into many hadronic interaction studies

- average shape of longitudinal profiles
- frequency of anomalous showers

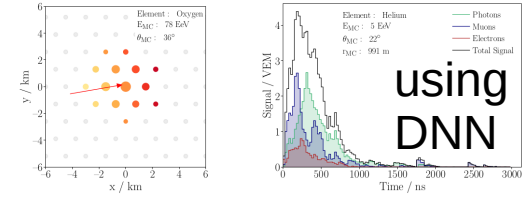
# Observables relevant to hadronic interaction models

[accepted in PRD, arXiv:2406.06319]

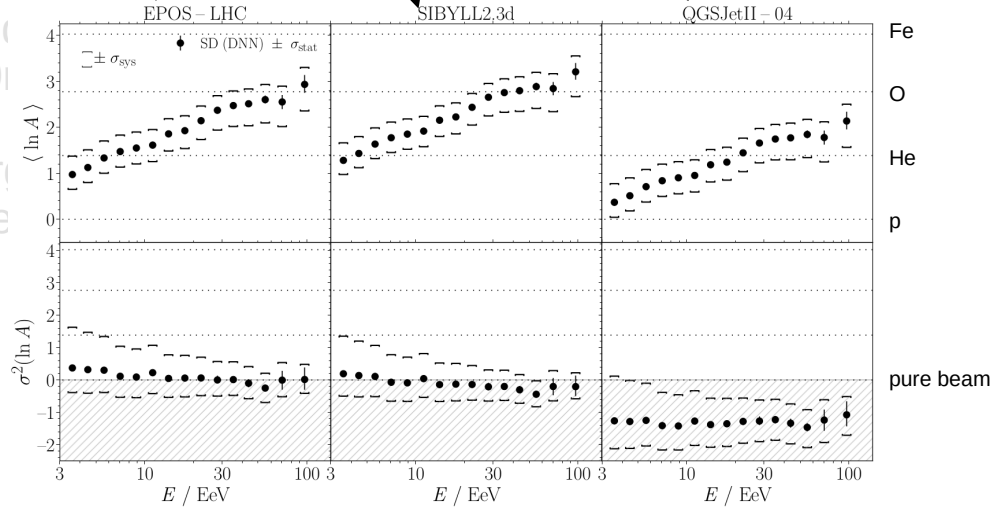
**10<sup>18.5-20.0</sup> eV**



## FD longitudinal profile



- interpretation of  $X_{\max}$  moments using  $\ln A$



$$\langle \ln A \rangle = \frac{\langle X_{\max} \rangle - \langle X_{\max} \rangle_p}{f_E}$$

$$\sigma_{\ln A}^2 = \frac{\sigma^2(X_{\max}) - \sigma_{\text{sh}}^2(\langle \ln A \rangle)}{b \sigma_p^2 + f_E^2}$$

[JCAP 02 (2013) 026]

**Strong dependence on the MC  $X_{\max}$  scale**

- SD signal
- muon count
- from scintillator
- from muon detector
- muon profile
- for core position
- $r > 1500$  m
- muon energy
- from atmospheric muon flux
- $\theta$  and  $r$

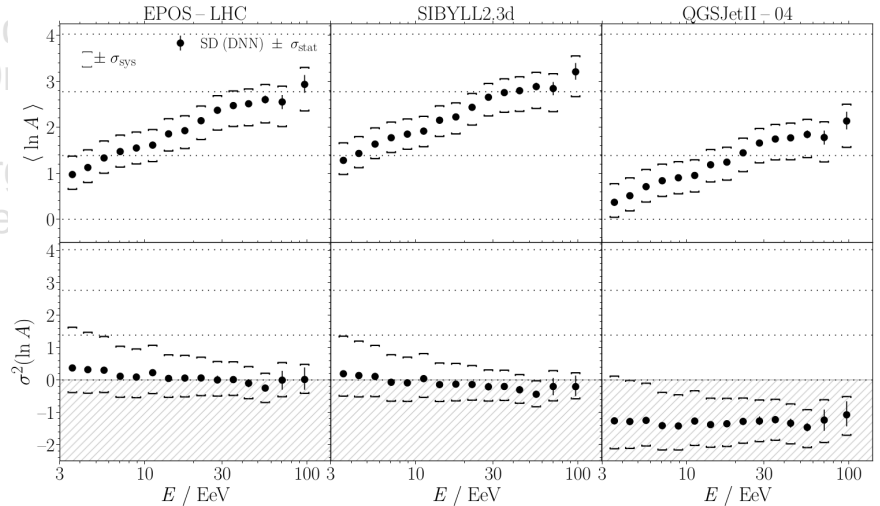
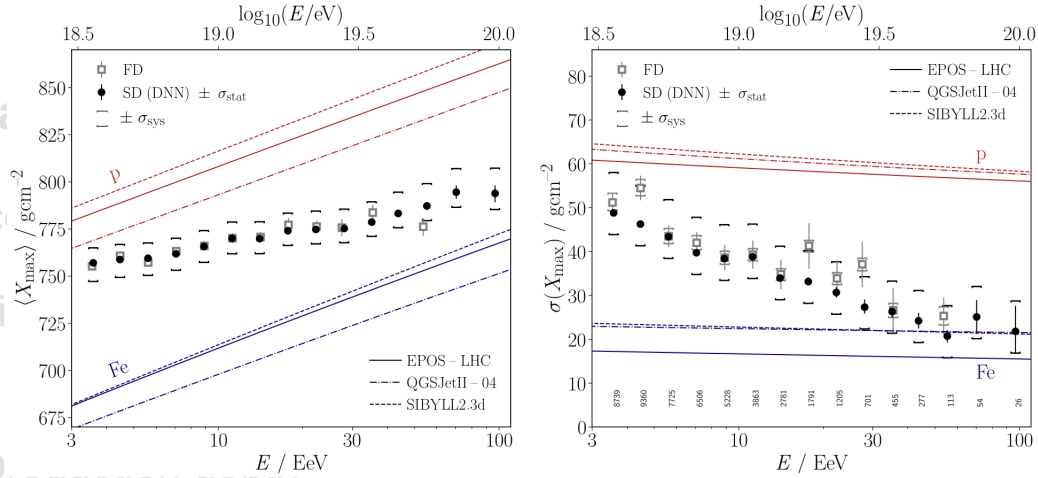
# Observables relevant to hadronic interaction models

[accepted in PRD, arXiv:2406.06319]

**10<sup>18.5-20.0</sup> eV**

## FD longitudinal profile

- estimation of primary masses from  $X_{\max}$  fits
- interpretation of  $X_{\max}$  moments using  $\ln A$
- p-air cross-section from tail of  $X_{\max}$  distribution



**Indication of too shallow predictions of  $\langle X_{\max} \rangle$  for all three models !**

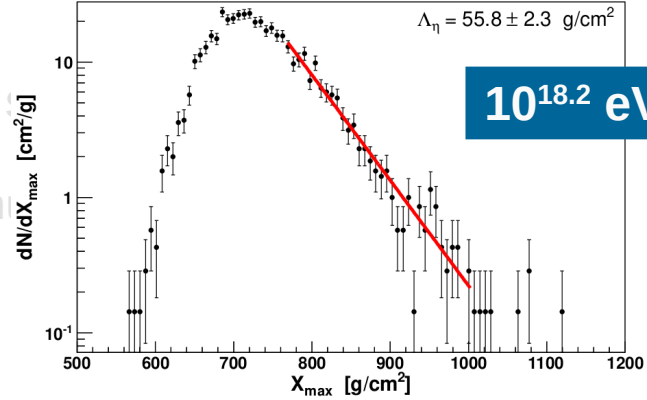
showers

- SD signal
- muon count
- from sci...
- from ...
- muon p...
- for core (r > 1500)
- muon energy
- from atte
- $\theta$  and r



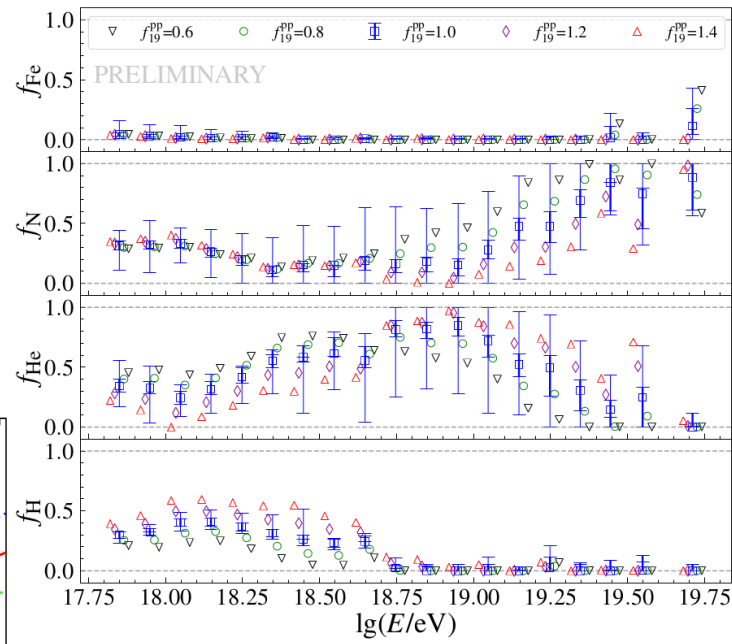
# Observables relevant to hadronic interaction models

[Phys. Rev. Lett. 109 (2012) 062002]

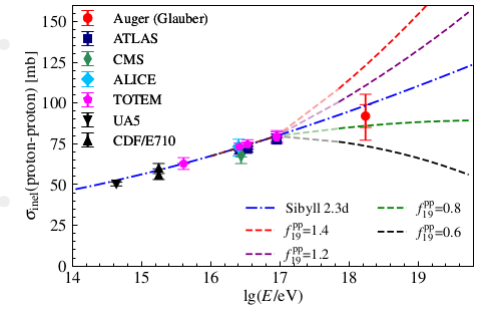


**10<sup>17.7-19.8</sup> eV ?**

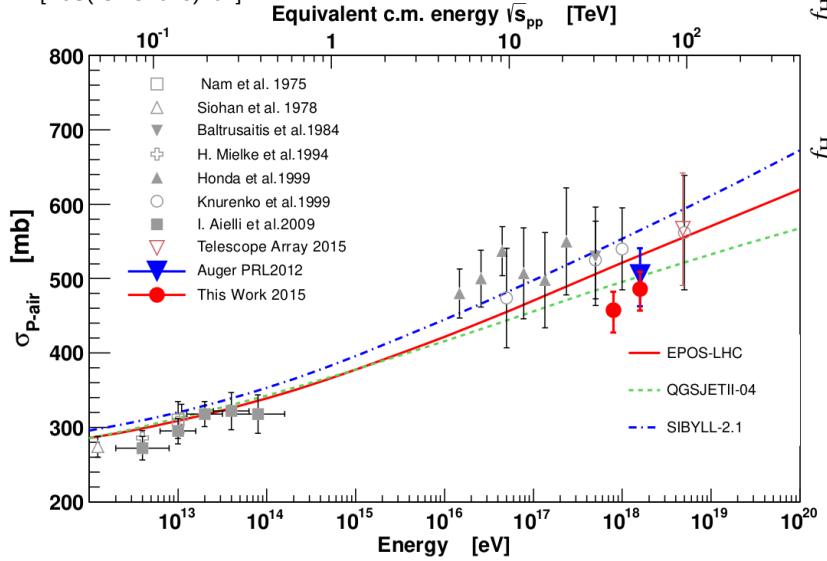
[O. Tkachenko for Pierre Auger Coll. PoS(ICRC2023)438]



## FD longitudinal profile



[PoS(ICRC2015)401]

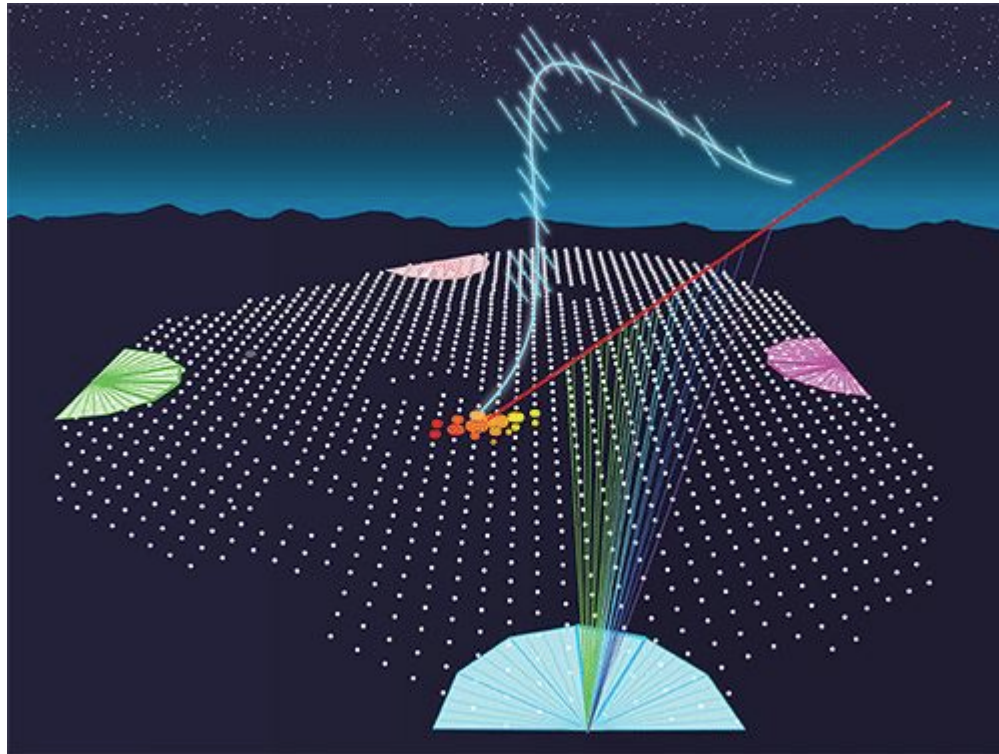


- **p-air cross-section** from tail of  $X_{max}$  distribution

• average shape of longitudinal profiles

- p-air cross-section consistent with current models
- **new approach**: composition+cross-section fit (decrease of systematics from He and  $X_{max}$  scale)

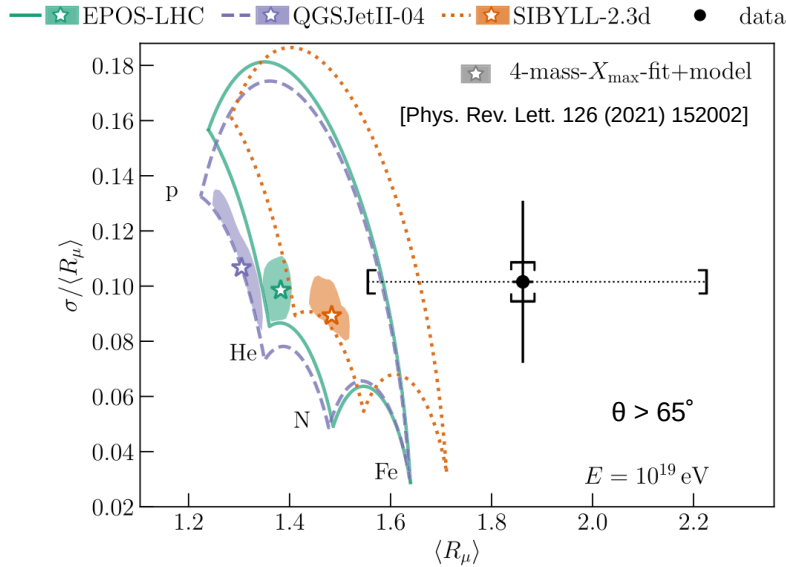
# Combining SD and FD observables



## Ground signal + Longitudinal profile

- inclined showers + FD  $\rightarrow \sigma(N_\mu)$
- correlation between  $X_{\max}$  and  $S(1000)$
- top-down approach  $\rightarrow R_{\text{had}}$
- applying shower-universality approach  $\rightarrow R_{\text{had}}$
- 2-dim distributions  $[S(1000), X_{\max}] \rightarrow R_{\text{had}}(\theta), \Delta X_{\max}$

# Combining SD and FD observables

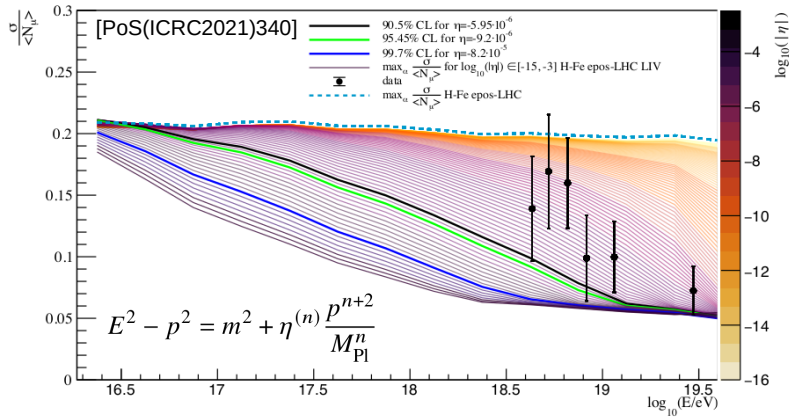


## Ground signal + Longitudinal profile

- inclined showers + FD  $\rightarrow \sigma(N_\mu)$  ~10<sup>18.6-19.5</sup> eV

- correlation between  $X_{\max}$  and  $S(1000)$
- top-down approach  $\rightarrow R_{\text{had}}$

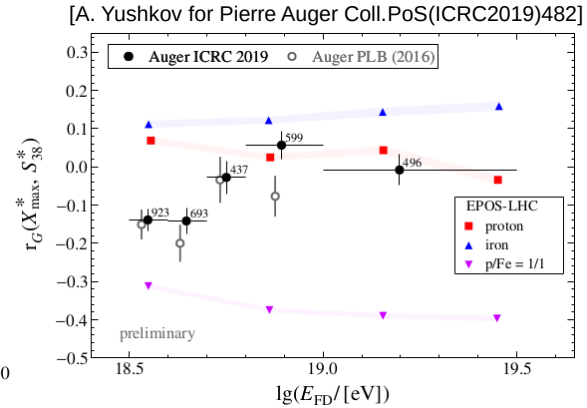
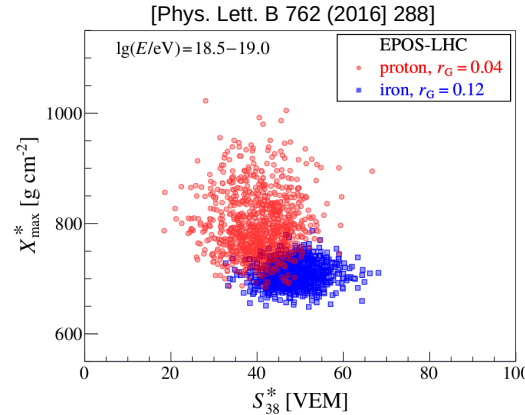
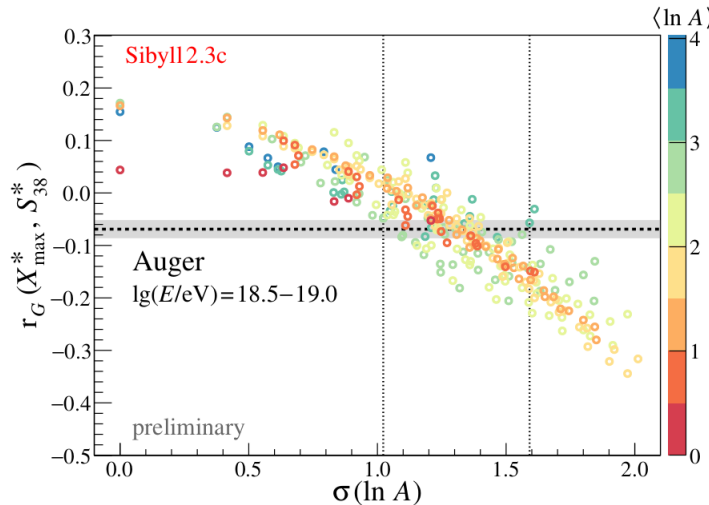
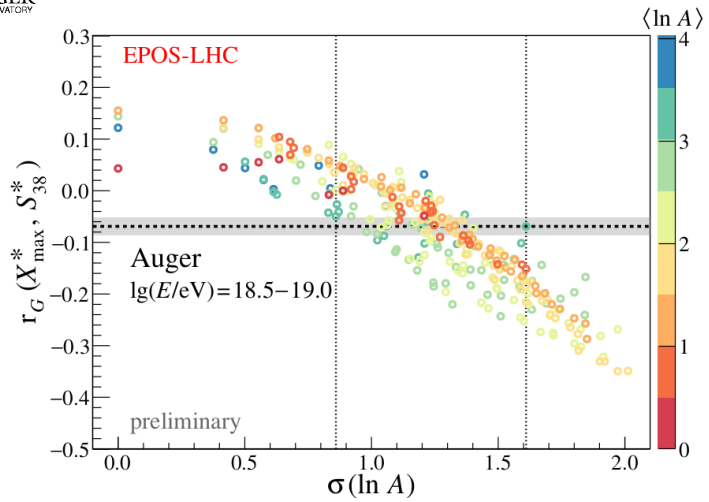
- confirmation of a problem to describe the size of the muon content: **factor ~1.3-1.6**
- muon fluctuations are consistent with data (no obvious problem in the first interaction)  $\rightarrow$  strong constraints on the Lorentz invariance violation (journal publication in preparation)



$$E^2 - p^2 = m^2 + \eta^{(n)} \frac{p^{n+2}}{M_{\text{Pl}}^n}$$

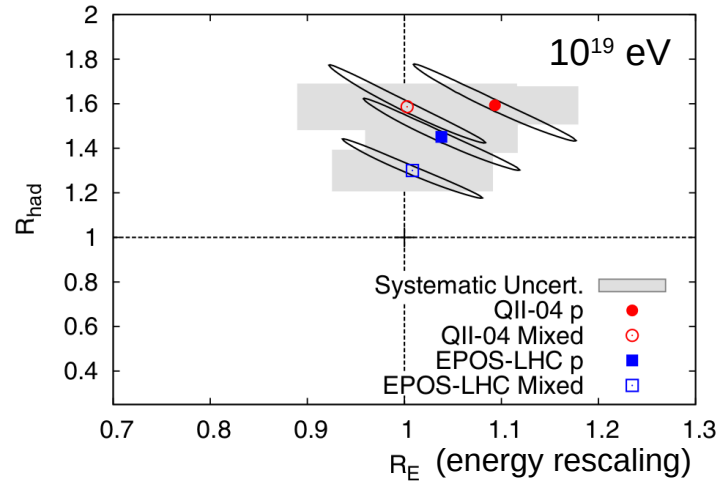
## Ground signal + Longitudinal profile

- inclined showers + FD  $\rightarrow \sigma(N_{\nu})$
- correlation between  $X_{\max}$  and  $S(1000)$

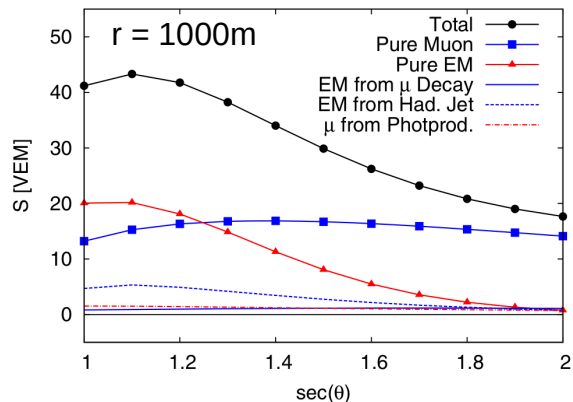


- $\sim$ model-independent estimator of spread of beam masses
- $>5\sigma$  tension with light masses from  $X_{\max}$  fits for QGSJet II-04 (too shallow  $X_{\max}$  scale)

# Combining SD and FD observables



$$S_{\text{resc}}(R_E, R_{\text{had}})_{i,j} \equiv R_E S_{\text{EM},i,j} + R_{\text{had}} R_E^\alpha S_{\text{had},i,j}$$



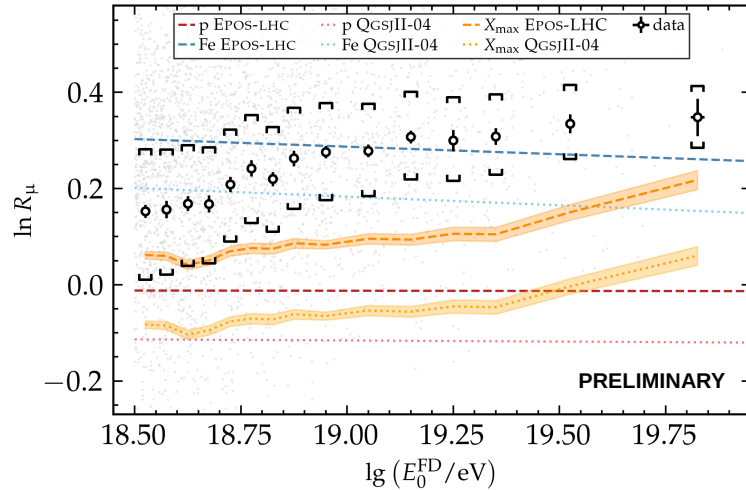
## Ground signal + Longitudinal profile

- inclined showers + FD  $\rightarrow \sigma(N_\mu)$
- correlation between  $X_{\text{max}}$  and  $S(1000)$
- top-down approach  $\rightarrow R_{\text{had}} \sim \mathbf{1.3 - 1.6 !}$
- [Phys. Rev. Lett. 117 (2016) 192001]
- applying shower-universality approach  $\rightarrow R_{\text{had}}$
- 2-dim distributions  $[S(1000), X_{\text{max}}] \rightarrow R_{\text{had}}(\theta), \Delta X_{\text{max}}$

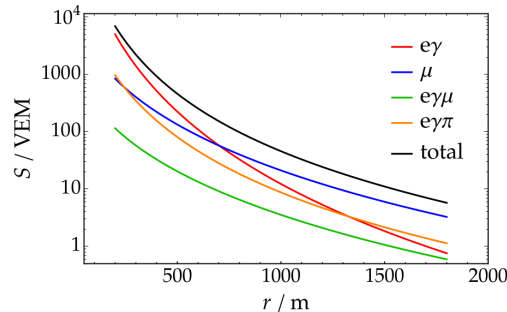
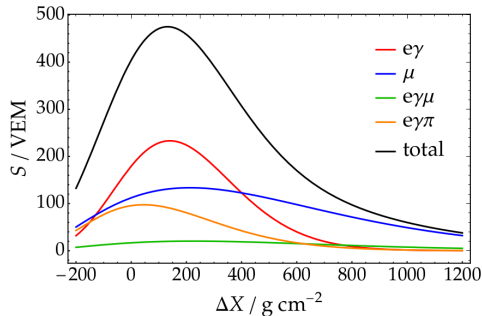
- mass from measured  $X_{\text{max}}$  - depends on MC  $X_{\text{max}}$  scale
- $\sim 2\text{-}3\sigma$  tension with strong dependence on energy scale

# Combining SD and FD observables

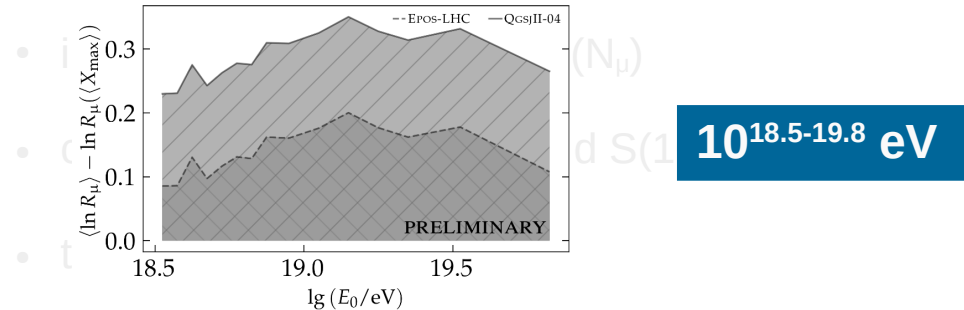
shower geometry, energy and  $X_{\max}$  from FD



$$S_{\text{tot}} \approx S_{e\gamma} + R_{\mu} (S_{\mu} + S_{e\gamma(\mu)} + S_{e\gamma(\pi)})$$



## Ground signal + Longitudinal profile



- applying shower-universality approach  
 $\rightarrow R_{\text{had}} \sim \mathbf{1.1 - 1.3}$  [PoS(ICRC2023)339, arXiv:2405.03494]

- 2-dim distributions  $[S(1000), X_{\max}] \rightarrow R_{\text{had}}(\theta), \Delta X_{\max}$

- $\sim 2\sigma$  tension
- $R_{\text{had}}$  smaller than in top-down approach
- $\sim$ insensitive to the MC  $X_{\max}$  scale
- journal publication in preparation



PIERRE AUGER OBSERVATORY

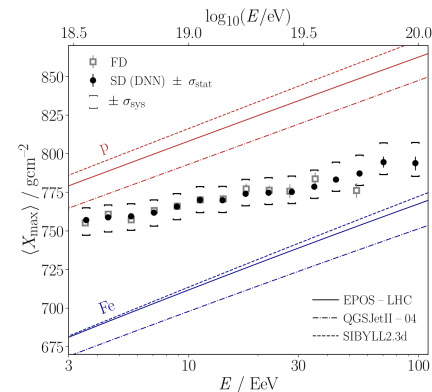
# Mass composition & tests of hadronic interactions

[accepted in PRD, arXiv:2406.06319]

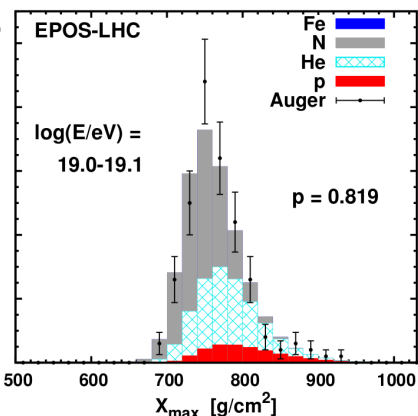
[Phys. Rev. D 90 (2014) 122006]

[Phys. Rev. Lett. 117 (2016) 192001]

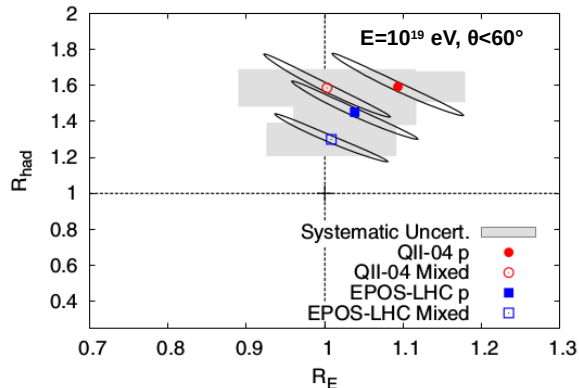
[Phys. Lett. B 762 (2016) 288]



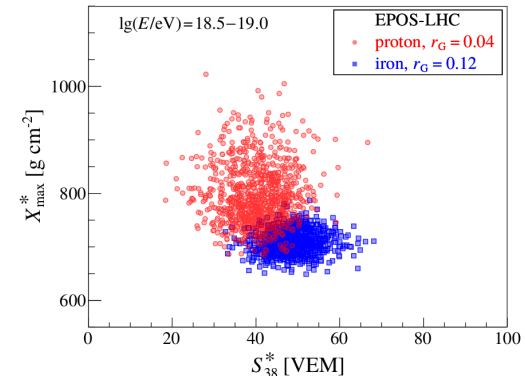
MC  $X_{\max}$  scale ?



Primary fraction fit



Deficit in MC hadronic signal



~ model-independent estimation of beam mixing from  $[X_{\max}, S(1000)]$  correlation

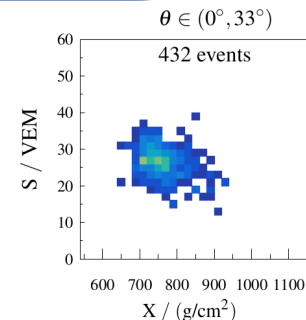
MC:

$$S_{\text{had}}(\theta) \rightarrow S_{\text{had}}(\theta) \cdot R_{\text{had}}(\theta)$$

$$X_{\max} \rightarrow X_{\max} + \Delta X_{\max}$$

[Phys. Rev. D 109 (2024) 102001]

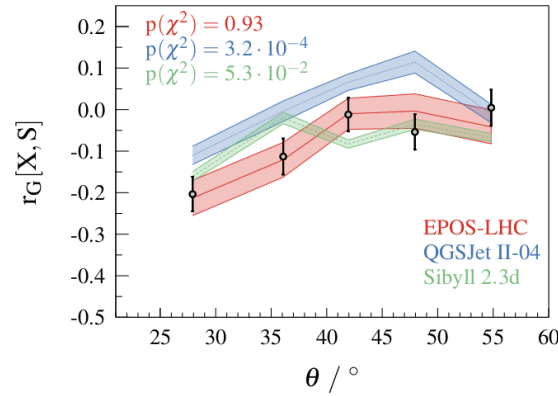
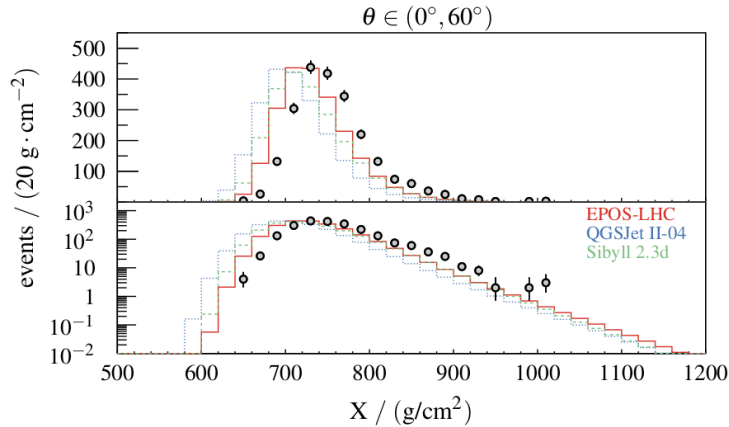
Mass composition fit of observed  $[X_{\max}, S(1000)](\theta)$  distributions with free modification of MC predictions **not only of hadronic signal but also of  $X_{\max}$**



# Improvement in data description

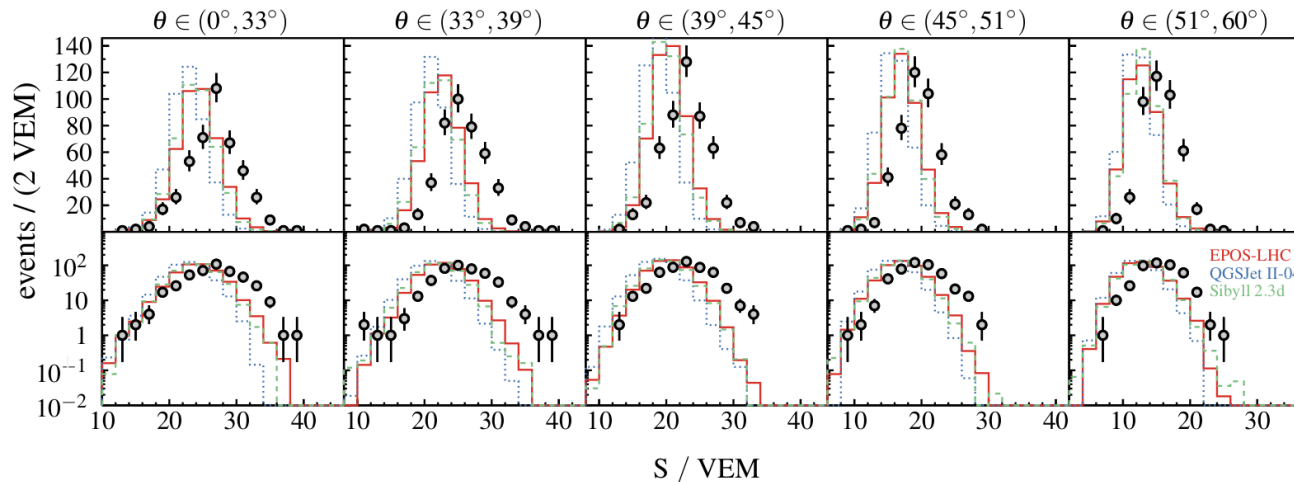
$10^{18.5-19.0}$  eV

[Phys. Rev. D 109 (2024) 102001]



$$\ln \mathcal{L} = \begin{cases} \sum_k \sum_j (C_{jk} - n_{jk} + n_{jk} \ln \frac{n_{jk}}{C_{jk}}), & n_{jk} > 0 \\ \sum_k \sum_j C_{jk}, & n_{jk} = 0 \end{cases}$$

$\ln \mathcal{L}_{\min}$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
none	2022.9	4508.0	2496.5
$\Delta X_{\max}$	738.6	1674.8	1015.7
$R_{\text{had}} = \text{const.}$	489.2	684.4	521.6
$R_{\text{had}}(\theta)$	489.2	673.9	517.6
$R_{\text{had}} = \text{const. and } \Delta X_{\max}$	452.2	486.7	454.2
$R_{\text{had}}(\theta) \text{ and } \Delta X_{\max}$	451.9	476.3	451.6

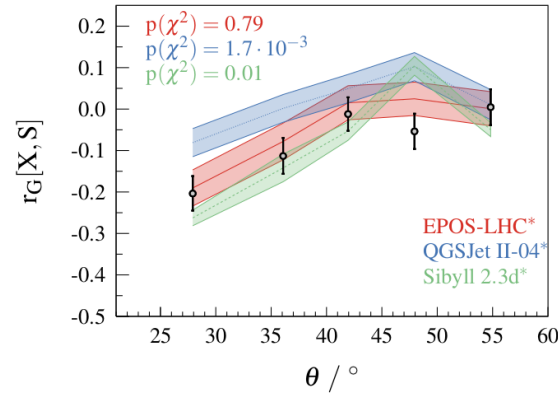
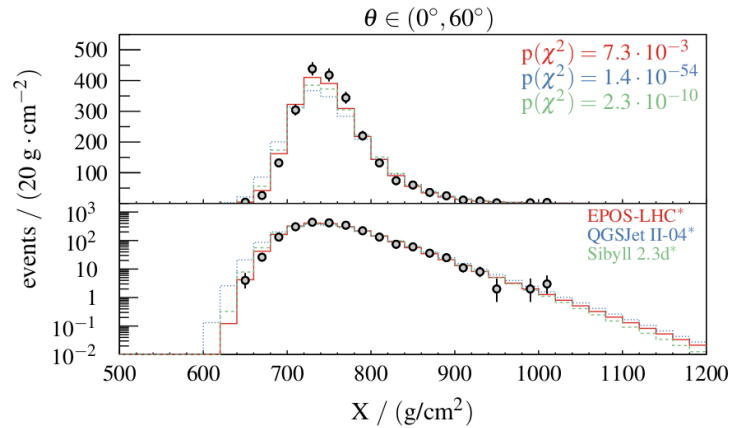




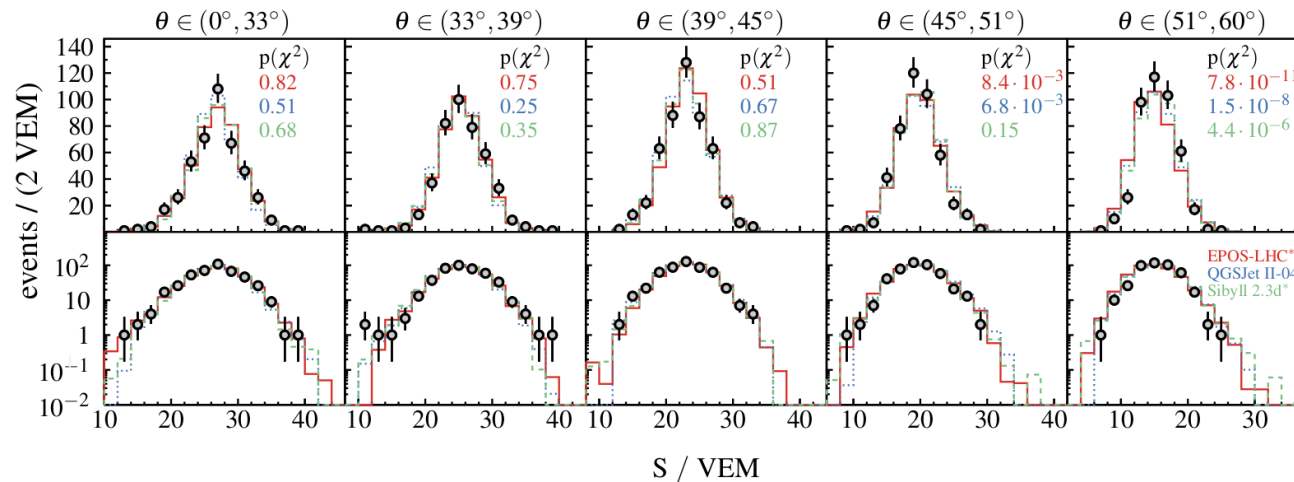
# Improvement in data description

$10^{18.5-19.0}$  eV

[Phys. Rev. D 109 (2024) 102001]



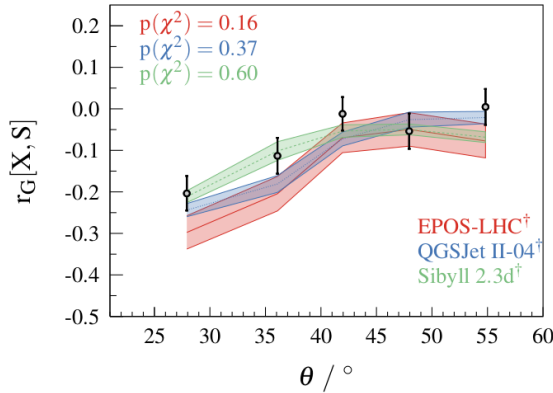
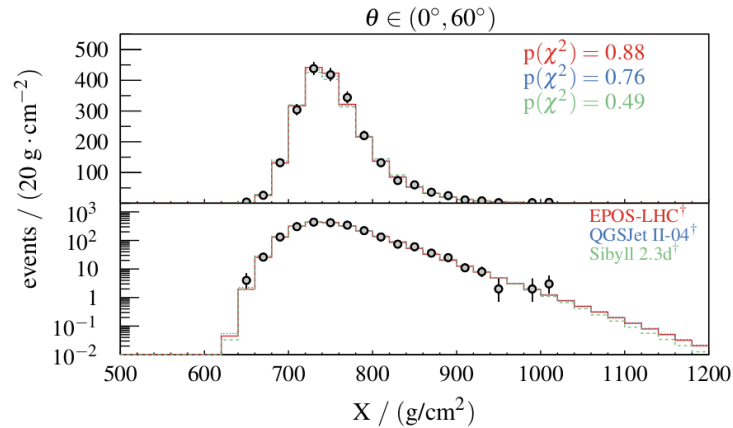
$\ln \mathcal{L}_{\min}$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
none	2022.9	4508.0	2496.5
$\Delta X_{\max}$	738.6	1674.8	1015.7
$R_{\text{had}} = \text{const.}$	489.2	684.4	521.6
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$R_{\text{had}}(\theta)$ and $\Delta X_{\max}$	451.9	476.3	451.6



# Improvement in data description

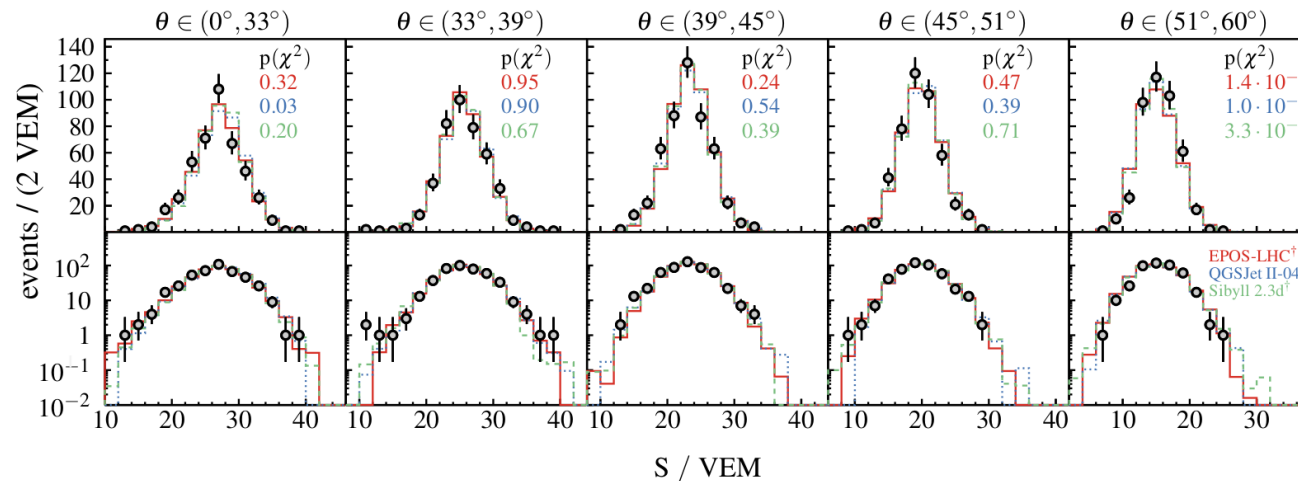
$10^{18.5-19.0}$  eV

[Phys. Rev. D 109 (2024) 102001]



*p-values of fits from MC-MC tests > 10% for all three models*

$\ln \mathcal{L}_{\min}$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
none	2022.9	4508.0	2496.5
$\Delta X_{\max}$	738.6	1674.8	1015.7
$R_{\text{had}} = \text{const.}$	489.2	684.4	521.6
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$R_{\text{had}}(\theta)$ and $\Delta X_{\max}$	451.9	476.3	451.6



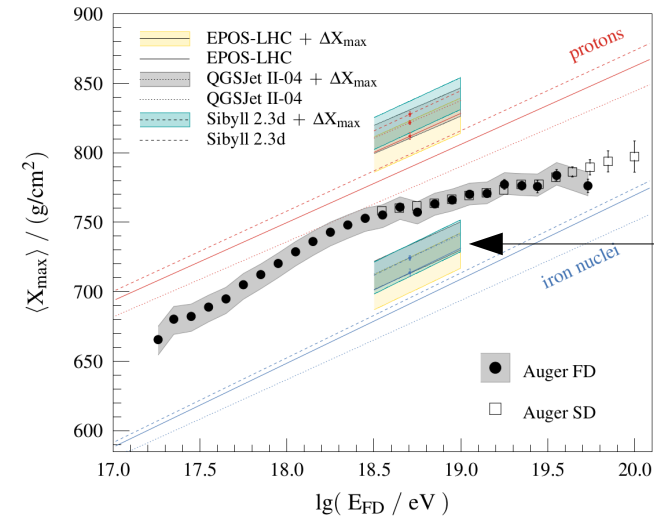
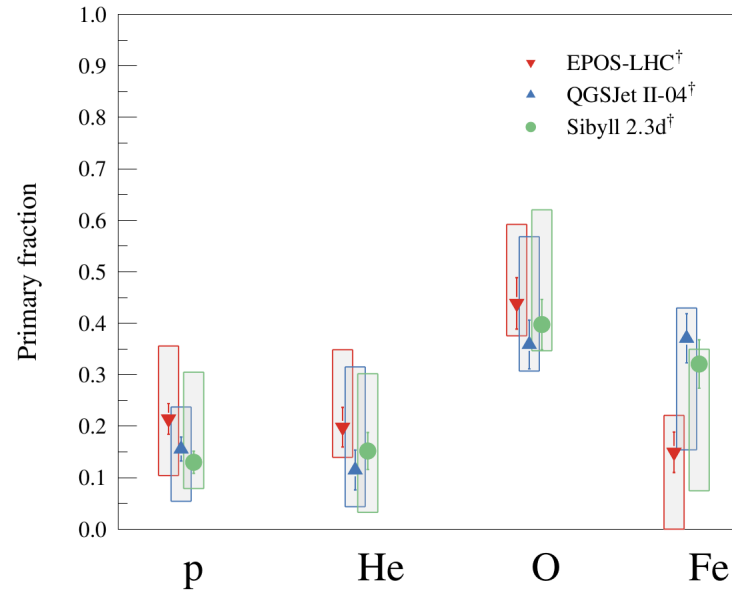
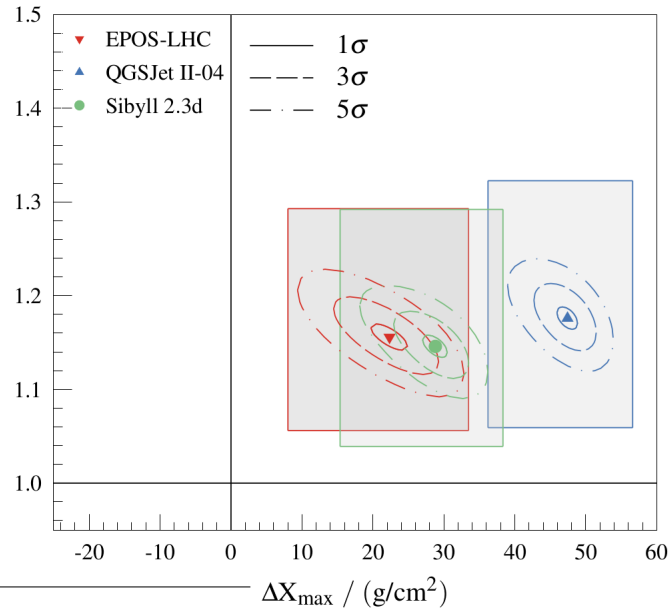
Significant improvement  $>5\sigma$  using  $R_{\text{had}}$  and  $\Delta X_{\max}$  (Likelihood ratio tests for nested model using Wilks' theorem)

# Fitted parameters

[Phys. Rev. D 109 (2024) 102001]

Zenith dependence of  $R_{\text{had}}$  assumed to be

linear in  $X_{\text{ground}} - X_{\text{max}}$   
 $\rightarrow R_{\text{had}}(\theta_{\text{min}} \sim 28^\circ), R_{\text{had}}(\theta_{\text{max}} \sim 55^\circ)$

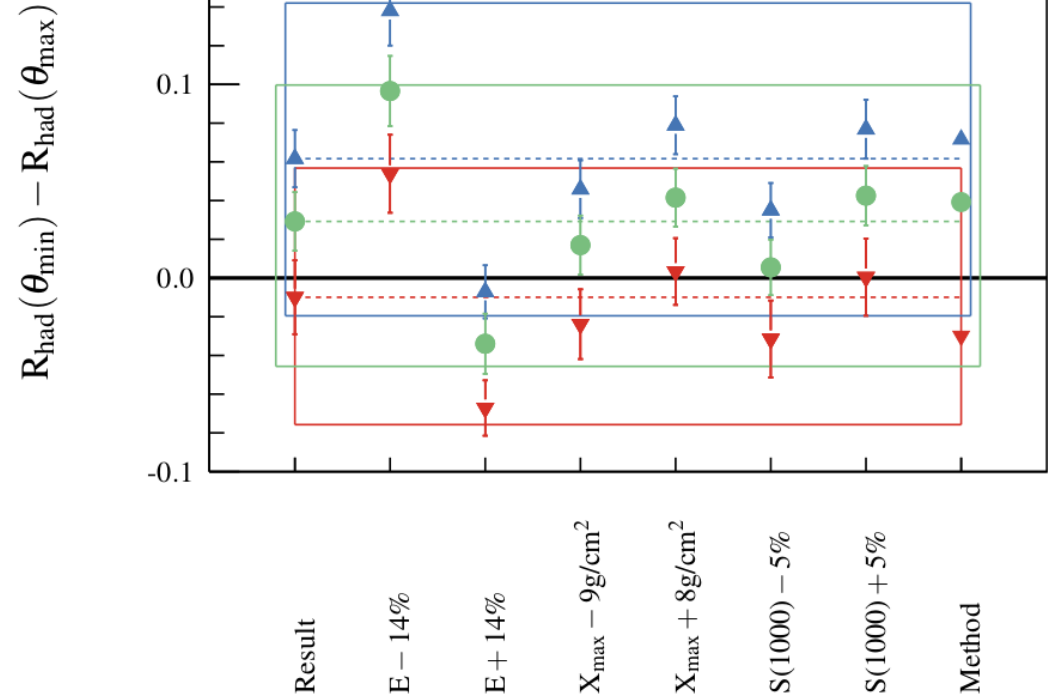
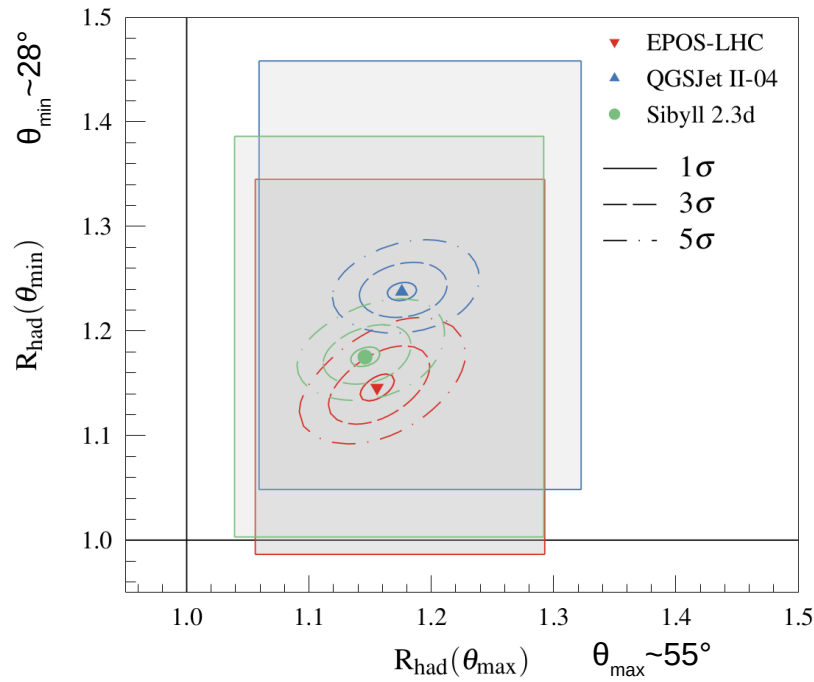


- deeper  $X_{\text{max}}$  predictions for all models !
- alleviated “muon problem“ to ~15-25%
- smaller model differences in mass composition

# Attenuation of hadronic signal with zenith angle

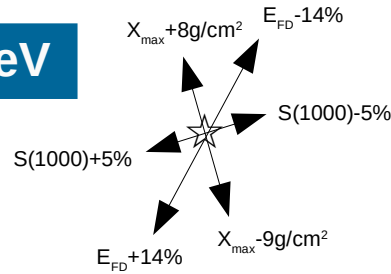
[Phys. Rev. D 109 (2024) 102001]

**10<sup>18.5-19.0</sup> eV**



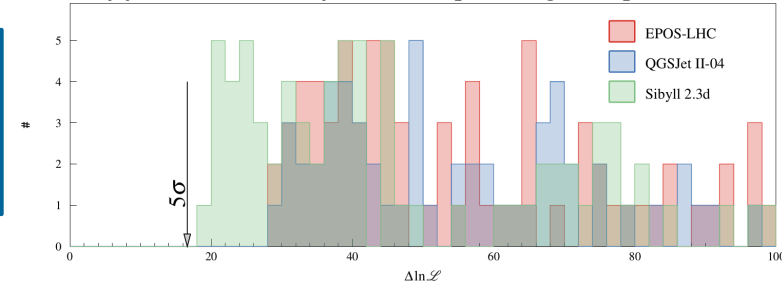
Indication of harder muon spectra in QGSJet II-04 than in data

$10^{18.5-19.0}$  eV

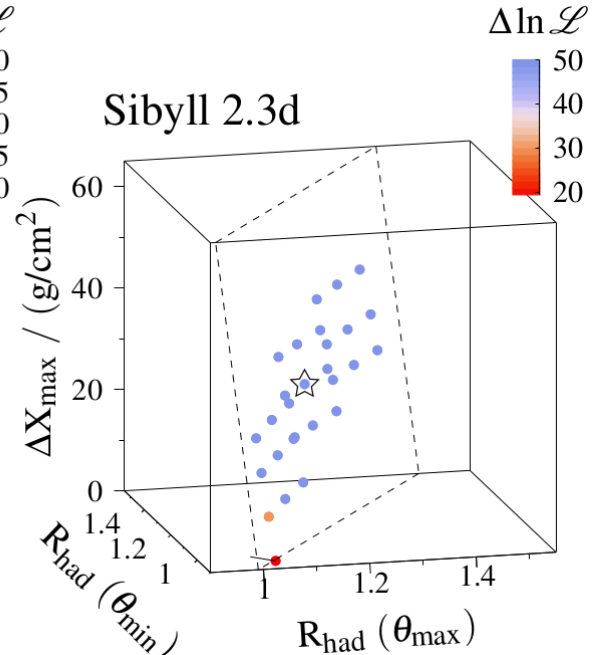
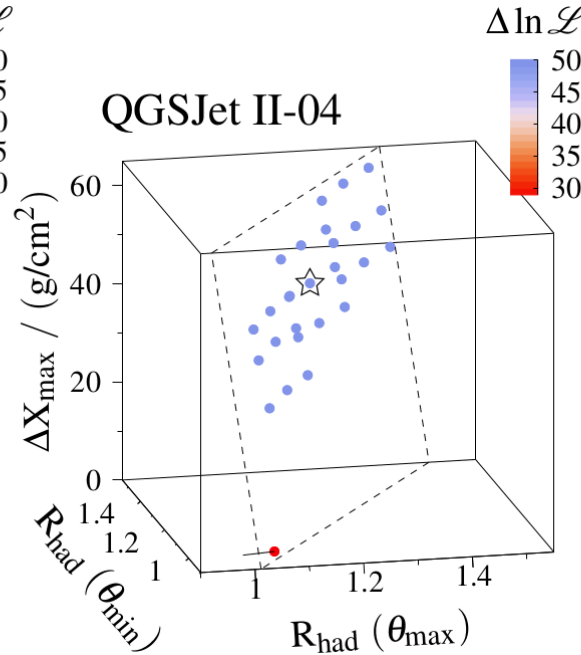
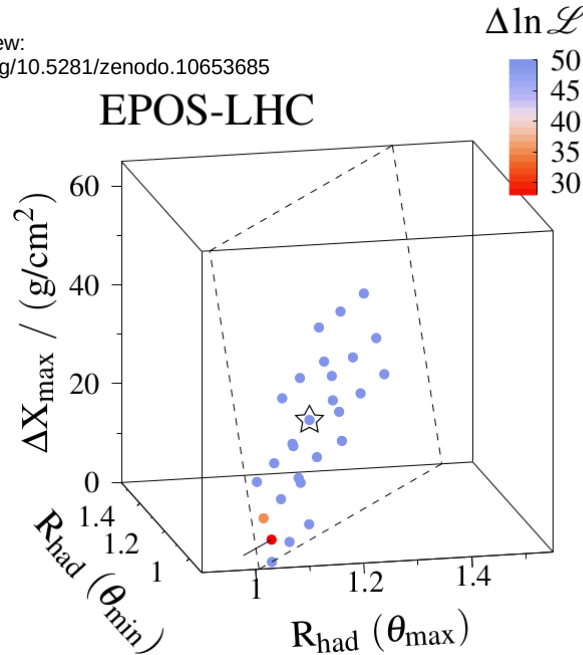


Significance of improvement  
of data description always  
above  $5\sigma$

Denser scan in the region of the closest  
approach of the plane to  $[1,1,0 \text{ g/cm}^2]$



Animated view:  
<https://doi.org/10.5281/zenodo.10653685>



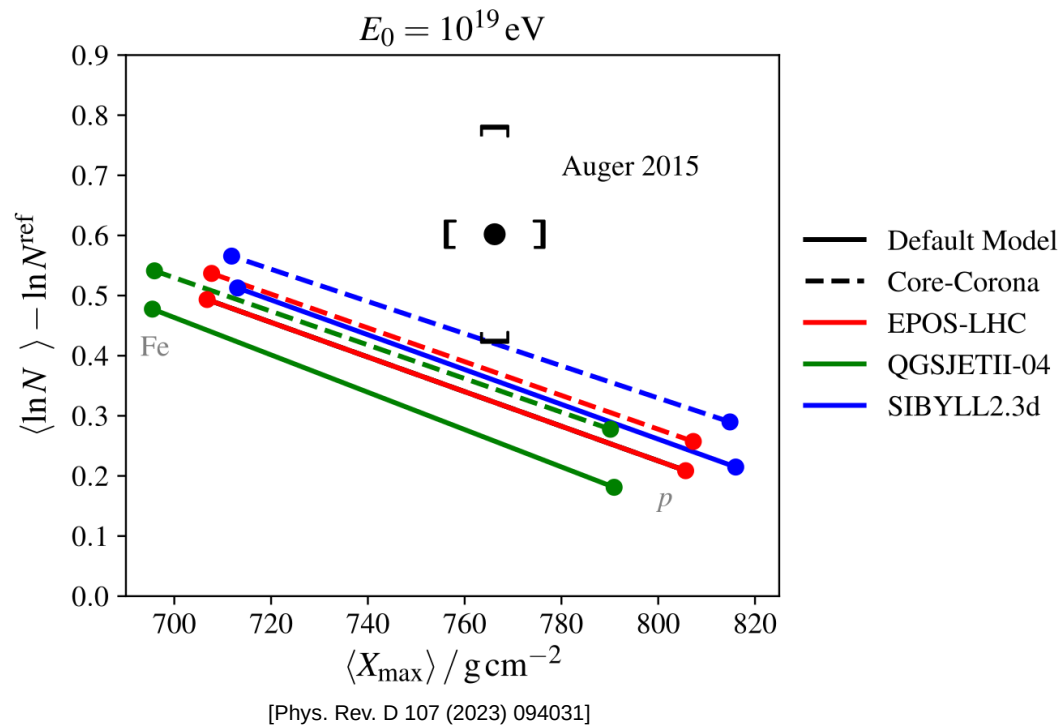
# Summary of tests of models using Auger data

test	energy / EeV	$\theta / ^\circ$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
$X_{\max}$ moments	$\sim 3$ to 50	0 to 80	no tension <span style="color: green;">■</span>	tension <span style="color: red;">■</span>	no tension (2.3c) <span style="color: green;">■</span>
$X_{\max}:S(1000)$ correlation	3 to 10	0 to 60	no tension <span style="color: green;">■</span>	tension <span style="color: red;">■</span>	no tension (2.3c) <span style="color: green;">■</span>
mean muon number	$\sim 10$	$\sim 67$	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>
mean muon number	0.2 to 2	0 to 45	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	—
fluctuation of muon number	4 to 40	$\sim 67$	no tension <span style="color: green;">■</span>	no tension <span style="color: green;">■</span>	no tension <span style="color: green;">■</span>
muon production depth	20 to 70	$\sim 60$	tension <span style="color: red;">■</span>	no tension <span style="color: green;">■</span>	—
$S(1000)$	$\sim 10$	0 to 60	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	—
$[X_{\max}, S(1000)]$ fits	3 to 10	0 to 60	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>

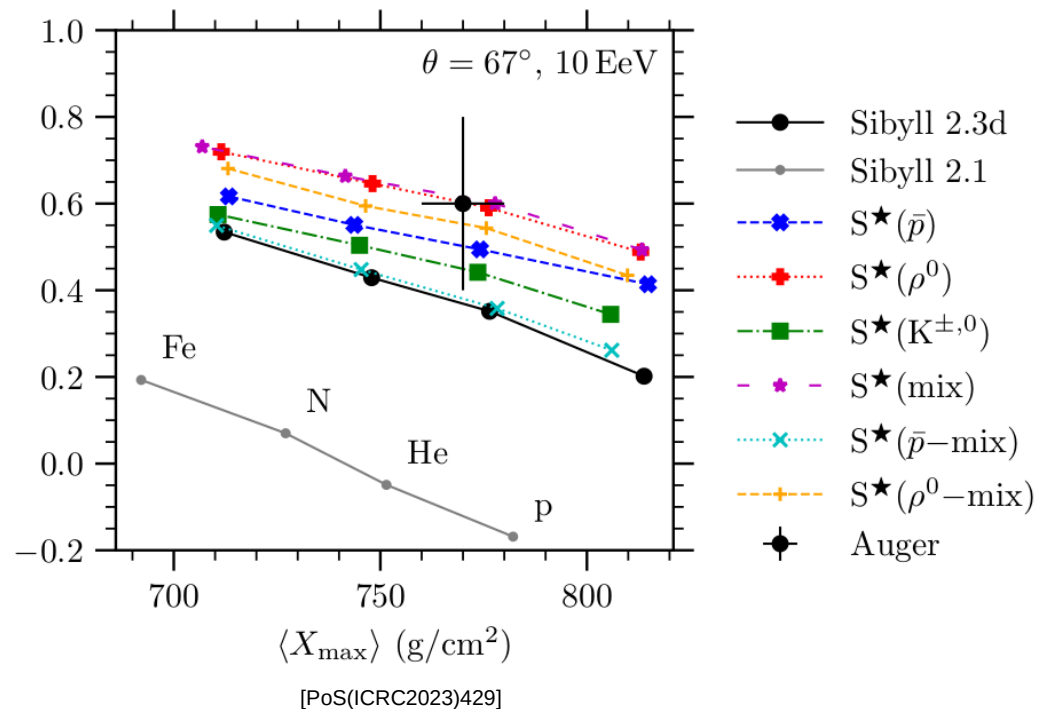
- all models have problems ...
- a need to describe consistently both  $X_{\max}$  and ground signal  
- issue in both observables !

# Adding muons ~ without changing $X_{\max}$

Core-corona model - collective statistical hadronization → EPOS 4

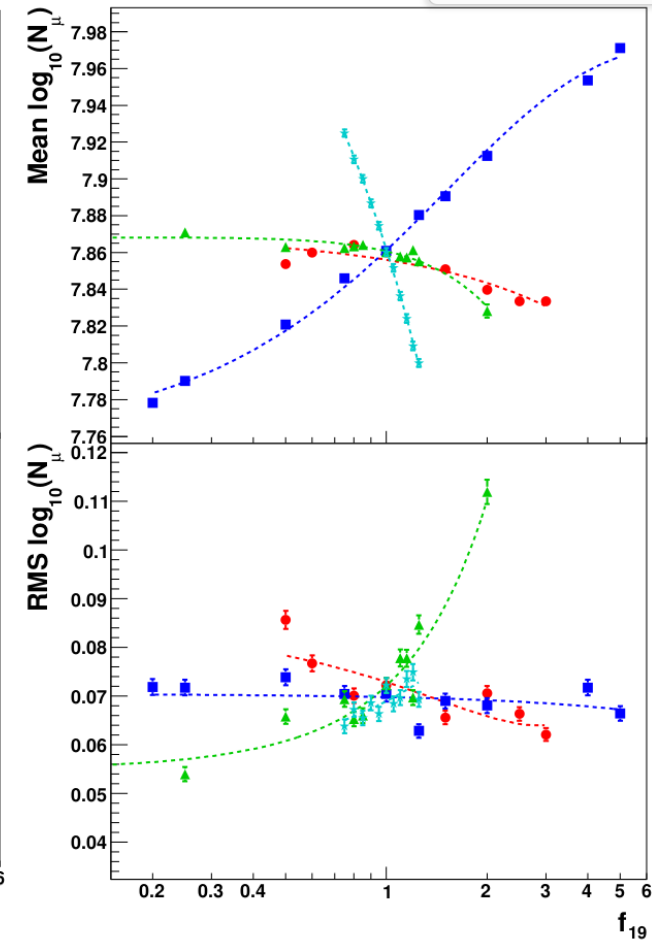
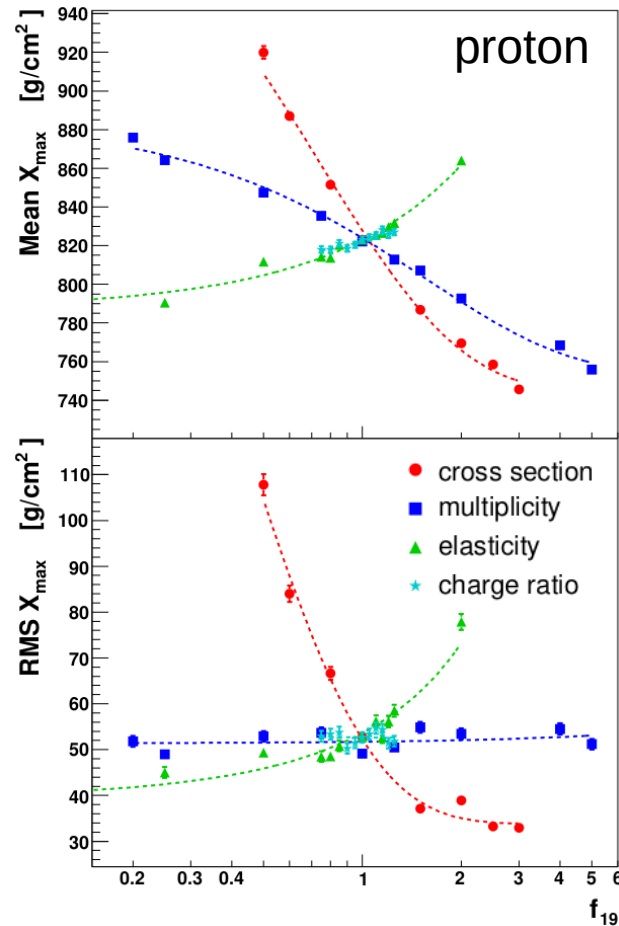


Sibyll \* - artificial enhancement of muons



# Modifications of hadronic interactions

- 1D CONEX simulations
- Sibyll 2.1 @  $10^{19.5}$  eV
- cross-section modification, or resampling of produced particles
- energy threshold for modifications  $10^{15}$  eV



[Phys. Rev. D 83 (2011) 054026]



# Towards more complex explanation: MOCHI

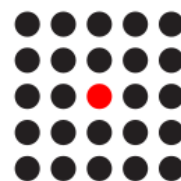
## *MO*Modified *CH*aracteristics of *H*adronic *I*nteractions

J. Ebr, J.V, J. Blažek, T. Pierog, E. Santos,  
P. Travnicek, N. Denner and R. Ulrich  
[PoS(ICRC2023)245]

- CONEX in CORSIKA: 3D information
- modification factors in **cross-section**, **multiplicity** and **elasticity**



0.8

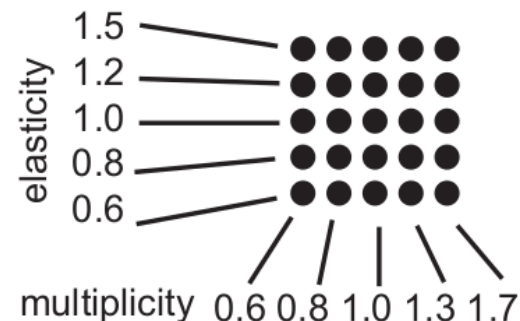


1.0



1.2

cross-section



- **MOCHI library:**

- Sibyll 2.3d
- energy  $10^{18.7}$  eV
- protons and iron nuclei
- 5 zenith angles
- 1000 showers per „bin“
- 750 000 showers (~200 TB, ~250y CPU time)

# Range of modifications and thresholds

J. Ebr, J.V., J. Blažek, T. Pierog, E. Santos,  
P. Travnicek, N. Denner and R. Ulrich  
[PoS(ICRC2023)245]

## Cross-section ( $E_{\text{thr}} = 10^{16}$ eV)

- well constrained for p-p at LHC to a few %
- unc. in conversion to p-A limited by CMS p-Pb measurement

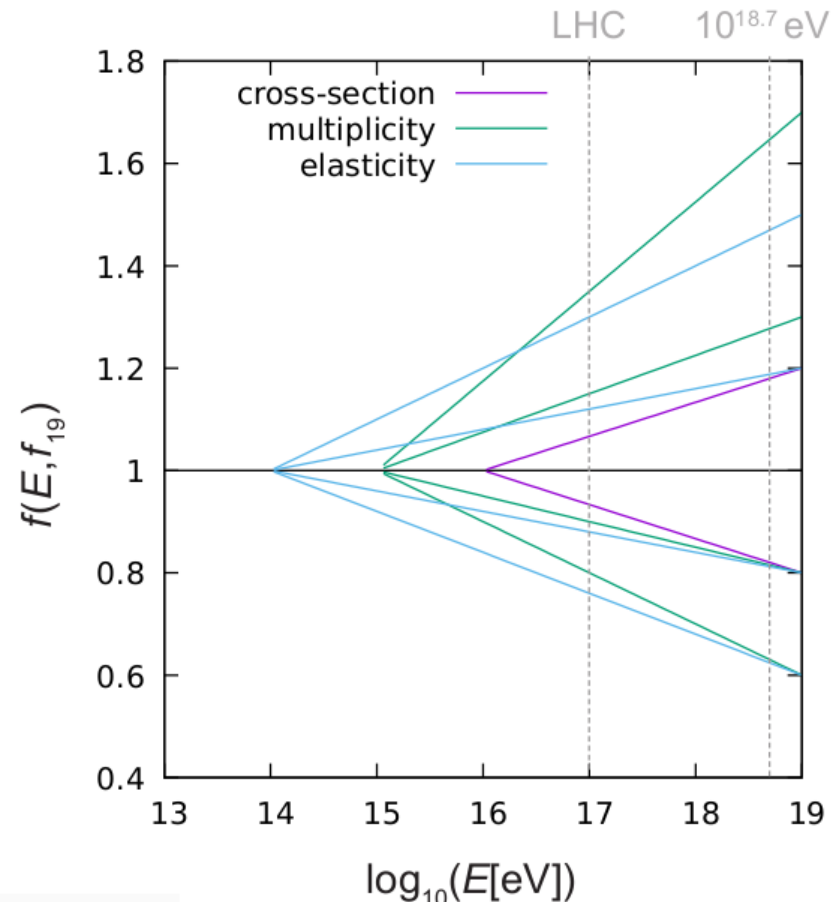
## Multiplicity ( $E_{\text{thr}} = 10^{15}$ eV)

- no p-A data, limited rapidity coverage

## Elasticity ( $E_{\text{thr}} = 10^{14}$ eV)

- difficult at accelerators, limits from nuclear emulsion chambers
- recent LHCf neutron elasticity measurement?
- range of modifications limited by internal consistency

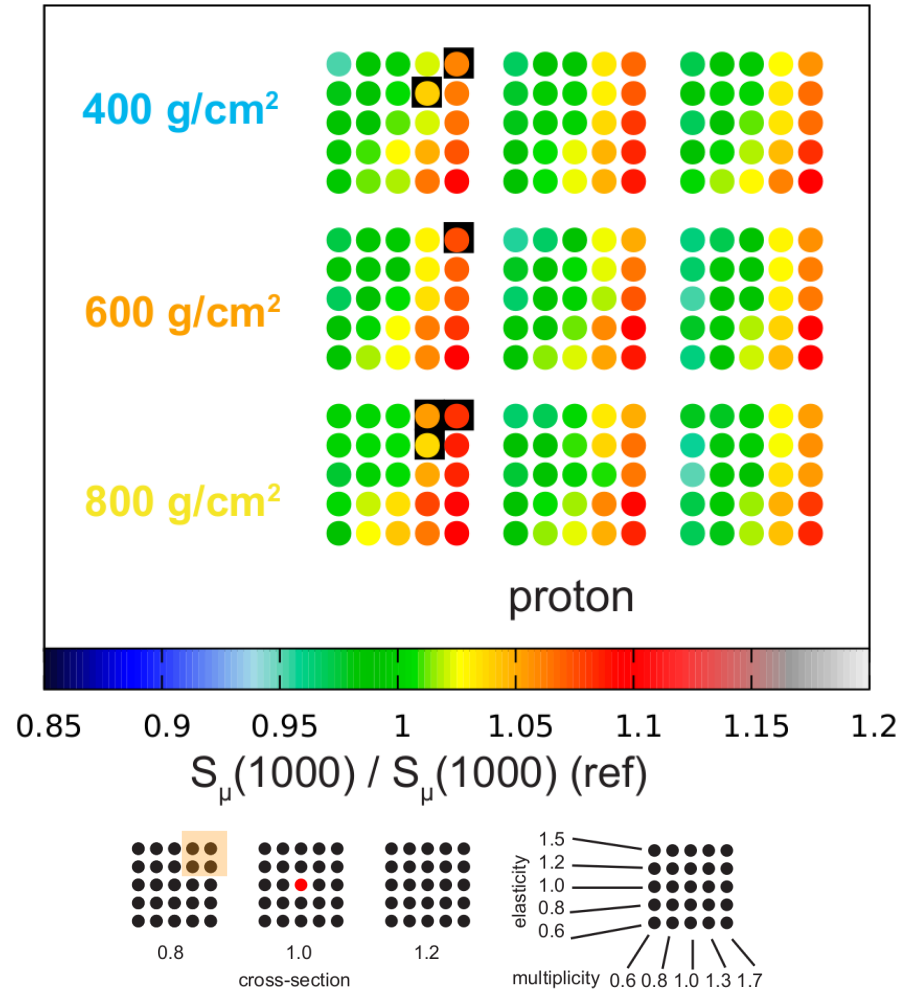
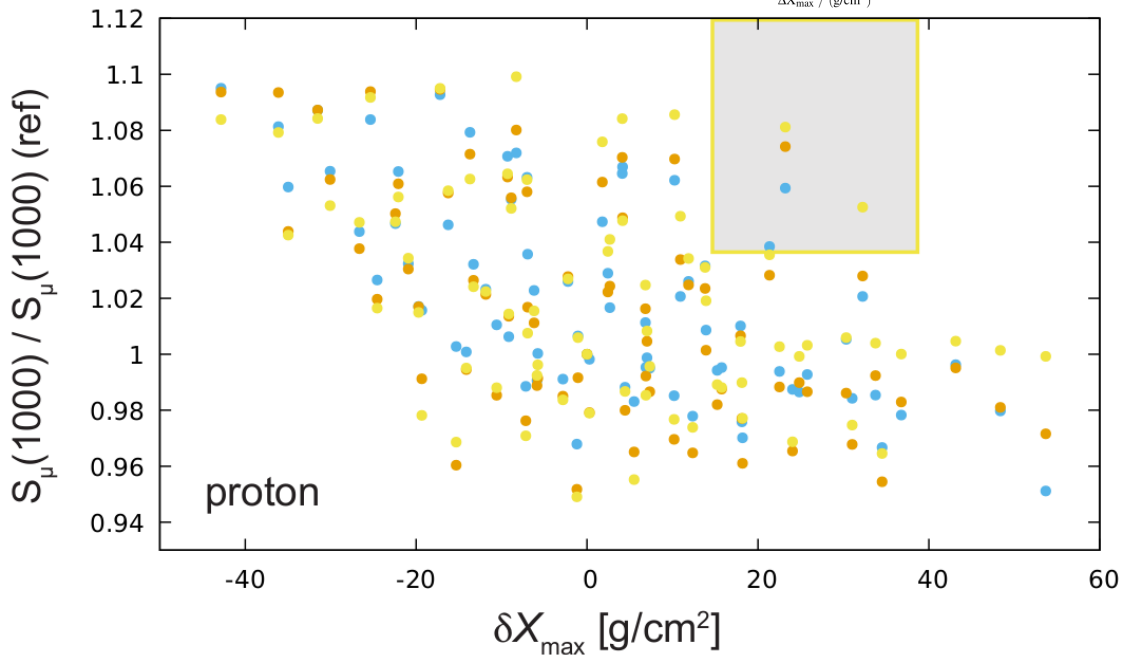
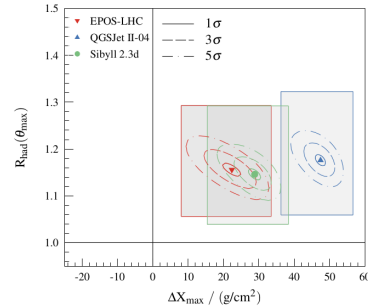
$$f(E, f_{19}) = 1 + (f_{19} - 1) \cdot \frac{\log_{10}(E/E_{\text{thr}})}{\log_{10}(10 \text{ EeV}/E_{\text{thr}})}$$



# Comparison with Auger results

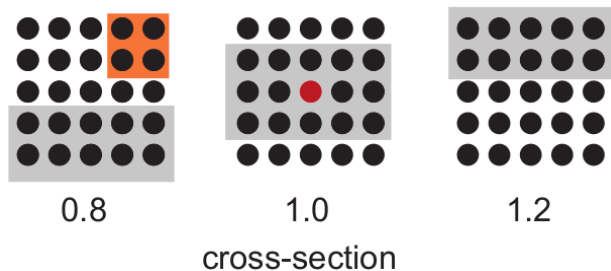
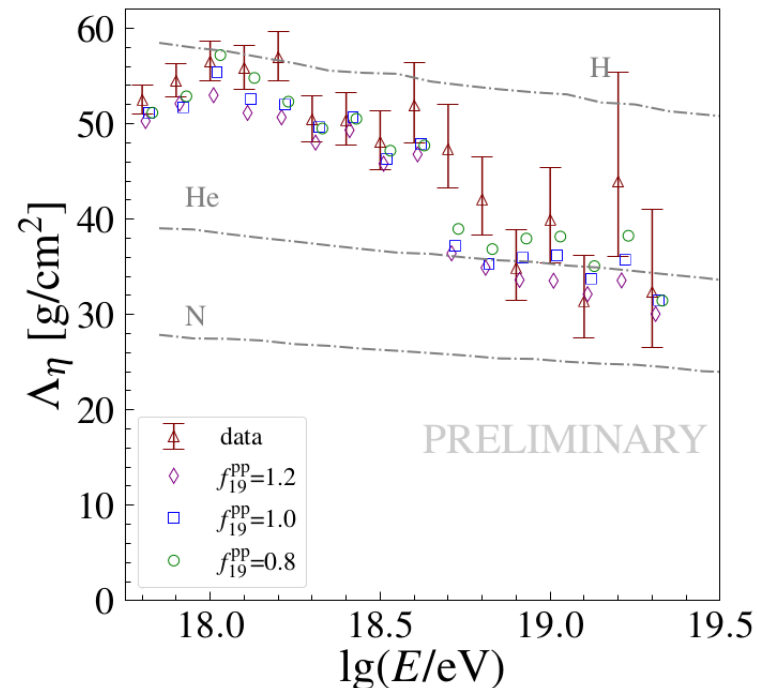
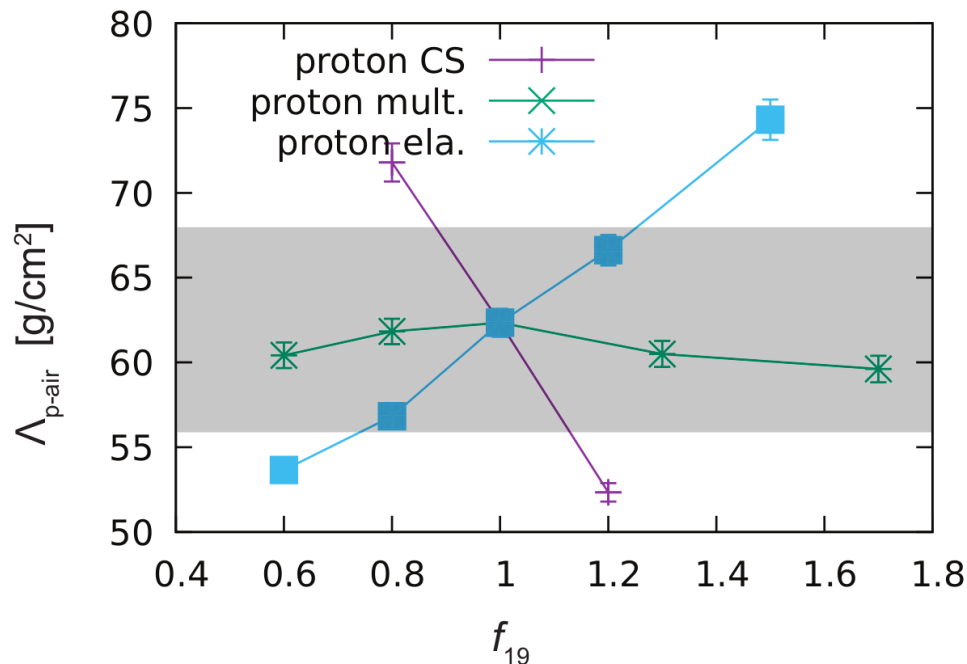
J. Ebr, J.V, J. Blažek, T. Pierog, E. Santos,  
P. Travnicek, N. Denner and R. Ulrich  
[PoS(ICRC2023)245]

[Phys. Rev. D 109 (2024) 102001]



# Effect on tail of $X_{\max}$ distribution

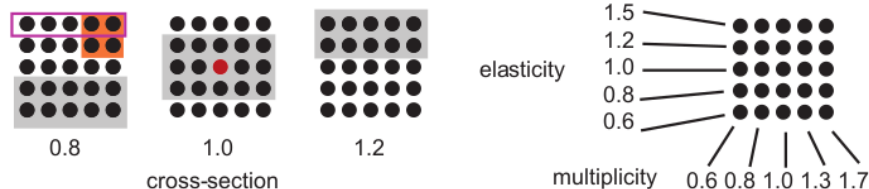
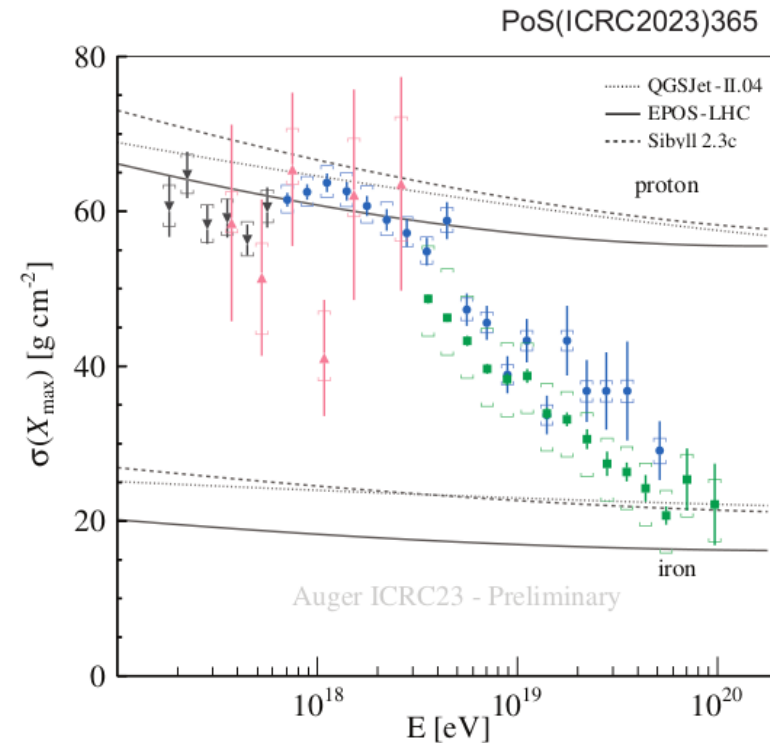
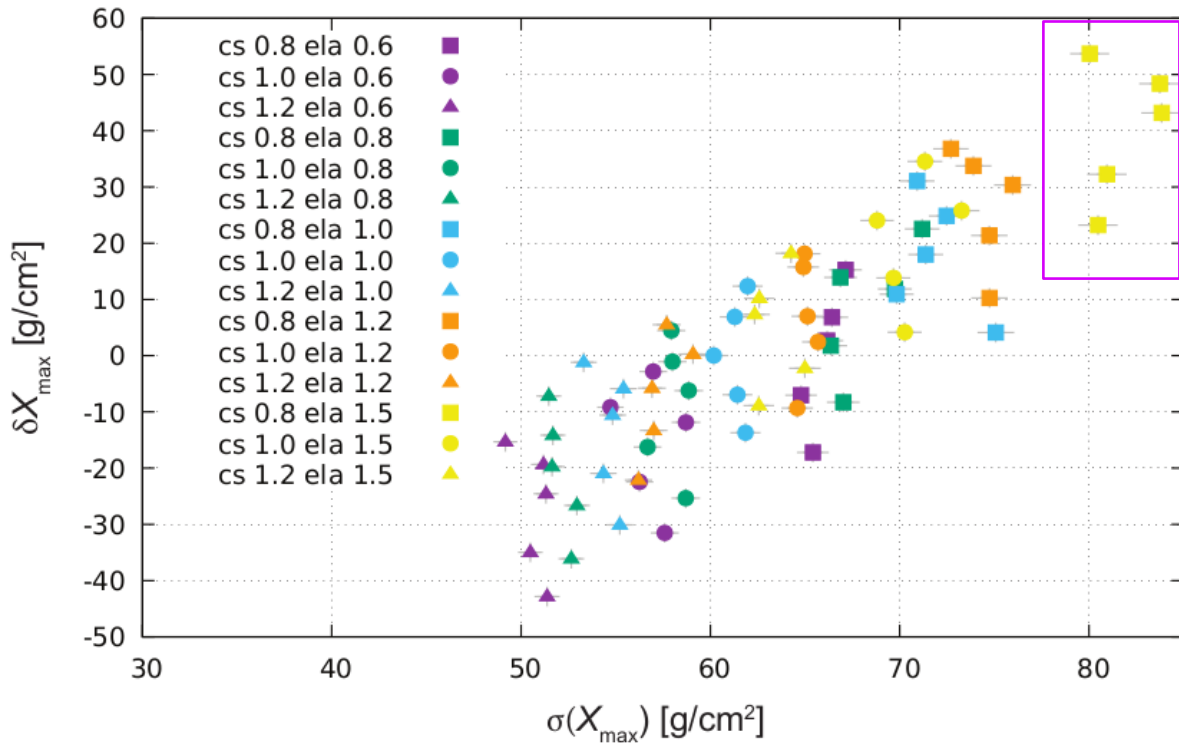
J. Ebr, JV, J. Blažek, T. Pierog, E. Santos, P. Travnicek, N. Denner and R. Ulrich [PoS(ICRC2023)245]



Slope of  $X_{\max}$  tail distribution for protons too constrained by Auger data

# Effect on $X_{\max}$ fluctuations

J. Ebr, J.V, J. Blažek, T. Pierog, E. Santos,  
P. Travnicek, N. Denner and R. Ulrich  
[PoS(ICRC2023)245]

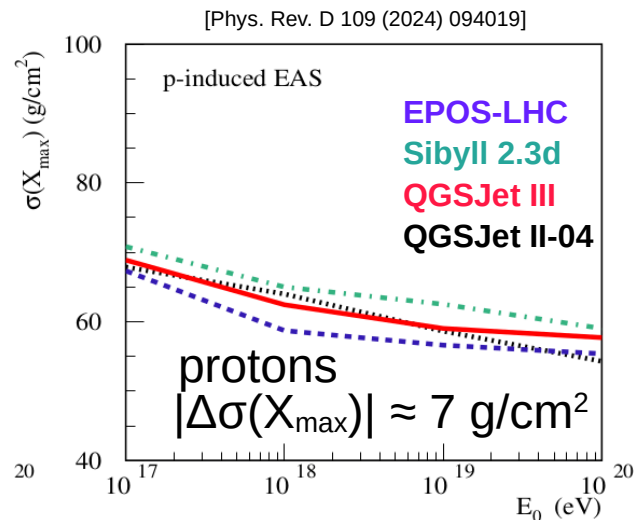


Lower cross-section and high elasticity leads to very high  $X_{\max}$  fluctuations that may be difficult to reconcile with data

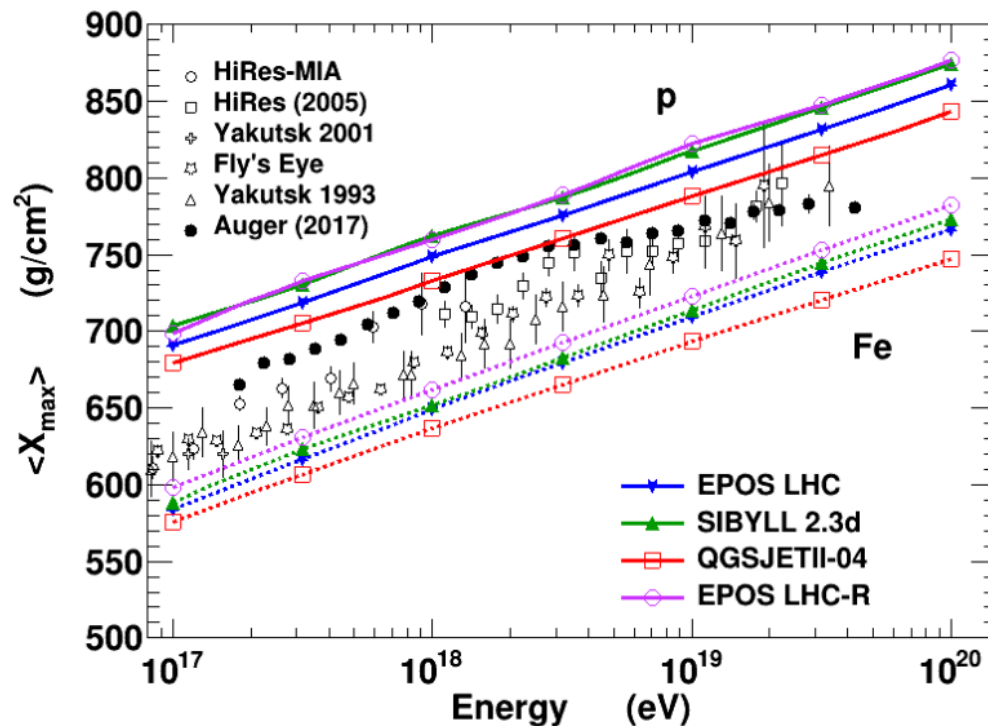
# Summary on tests of models of hadronic interactions

- $\sim 2\text{-}3\sigma$  data/MC tensions in many analyses, but some experiments are consistent
  - ➔ systematics on energy estimation is crucial ➔ **multi-detector measurements needed** and cross-calibration methods seems to be essential !
- yet, it does not seem to be a solution ➔ **connections of low and high energy tests** of model predictions are crucial for understanding the systematic uncertainties on mass composition coming from shower modelling
- **news from Auger at 3-10 EeV: current models of hadronic interactions are proven to fail to describe combined FD+SD data with more than  $5\sigma$  !**
  - possible underestimation of experimental systematics ruled out
  - possibility of a heavier mass composition (disappointing scenario) should be seriously considered !
    - ➔ alleviation of the “muon problem“ and **start of the “ $X_{\max}$  problem“**
- modifications of macro-parameters (cross-section, multiplicity, elasticity) of hadronic interactions does not seem (preliminary) to be enough
  - ➔ different approach is needed: modifying micro parameters (production rates and energy spectra of secondary particles) or (not exclusively!) revisions of models of hadronic interactions

# $X_{\max}$ fluctuations of Fe and elongation rate are very universal



[T. Pierog, EPOS-LHCR, Workshop on Tuning models of hadronic interactions]



Correction of nuclear fragmentation in EPOS :

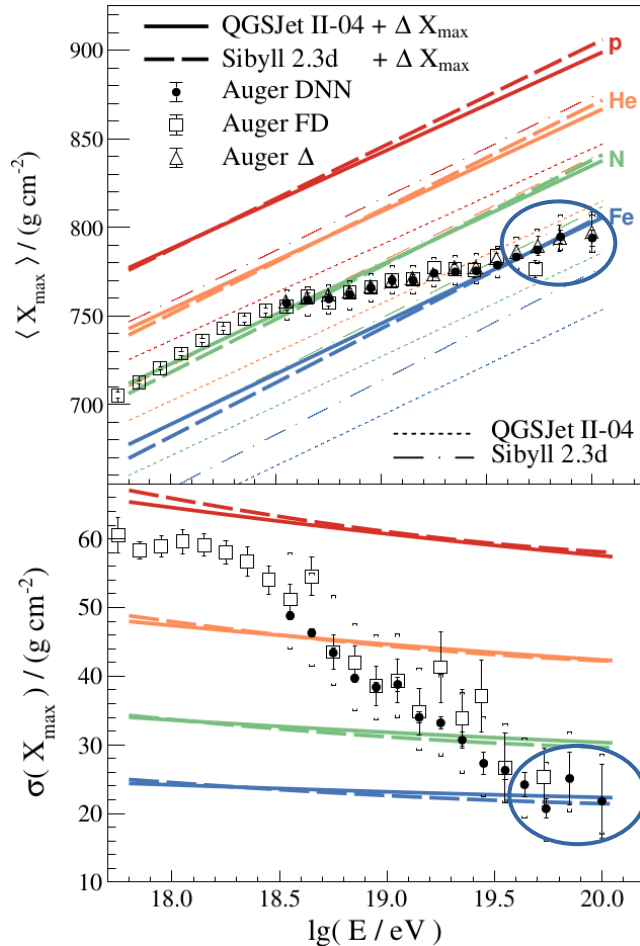
$X_{\max}$  RMS Fe  
 LHC=20g/cm<sup>2</sup>  
**LHC-R=24g/cm<sup>2</sup>**  
 SIB=25g/cm<sup>2</sup>  
 QII=25g/cm<sup>2</sup>

iron nuclei  
 $|\Delta\sigma(X_{\max})| \approx 1 \text{ g/cm}^2$

$|\Delta D_{10}| \approx 4 \text{ g/cm}^2 / \lg E$

# Heavy-metal scenario

[JV, A. Bakalová, O. Tkachenko, A. L. Müller, M. Stadelmaier, UHECR 2024]



## Assumptions

- $X_{\max}$  fluctuations and elongation rate from QGSJet II-04 and Sibyll 2.3d (bug in EPOS-LHC)
- pure Fe nuclei above  $10^{19.6}$  eV ( $\sim 40$  EeV)
- freedom in the predicted  $X_{\max}$  scale derived from Auger DNN [accepted in PRD, arXiv:2406.06319]

$$\Rightarrow \Delta X_{\max} = 52 \pm 1 \begin{matrix} +11 \\ -8 \end{matrix} \text{ g/cm}^2 \text{ for QGSJET-II-04}$$

$$\Rightarrow \Delta X_{\max} = 29 \pm 1 \begin{matrix} +12 \\ -7 \end{matrix} \text{ g/cm}^2 \text{ for SIBYLL 2.3d}$$

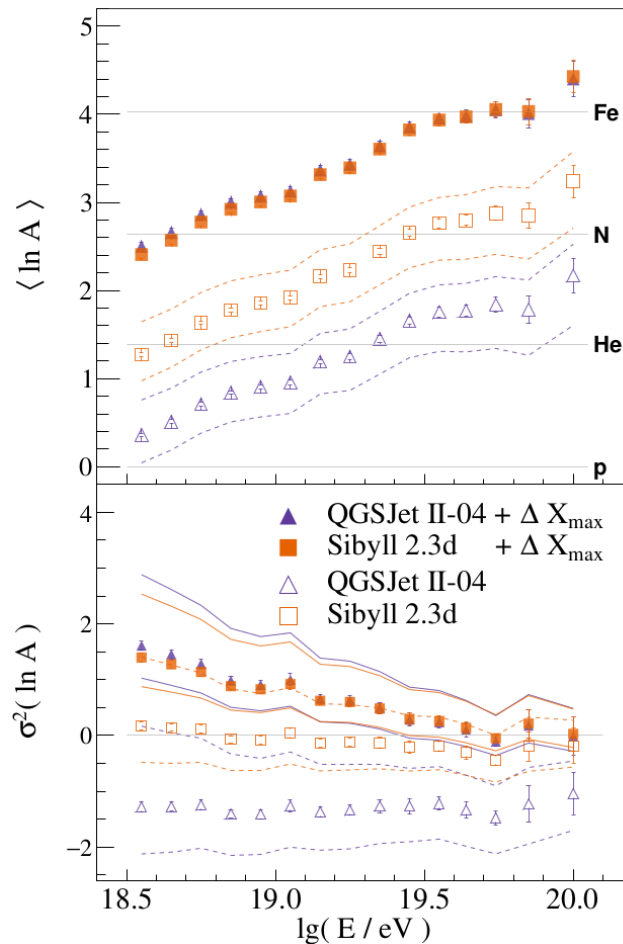
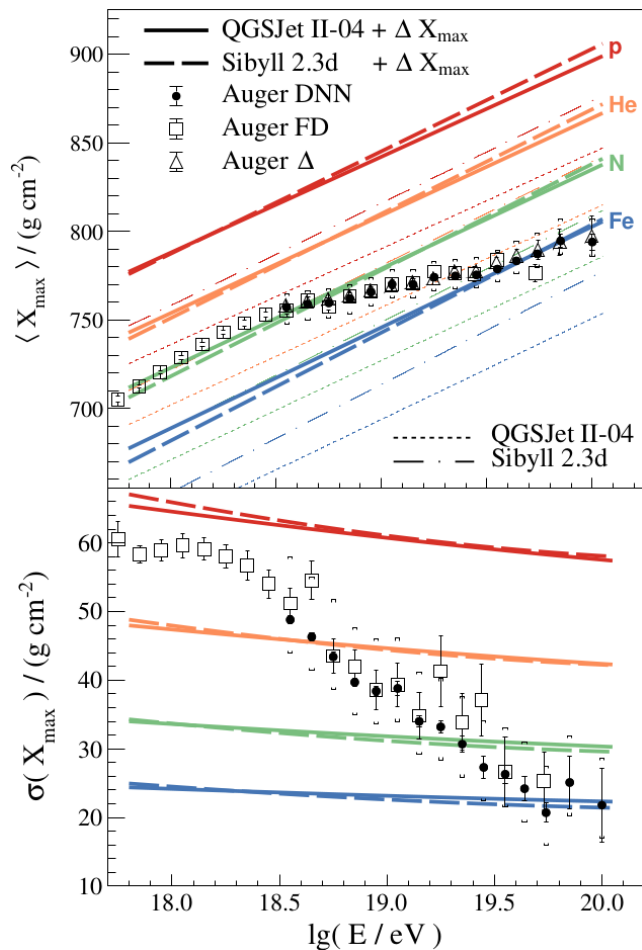
[Phys. Rev. D 109 (2024) 102001]

	$R_{\text{had}}(\theta_{\min})$	$R_{\text{had}}(\theta_{\max})$	$\Delta X_{\max}/(\text{g/cm}^2)$
EPOS-LHC	$1.15 \pm 0.01 \begin{matrix} +0.20 \\ -0.16 \end{matrix}$	$1.16 \pm 0.01 \begin{matrix} +0.14 \\ -0.10 \end{matrix}$	$22 \pm 3 \begin{matrix} +11 \\ -14 \end{matrix}$
QGSJET-II-04	$1.24 \pm 0.01 \begin{matrix} +0.22 \\ -0.19 \end{matrix}$	$1.18 \pm 0.01 \begin{matrix} +0.15 \\ -0.12 \end{matrix}$	$47 \begin{matrix} +2 & +9 \\ -1 & -11 \end{matrix}$
SIBYLL 2.3d	$1.18 \pm 0.01 \begin{matrix} +0.21 \\ -0.17 \end{matrix}$	$1.15 \pm 0.01 \begin{matrix} +0.15 \\ -0.11 \end{matrix}$	$29 \pm 2 \begin{matrix} +10 \\ -13 \end{matrix}$



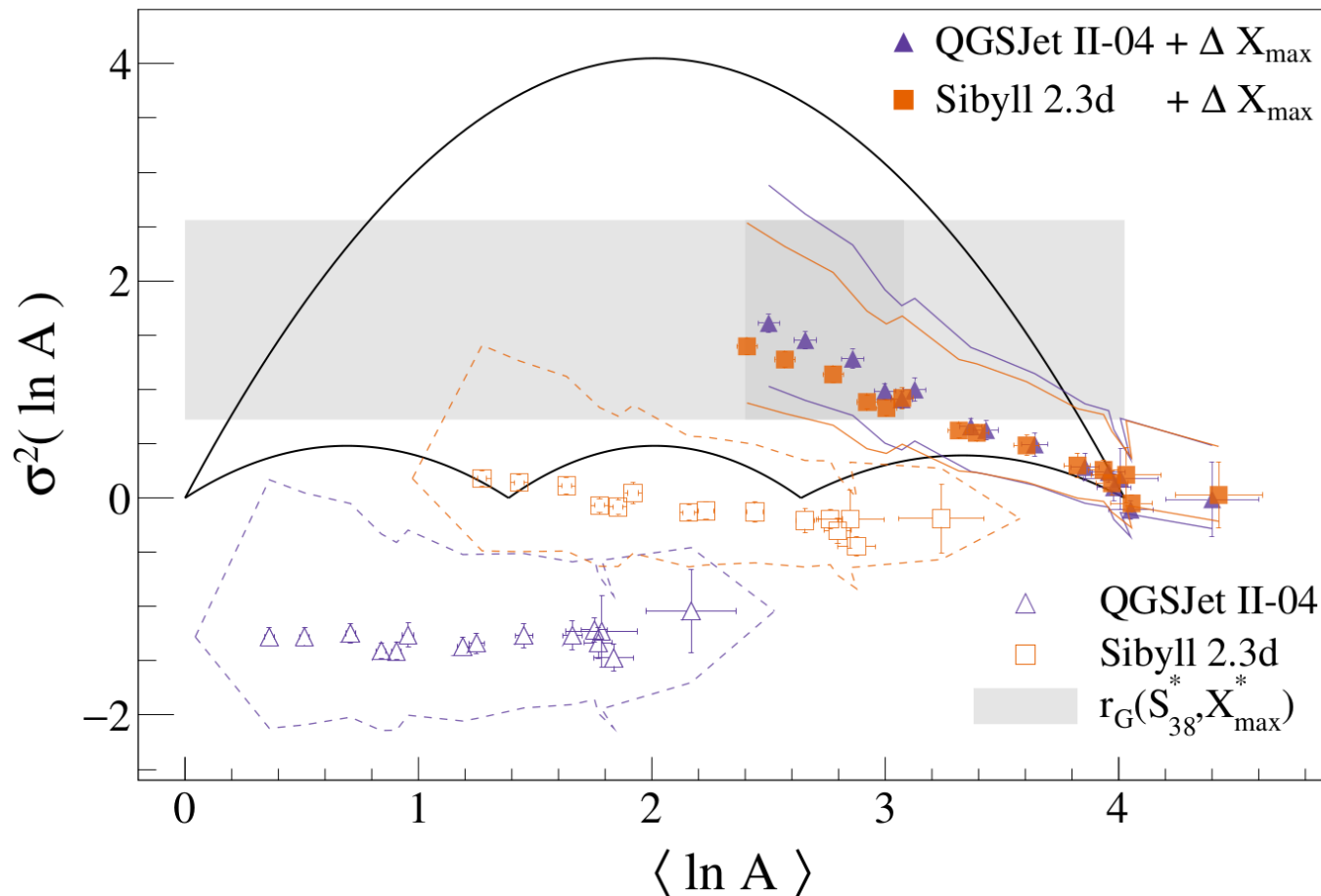
# Heavy-metal scenario: In A moments

[JV, A. Bakalová, O. Tkachenko, A. L. Müller, M. Staelmaier, UHECR 2024]



# Heavy-metal scenario: In A moments

[JV, A. Bakalová, O. Tkachenko, A. L. Müller, M. Stadelmaier, UHECR 2024]



- $\Delta X_{\max}$  consistent with results from  $[X_{\max}, S(1000)](\theta)$  fits

[Phys. Rev. D 109 (2024) 102001]

- $\sigma^2(\ln A)$  consistent with result from  $X_{\max}$ - $S_{38}$  correlation

[Phys. Lett. B 762 (2016) 288]

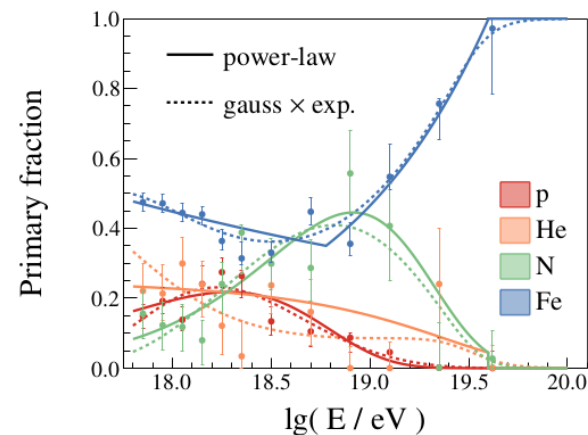
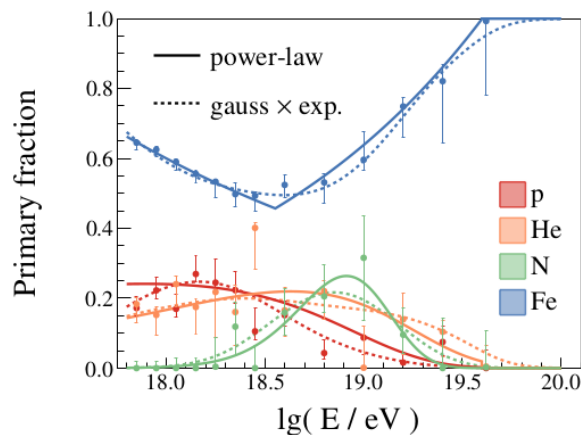
- umbrella plot,  $\sigma^2(\ln A)$  vs.  $\langle \ln A \rangle$ , generally more physical

# Heavy-metal scenario: energy evolution of individual primary fractions and fluxes

[JV, A. Bakalová, O. Tkachenko, A. L. Müller, M. Stadelmaier, UHECR 2024]

1) parameterization of energy evolution of primary fractions using Auger  $X_{\max}$  data

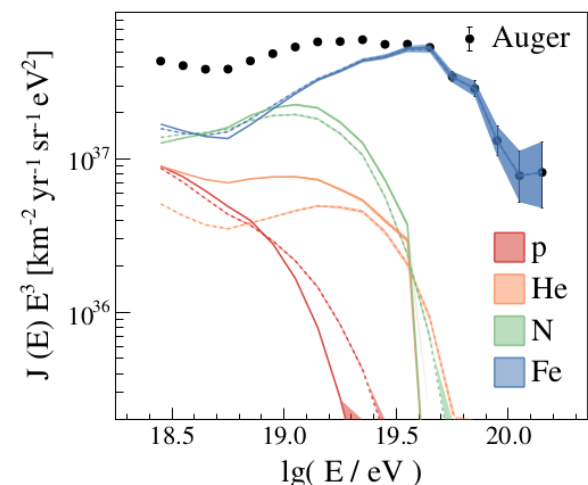
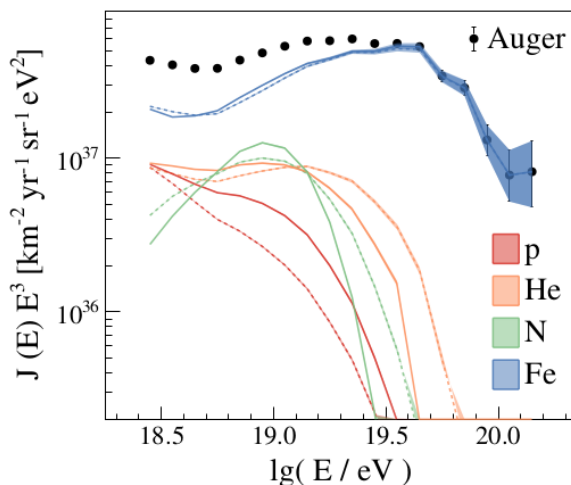
[Phys. Rev. D 90 (2014) 122005]



2) derivation of fluxes of primary species from Auger energy spectrum

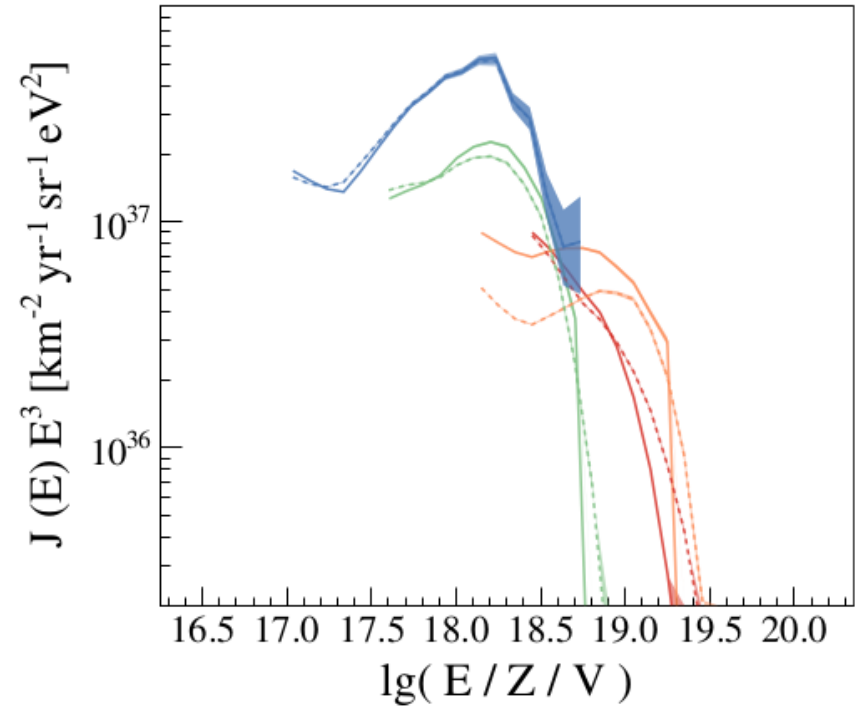
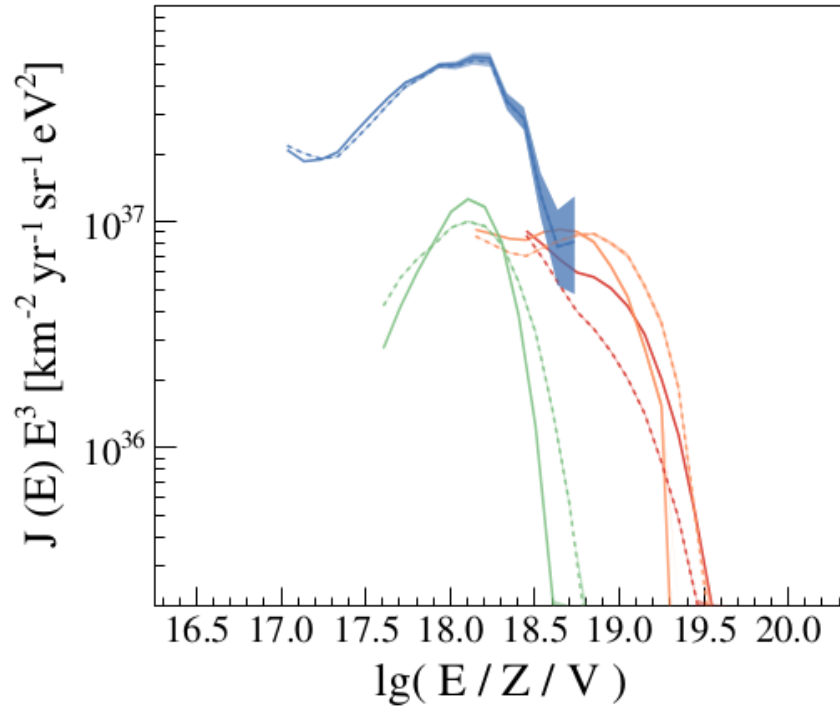
[PRD 102 (2020) 062005]

instep feature ( $\sim 15$  EeV) caused by fading of N



# Heavy-metal scenario: energy evolution of rigidity ( $E/Z$ )

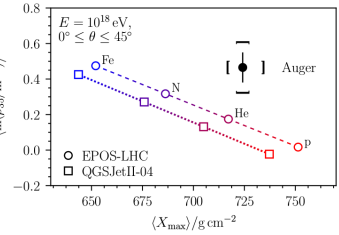
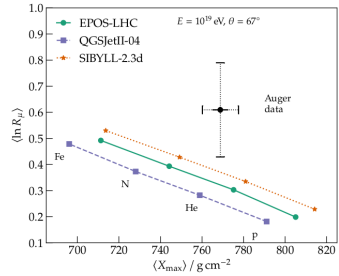
[JV, A. Bakalová, O. Tkachenko, A. L. Müller, M. Stadelmaier, UHECR 2024]



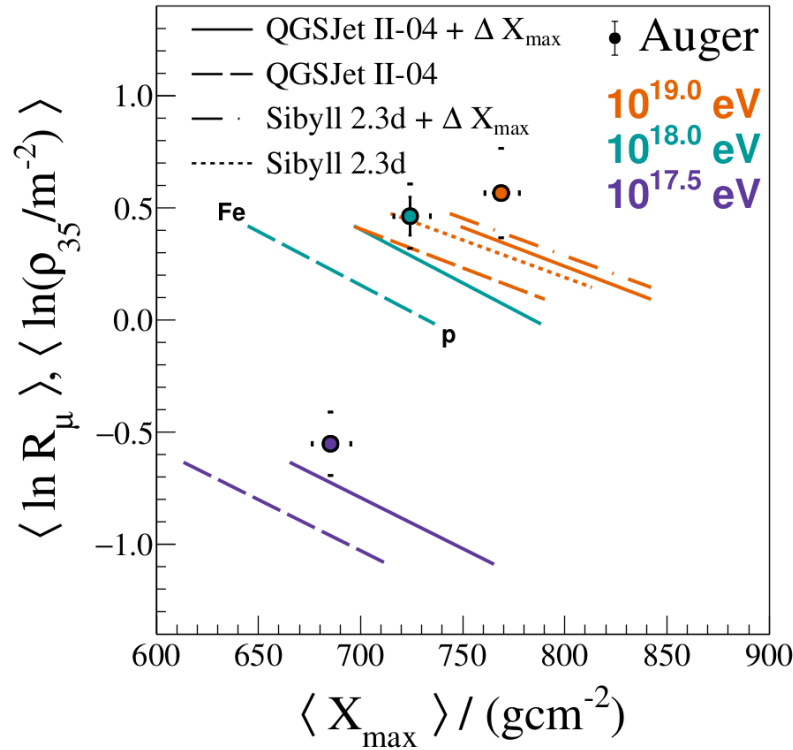
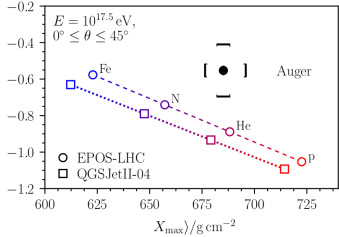
Fe and N nuclei might have a common origin

# Heavy-metal scenario: number of muons

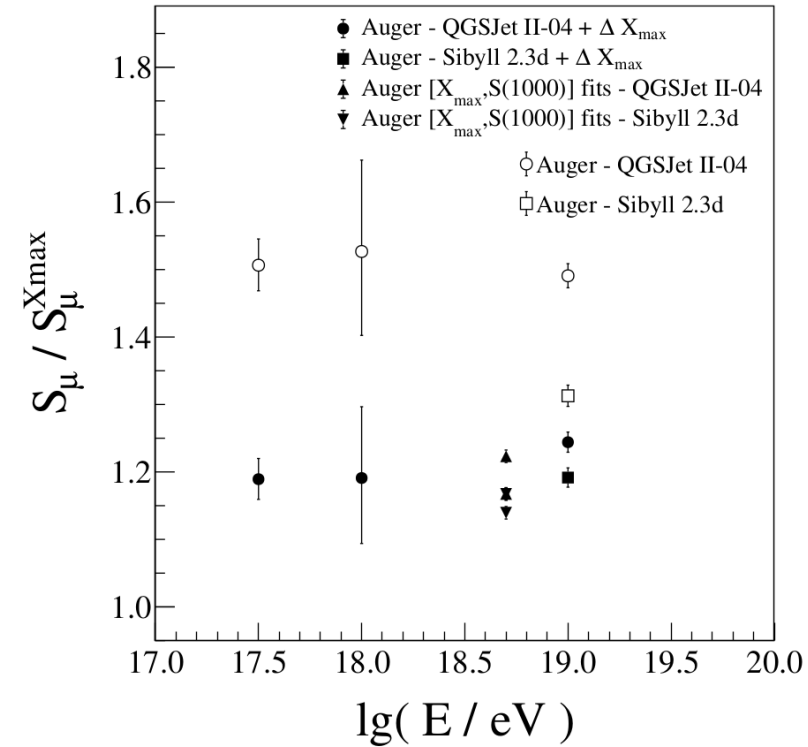
[Phys. Rev. Lett. 126 (2021) 152002]



[Eur. Phys. J. C 80 (2020) 751]



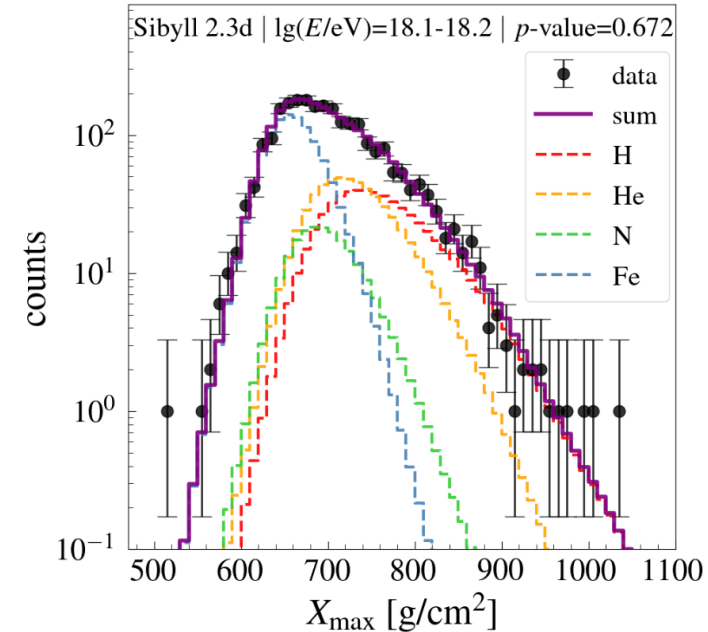
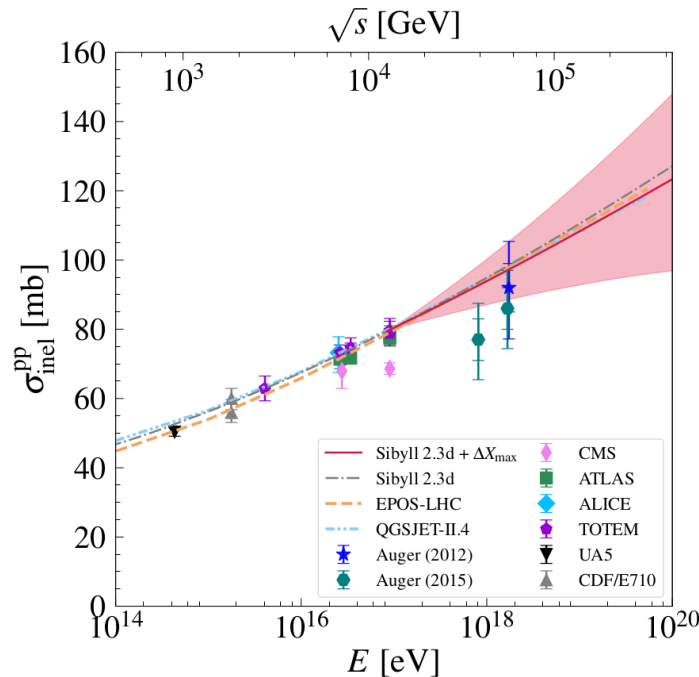
[JV, A. Bakalová, O. Tkachenko, A. L. Müller, M. Stadelmaier, UHECR 2024]



Muon problem alleviated to ~20%, ~independently on energy

# Heavy-metal scenario: cross-section modification

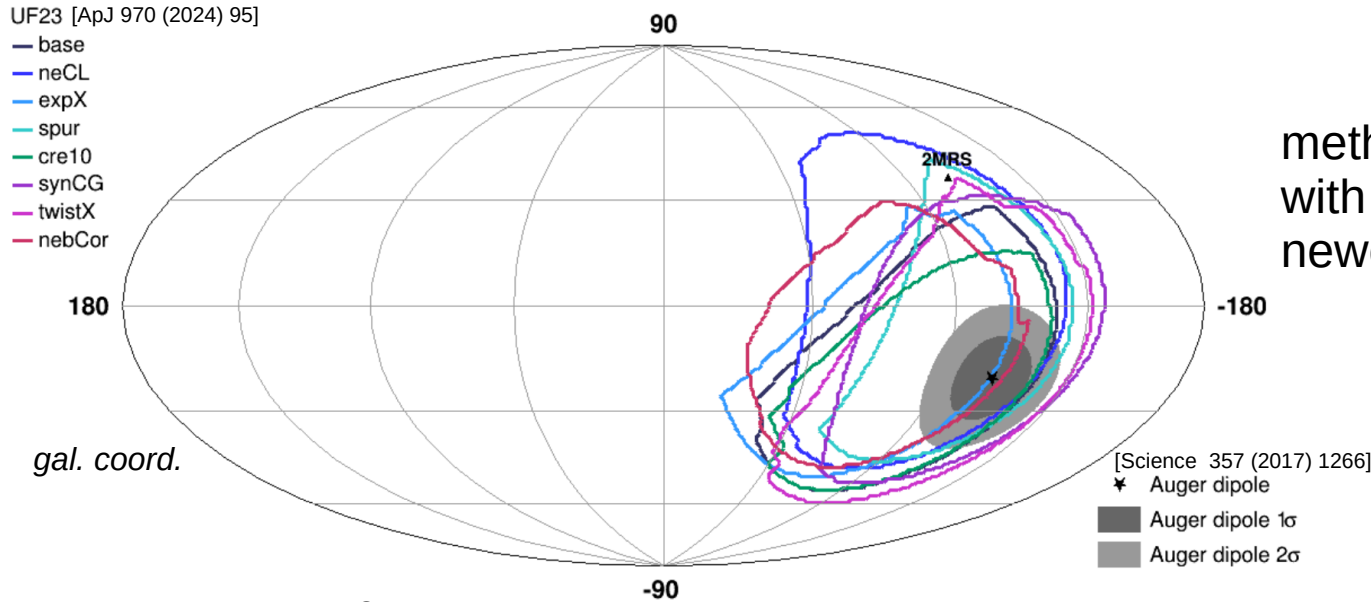
[JV, A. Bakalová, O. Tkachenko, A. L. Müller, M. Stadelmaier, UHECR 2024]



- $X_{\max}$  data from [Phys. Rev. D 90 (2014) 122005] , method from [O. Tkachenko for Pierre Auger Coll. PoS(ICRC2023)438]
- no modification of cross-section in models is needed
- very good description of  $X_{\max}$  distributions obtained

# Heavy-metal scenario: backtracking in Galactic magnetic field

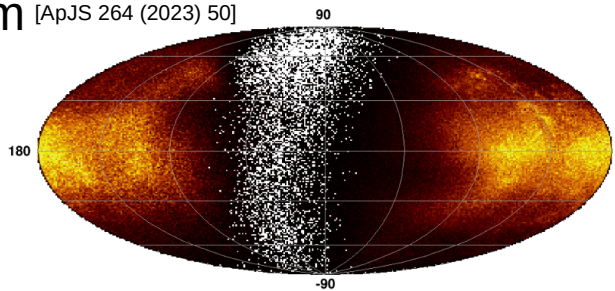
[JV, A. Bakalová, O. Tkachenko, A. L. Müller, M. Stadelmaier, UHECR 2024]



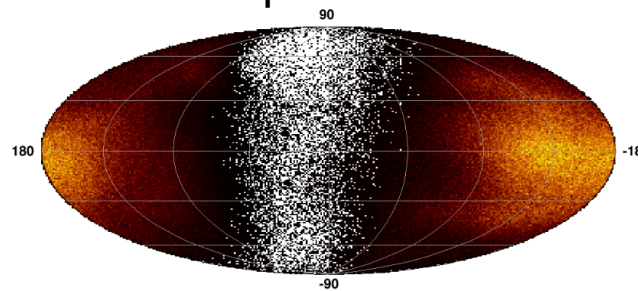
method from [A. Bakalová, JV, P. Trávníček, JCAP12 (2023) 016]  
with H-m composition and newer model of GMF

➔ constraints on direction of an extragalactic dipole above 8 EeV

89 events,  $E > 78$  EeV,  $\theta < 60^\circ$  as Fe,  
from [ApJS 264 (2023) 50]



Isotropic distribution

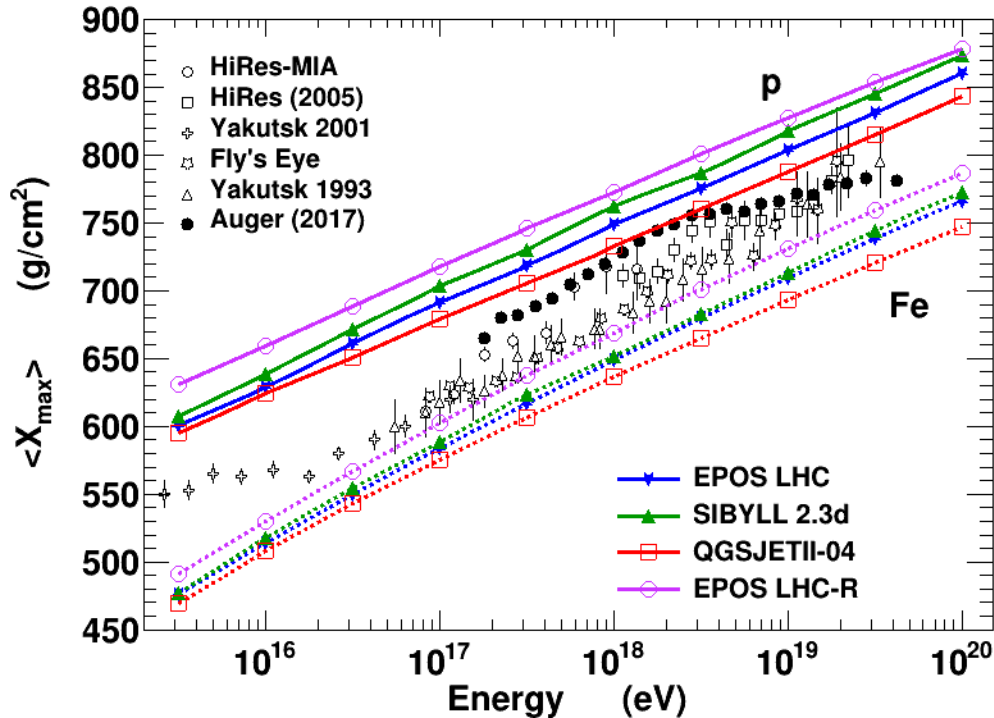


low rigidity causing de-magnification of sources towards GC

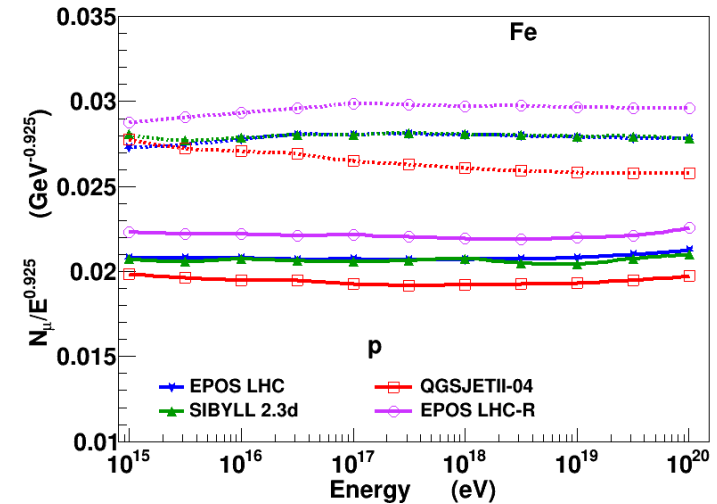
# EPOS-LHCR is approaching !

[T. Pierog, Dec 2024 - CRs and  $\nu$  in MM era, APC, Paris, France]

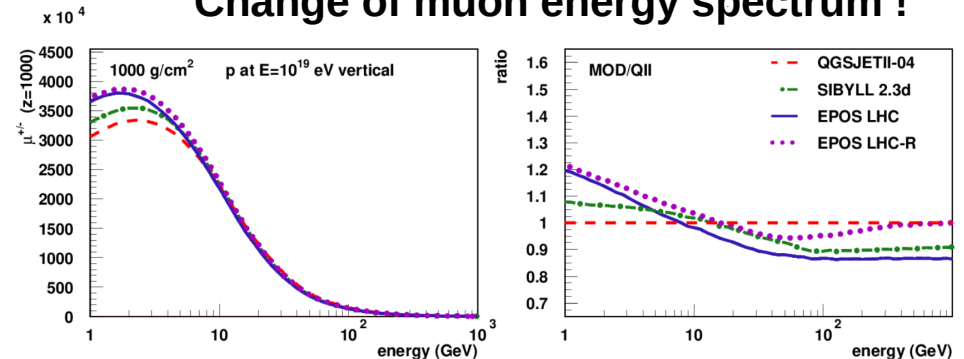
Deeper  $X_{\max}$  by  $\sim 20\text{-}30 \text{ g/cm}^2$ !



More muons by  $\sim 10\%$  !



Change of muon energy spectrum !

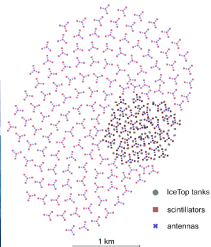
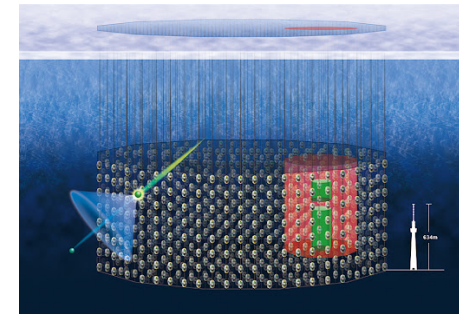
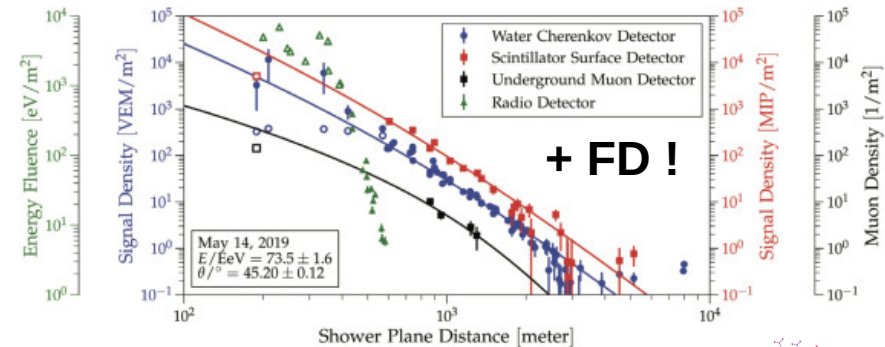




# More air-shower studies yet to come! Stay tuned

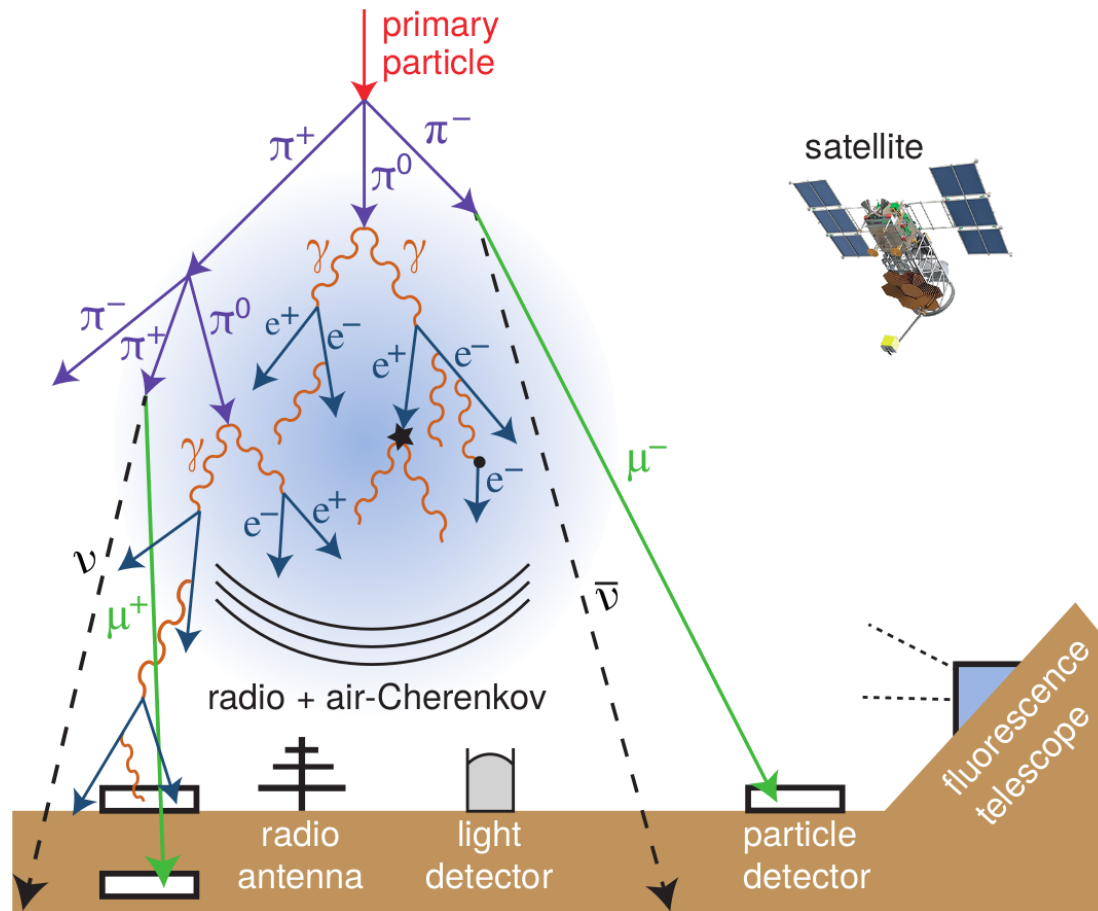
- **new models** of hadronic interactions (EPOS 4(LHCR), QGSJet III, Sibyll \*\*, ...) and **new air-shower generator** (CORSIKA 8) are expected to decrease the systematic uncertainties on mass composition of cosmic rays
  - ➔ **p + O collisions at the end of Run 3** at LHC are very important !
- **AugerPrime** (2024-2035) will be the best testing facility for forward hadronic interactions at  $\sqrt{s} \sim 10\text{-}200$  TeV
- + **IceCube-Gen2** (2032-?) at  $\sqrt{s} \sim 1\text{-}50$  TeV
- + **LHAASO** (2023-?) at  $\sqrt{s} \sim 0.1\text{-}1$  TeV ?
- and new methods (Machine Learning) and more data ...

Thank you for your attention !



# Backup slides

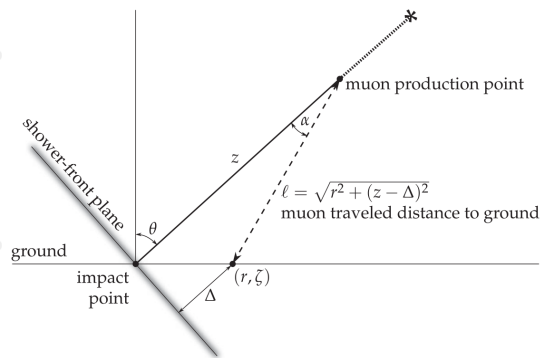
# Air-shower Measurements



# Observables relevant to hadronic interaction models

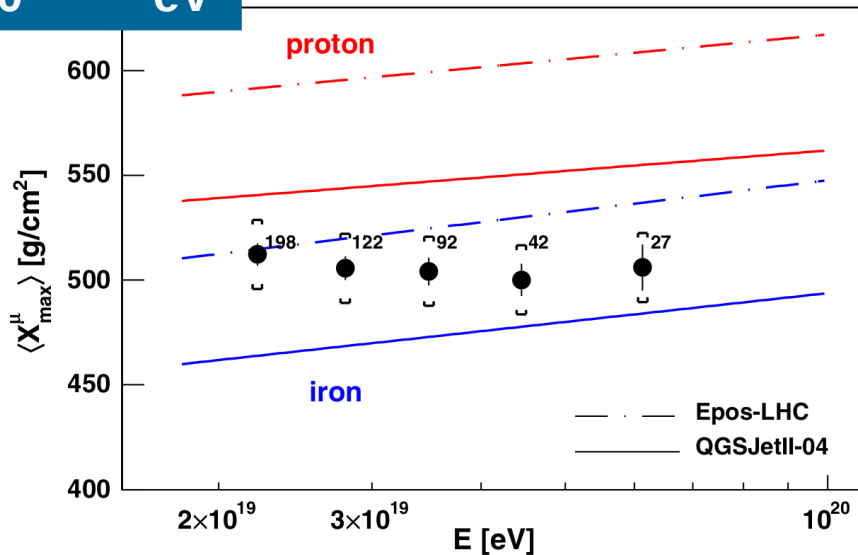
## SD signal

- muon content
  - from buried scintillators,  $\theta < 60^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$
- muon production depth
  - for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$

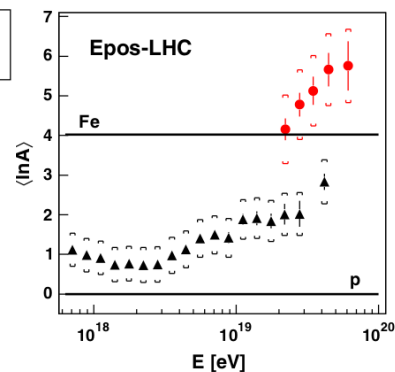
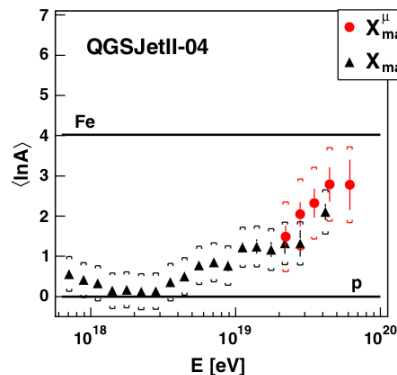
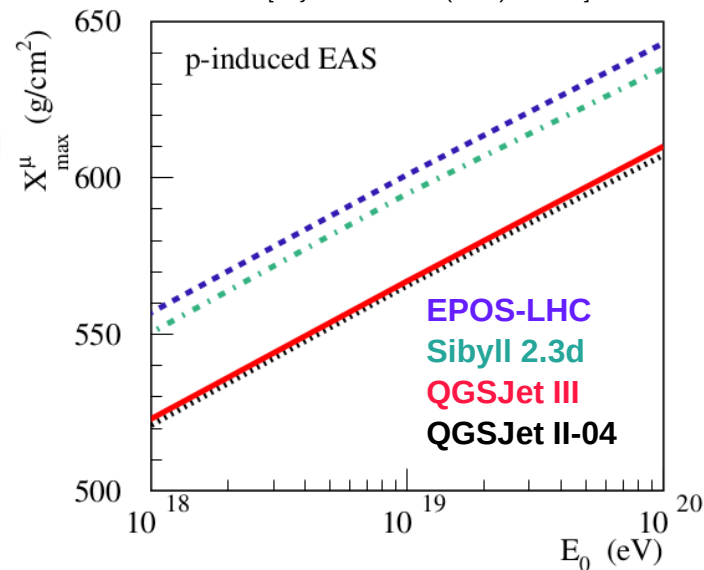


$10^{19.3-19.8}$  eV

[Phys. Rev. D 90 (2014) 012012]



[Phys. Rev. D 109 (2024) 094019]



- EPOS-LHC and (likely also) Sibyll 2.3d too deep  $\sim 2\sigma$
- MPD tunable by pion diffraction (loosely constrained by current accelerators data)

# Observables relevant to hadronic interaction models

## SD signal

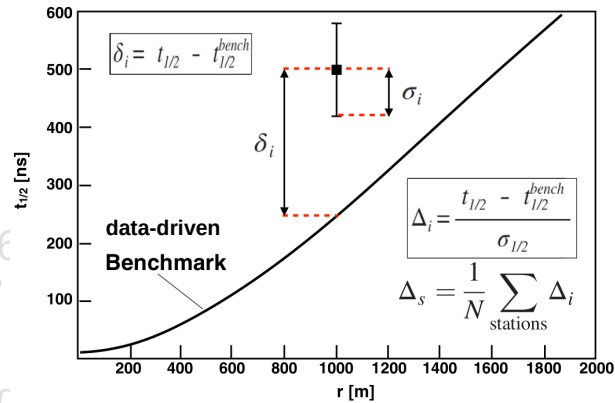
- muon content
- from buried scintillators,  $\theta < 65^\circ$
- from  $N_{19}$ ,  $\theta > 65^\circ$

- muon production  $\rho_{\text{mu}}$
- for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$

- muon energy spectrum
- from attenuation with  $\theta$  and  $r$

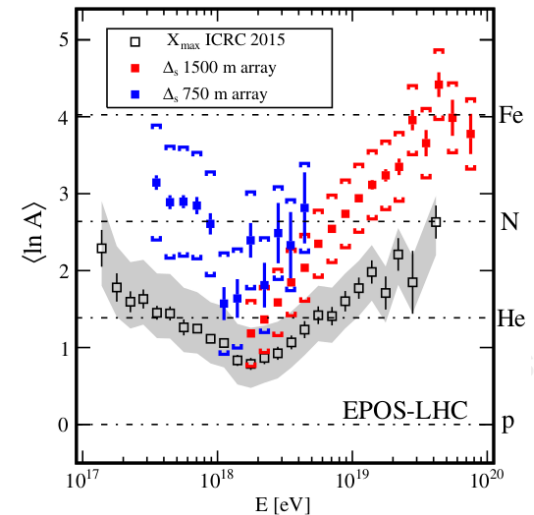
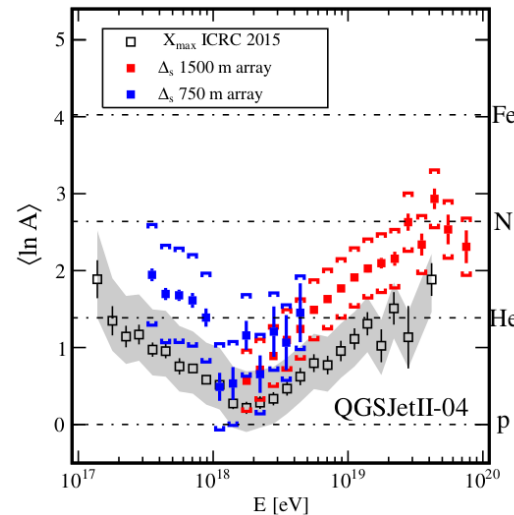
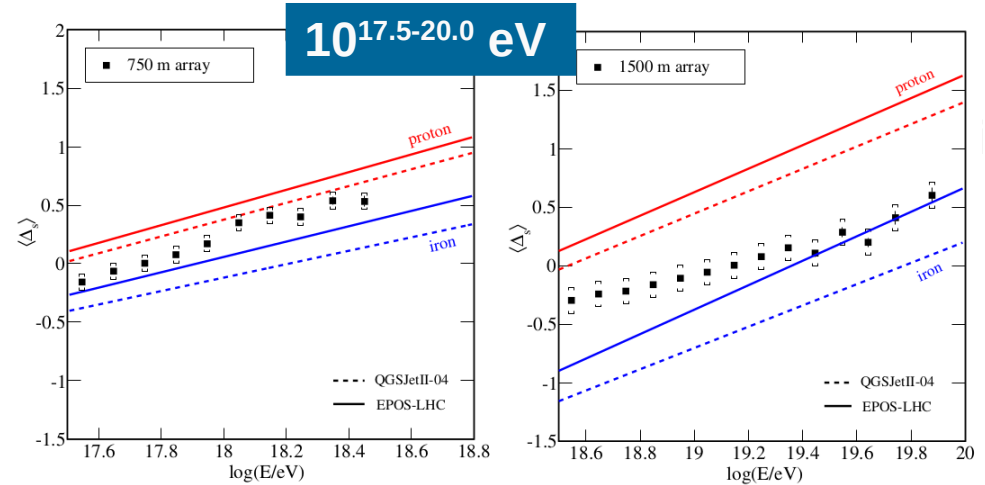
- rise time of signal vs.  $r$

[Phys. Rev. D 96 (2017) 122003]



$$\langle \ln A \rangle = \ln 56 \frac{\langle \Delta_s \rangle_p - \langle \Delta_s \rangle_{\text{data}}}{\langle \Delta_s \rangle_p - \langle \Delta_s \rangle_{\text{Fe}}}$$

**~1-2 $\sigma$  inconsistent interpretation of  $\langle \ln A \rangle$  between  $\Delta_s$  and  $X_{\text{max}}$**



# Observables relevant to hadronic interaction models

[JCAP 03 (2019) 018]

**10<sup>17.8-19.5</sup> eV**

SD signal

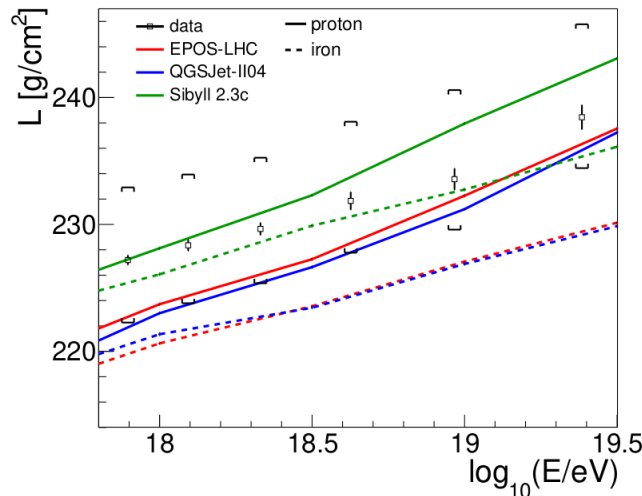
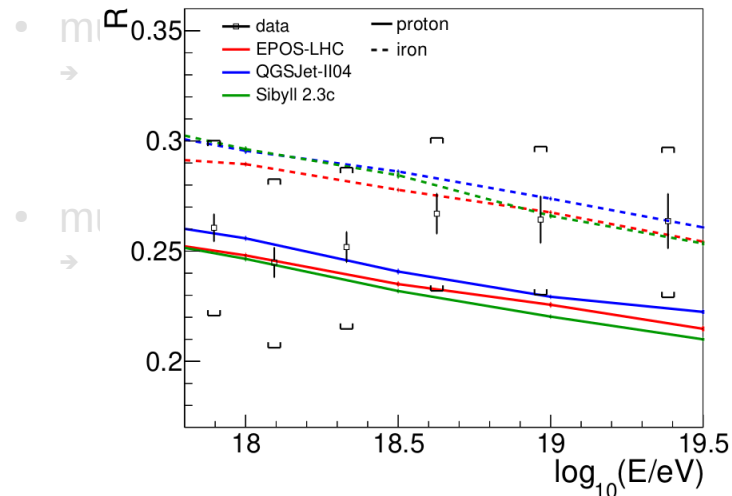
$$f_{GH}(X) = (dE/dX)_{\max} \left( \frac{X - X_0}{X_{\max} - X_0} \right)^{\frac{X_{\max} - X_0}{\lambda}} \exp \left( -\frac{X_{\max} - X}{\lambda} \right)$$

$$(dE/dX)' = \left( 1 + R \frac{X'}{L} \right)^{R-2} \exp \left( -\frac{X'}{RL} \right)$$

FD longitudinal profile

- muon content
  - from buried scintillators,  $\theta < 60^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$

- so far consistent within  $\sim 2\sigma$  with models
- smaller systematics on aerosol measurement could improve constraints



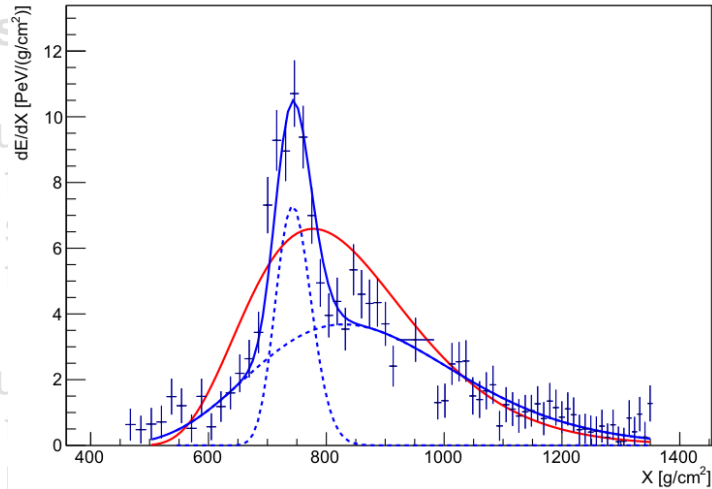
- average shape of longitudinal profiles

# Observables relevant to hadronic interaction models

[EPJ Web Conf. 144 (2017) 01009]  
FD profile

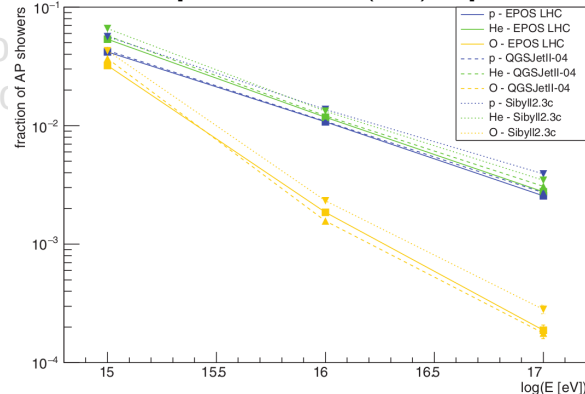
$10^{17.2-18.5}$  eV ?

FD longitudinal profile

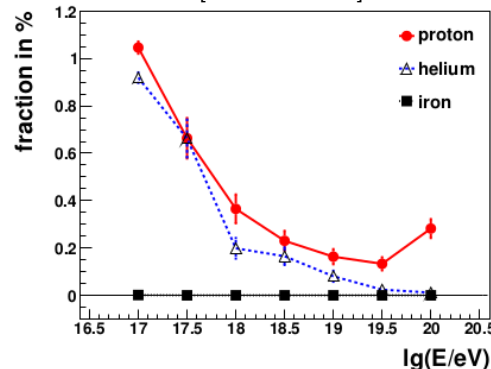


- % effect at  $10^{18}$  eV, % effect at  $10^{16}$  eV
- hard to reject presence of clouds  
→ additional cloud measurement is needed
- possible constraints on presence of lightest primaries (and cross-section/elasticity)
- no application to the data yet

[Astron. Nachr. 340 (2019) 234]



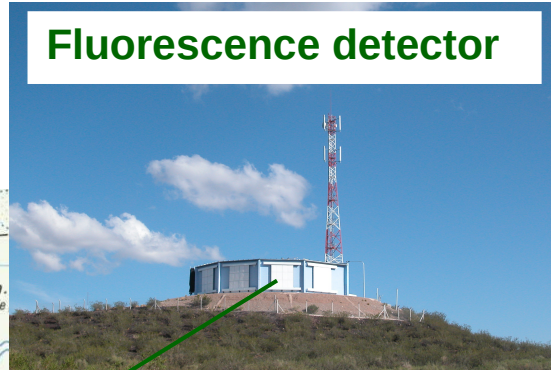
[arXiv:1111.0504]



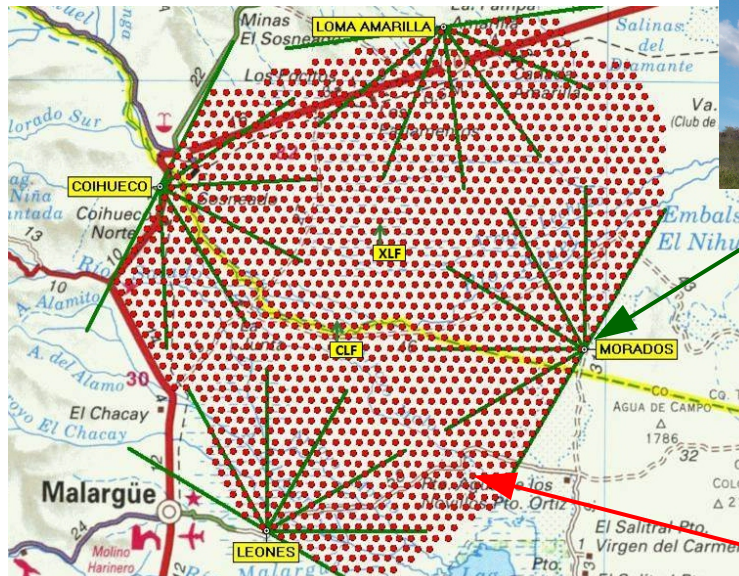
- average shape of longitudinal profiles
- frequency of **anomalous showers**

# Hybrid detection at the Pierre Auger Observatory

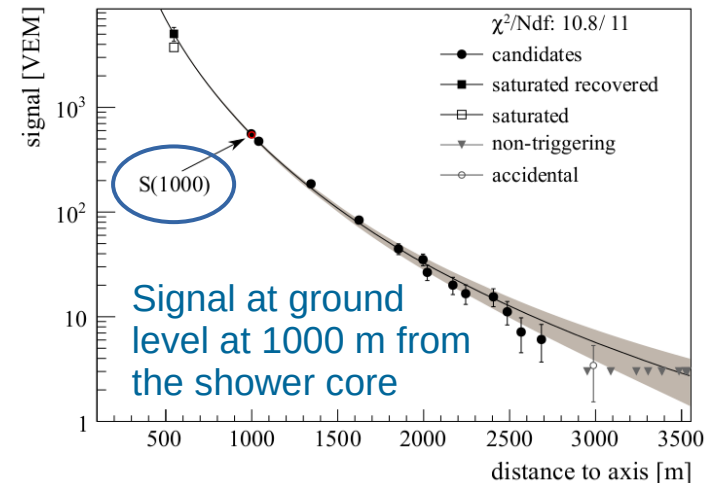
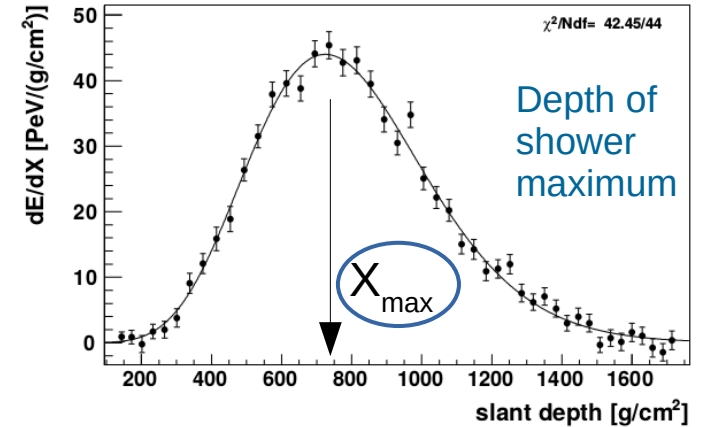
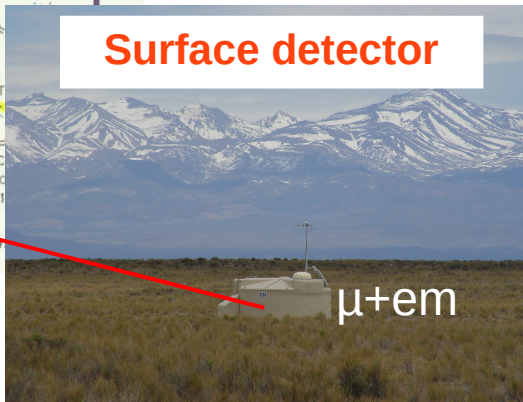
Fluorescence detector



[Nucl. Instrum. Meth. A 798 (2015) 172]



Surface detector





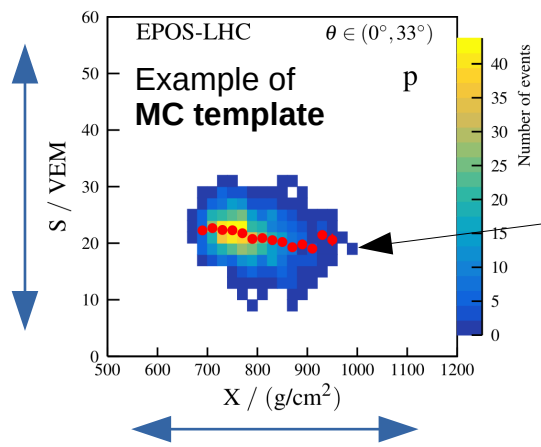
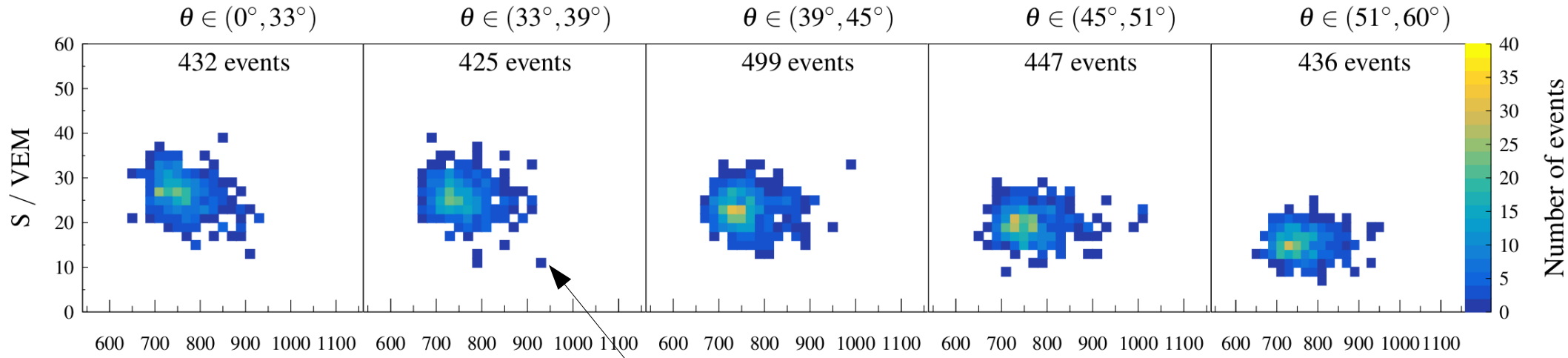
**Auger data:**  
2239 HQ events for  $10^{18.5-19.0}$  eV

# Method

$$S = S(1000) \left( \frac{E^{\text{ref}}}{E_{\text{FD}}} \right)^{1/B}$$

$$X = X_{\text{max}} + D \lg \left( \frac{E^{\text{ref}}}{E_{\text{FD}}} \right)$$

$E^{\text{ref}} = 10^{18.7}$  eV



$$\ln \mathcal{L} = \begin{cases} \sum_k \sum_j (C_{jk} - n_{jk} + n_{jk} \ln \frac{n_{jk}}{C_{jk}}), & n_{jk} > 0 \\ \sum_k \sum_j C_{jk}, & n_{jk} = 0 \end{cases}$$

$\theta$  bins  
2D bins

- **Freedom** in  $X_{\text{max}}$  ( $\Delta X_{\text{max}}$ ) and  $S(1000)$  ( $R_{\text{had}}(\theta)$ ) and **primary fractions**
- Change of  $S_{\text{had}}$  and  $S_{\text{em}}$  due to  $\Delta X_{\text{max}}$  incorporated

Simultaneous log-likelihood ratio fit of **two-dimensional distributions** of  $X_{\text{max}}$  and  $S(1000)$  in 5 zenith-angle bins with **MC templates** for combinations of four primary nuclei (p, He, O, Fe)

# Motivations for modifications of MC predictions

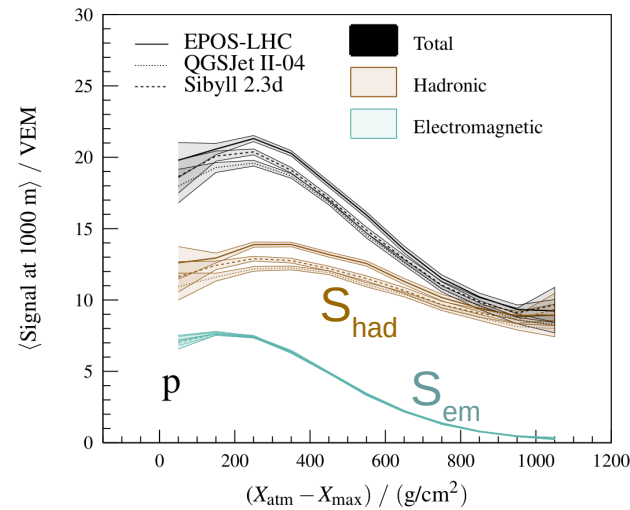
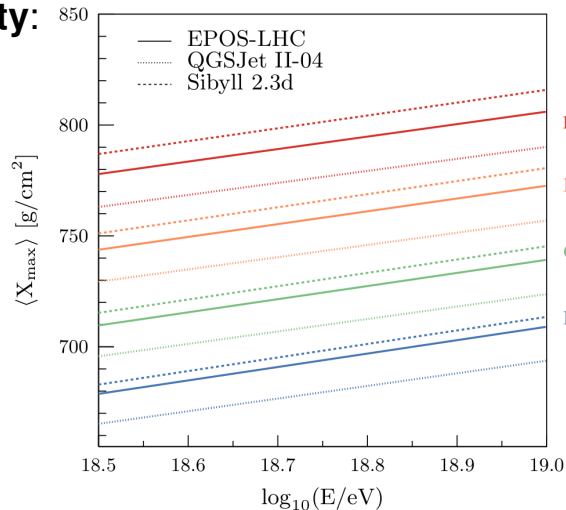
- Properties of **4-component shower universality**:

[Astropart. Phys. 87 (2017) 23, Astropart. Phys. 88 (2017) 46]

- $S(1000) = S_{had} + S_{em}$
- $S_{em}$  very universal

- Main differences** between model predictions:

- Scale of  $\langle X_{max} \rangle$  and  $\langle S_{had} \rangle(\theta)$  are **approx. primary and energy independent**



$$X_{atm} = 880 / \cos \theta \text{ g/cm}^2$$

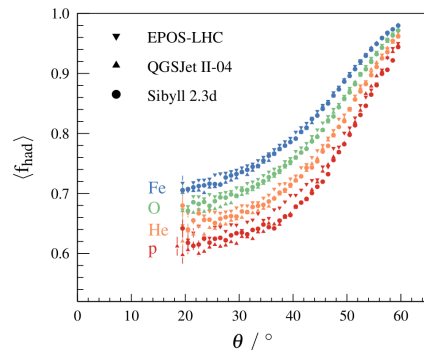
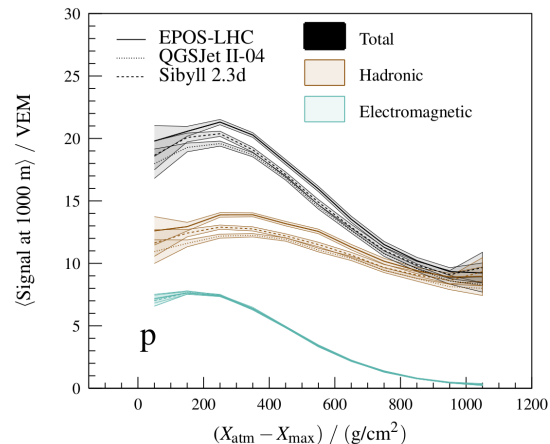
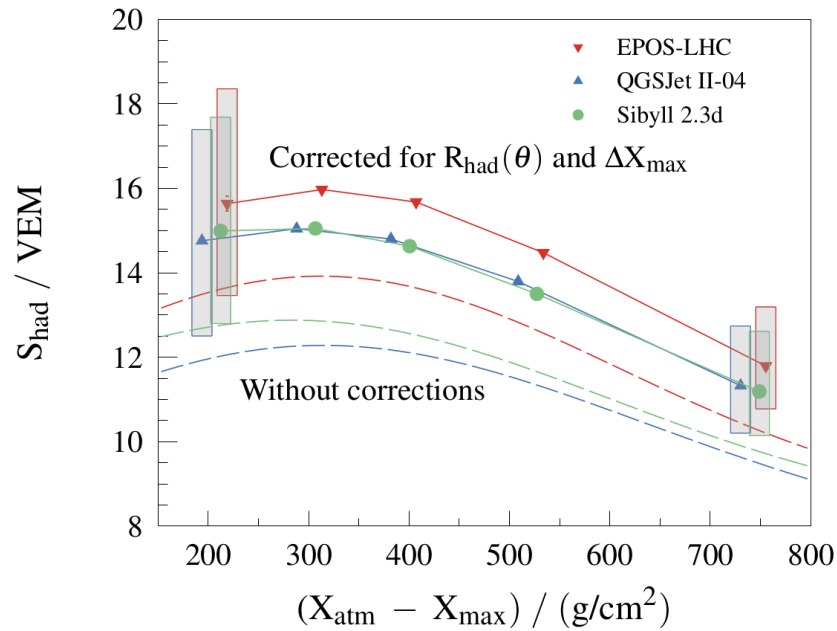
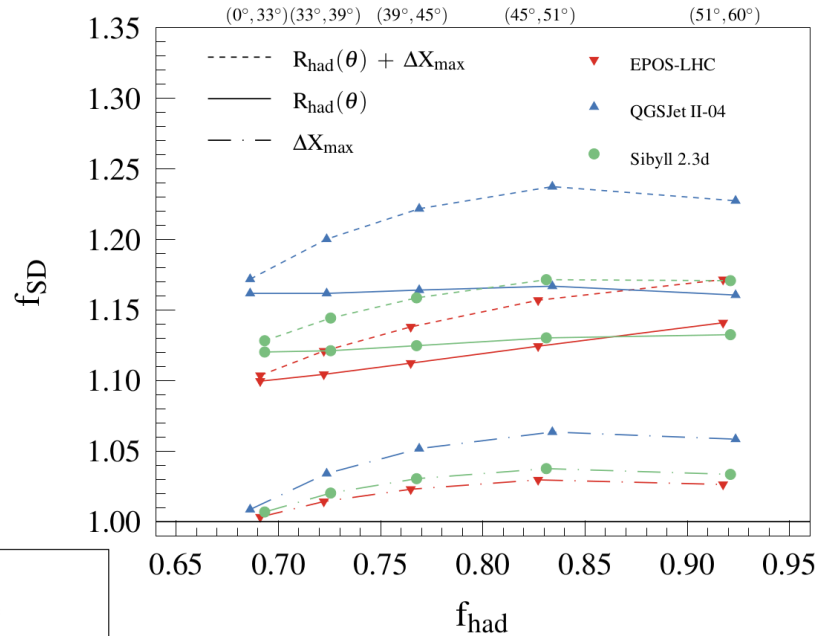
**Caveat:** no modifications in fluctuations or mass-dependencies etc. considered

## ad-hoc modifications

$$X_{max} \rightarrow X_{max} + \Delta X_{max}$$

$$S_{had}(\theta) \rightarrow S_{had}(\theta) \cdot R_{had}(\theta)$$

# Effect of modified $X_{\max}$ on the ground signal



# Assumption on primary species

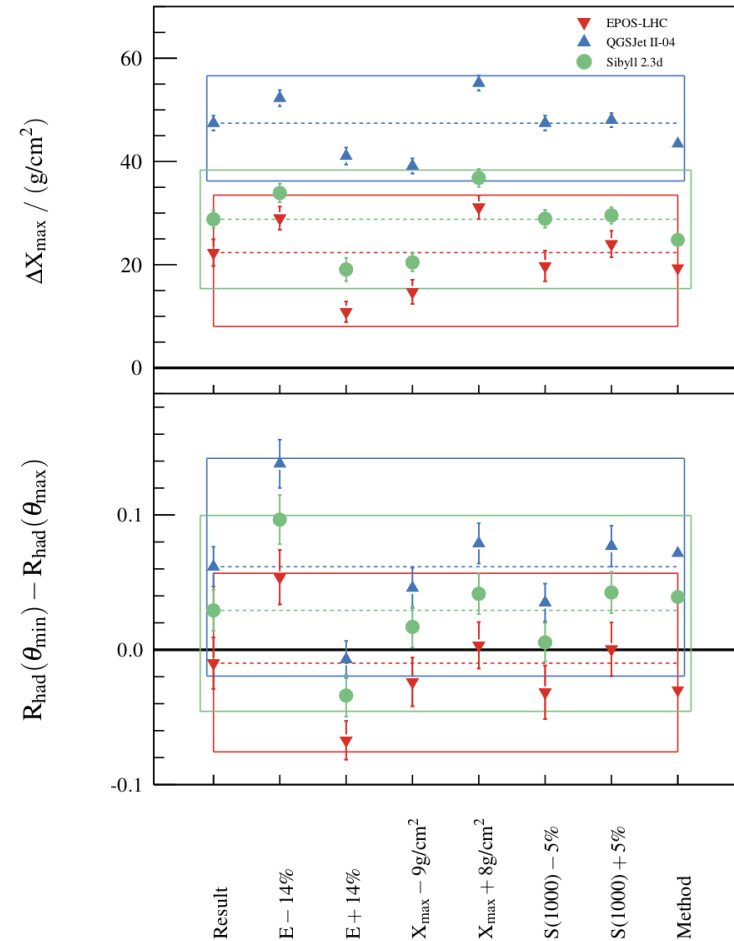
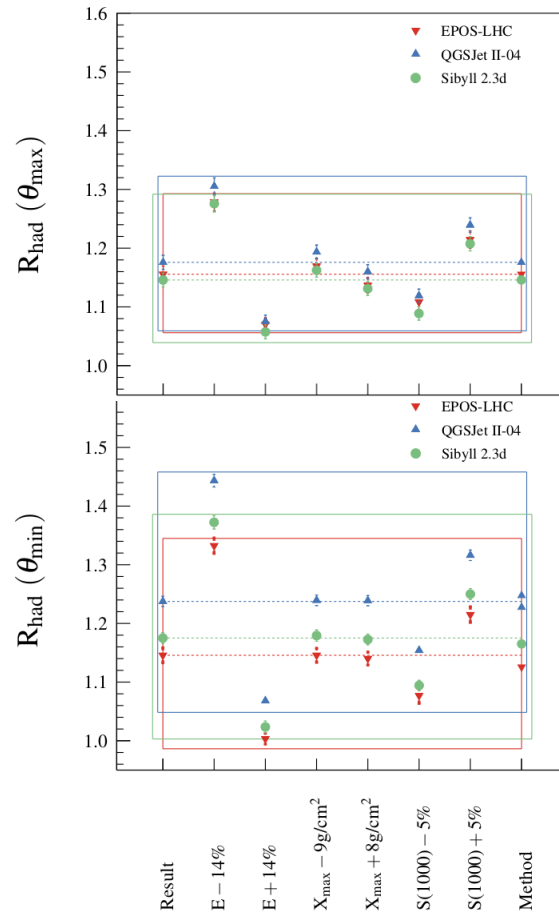
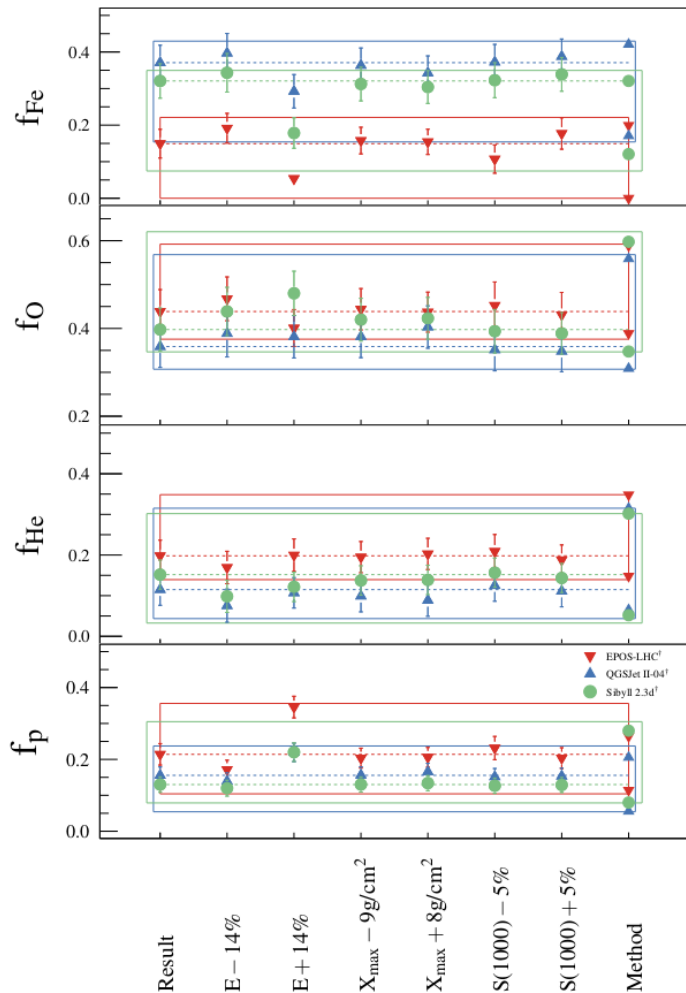
- $\Delta X_{\max}$  decreases by about 5-7, 10-17 and 30-40 g/cm<sup>2</sup> and  $R_{\text{had}}(\theta)$  increases by about 2-5%, 4-9% and 15-20% when the heaviest primary Fe is replaced by Si, O and He, respectively

$\ln \mathcal{L}_{\min}$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
p He	518.3	633.5	563.5
p He O	467.5	523.3	486.6
p He O Fe	451.9	476.3	451.6

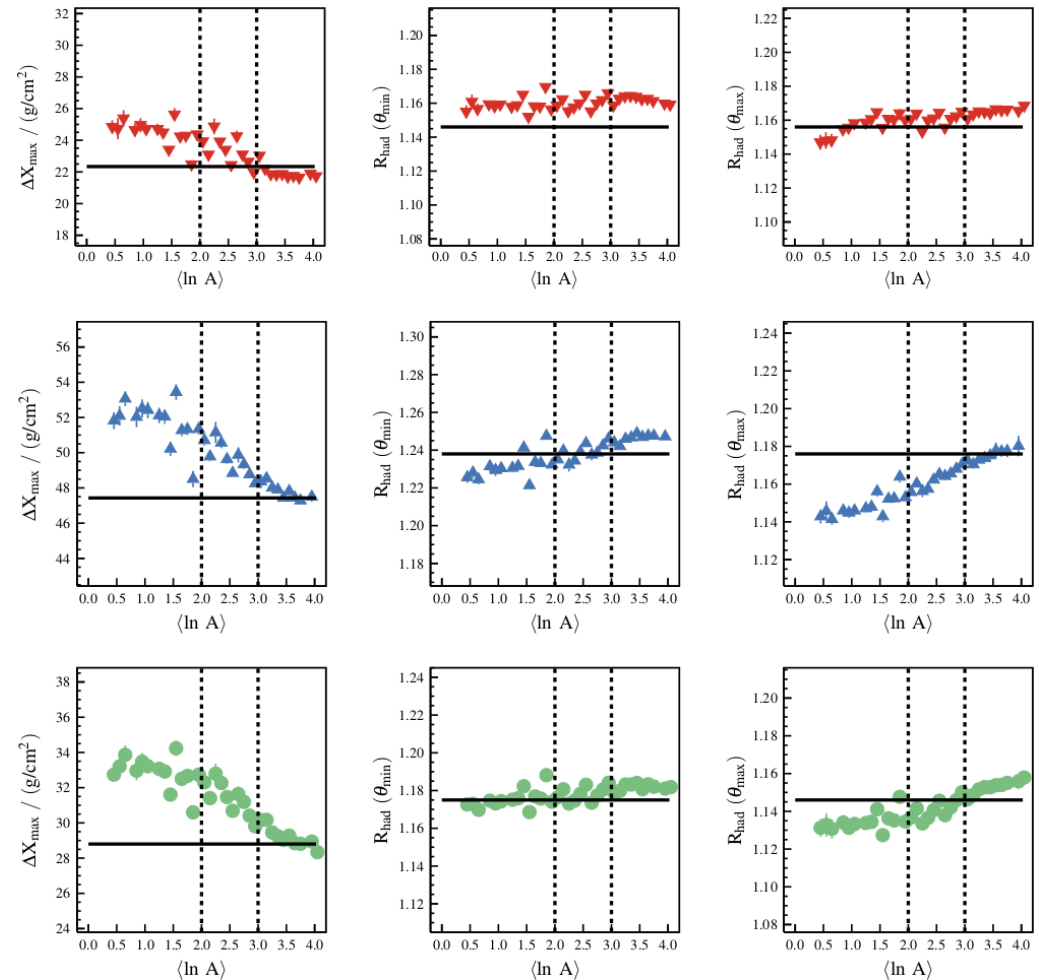
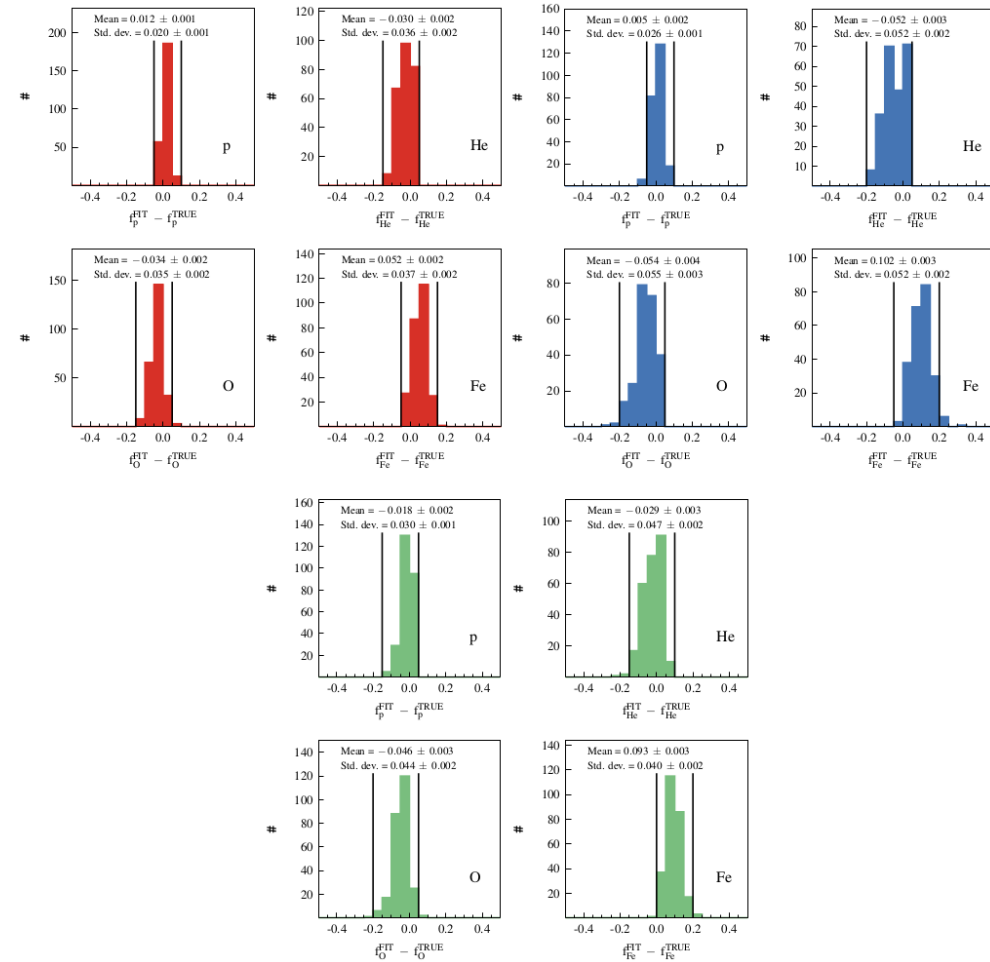


Significance of improvement of data description above  $5\sigma$

# Systematic uncertainties



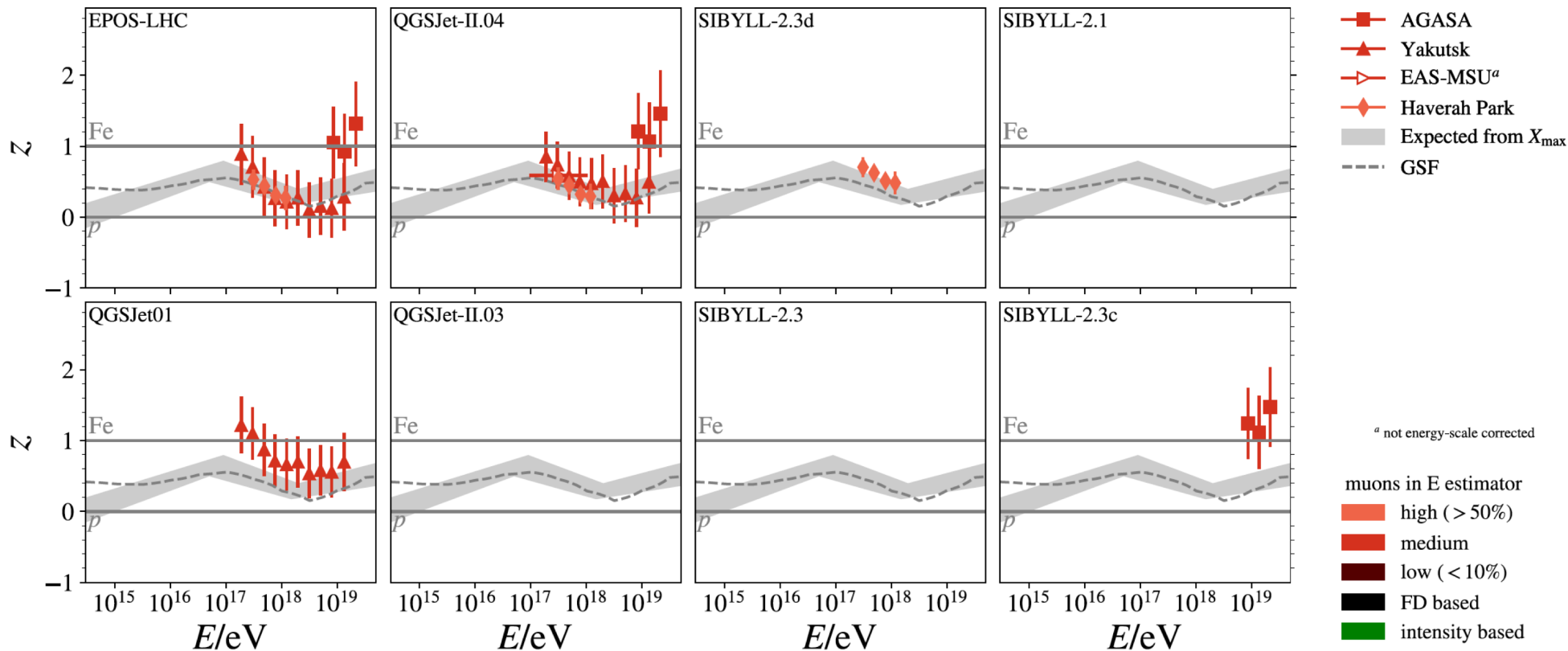
# MC-MC tests



# Experiments using muons for energy estimation

[PoS(ICRC2023)466, L.Cazon Jan 2024 - Workshop on the Tuning of hadronic interactions]

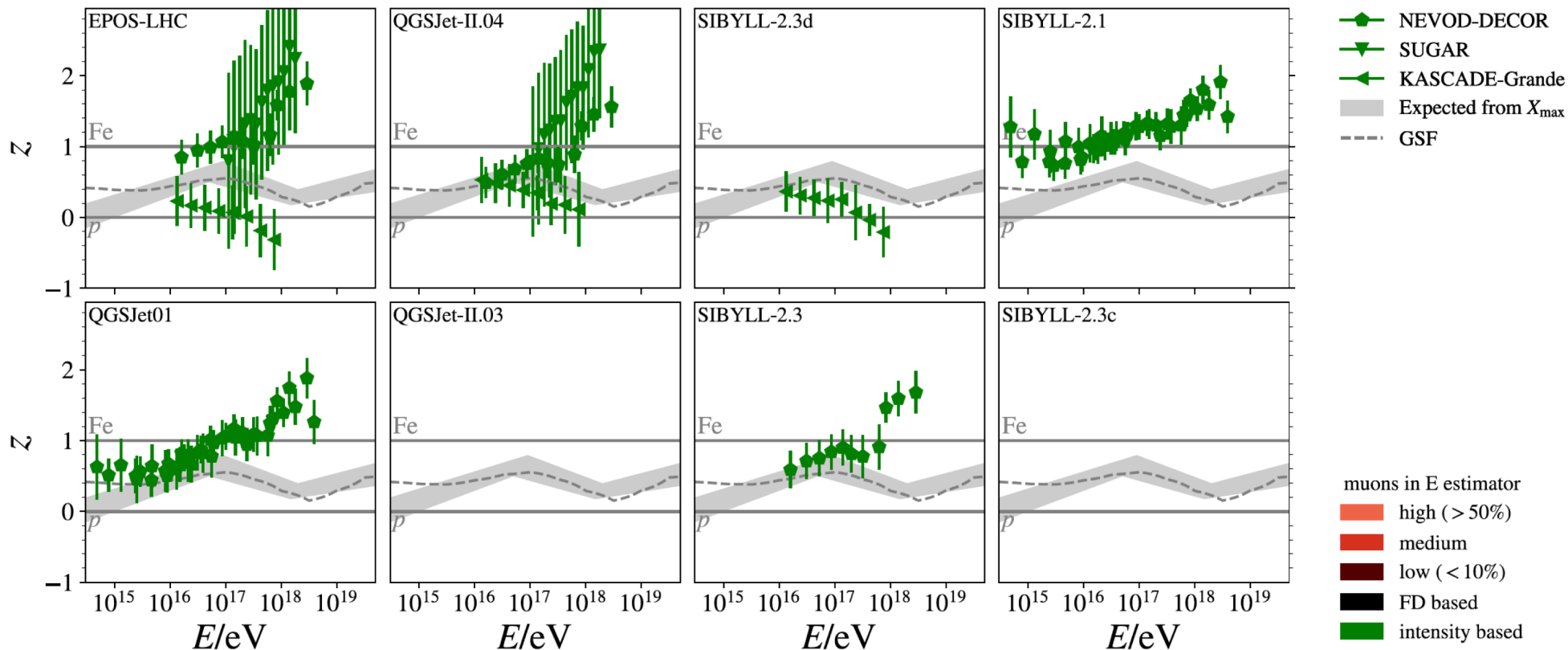
► Classification according to the muon contamination in the estimated primary energy.



# Experiments applying CR intensity estimation of energy

[PoS(ICRC2023)466, L.Cazon Jan 2024 - Workshop on the Tuning of hadronic interactions]

► Classification according to the muon contamination in the estimated primary energy.

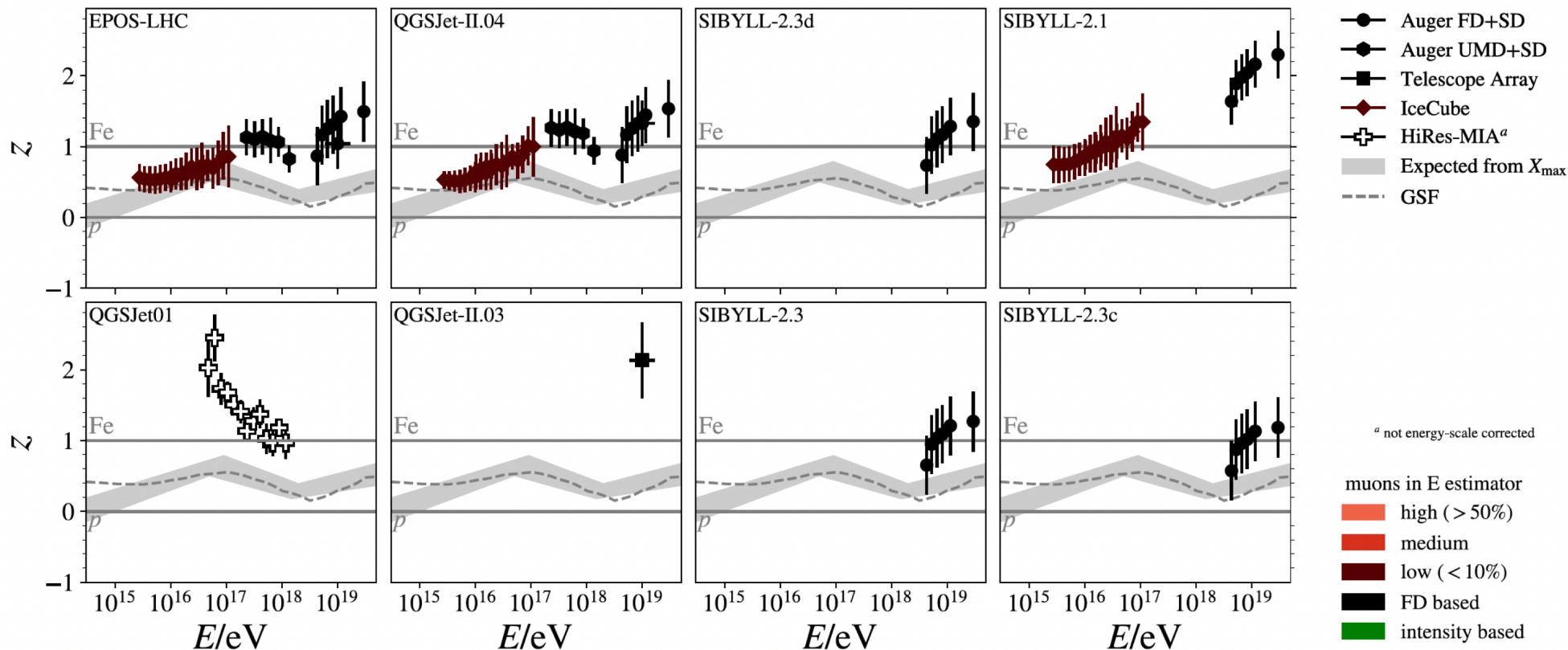




# Experiments using $\sim$ muon independent energy estimator

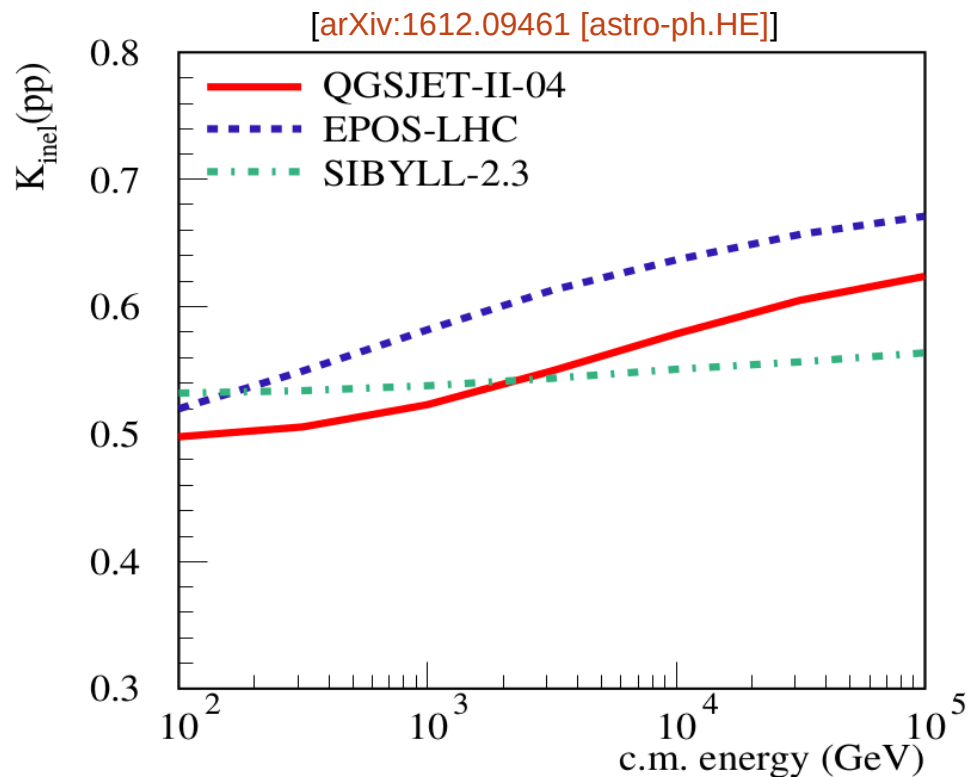
[PoS(ICRC2023)466, L.Cazon Jan 2024 - Workshop on the Tuning of hadronic interactions]

► Classification according to the muon contamination in the estimated primary energy.



# Possible mass-(in)dependence of $X_{\max}$ shift

“changing the normalization of energy dependence”  $\rightarrow$  mass independent modifications



multiplicity:  $N \propto N_0 \cdot E^\alpha$

inelasticity:  $\kappa \propto \kappa_0 \cdot E^{-\omega}$

$$X_{\max}^A = X_1^A + X_0 \ln \frac{\kappa E}{A \cdot 2N \xi_C^\pi} =$$

$$X_1^A + (1 - \alpha - \omega) \cdot \left( X_0 \ln \frac{E}{A \cdot \xi_C^\pi} \right) + X_0 \cdot (\ln \kappa_0 - \ln N_0)$$

$$\begin{matrix} \kappa_0 \rightarrow f_\kappa \kappa_0 \\ N_0 \rightarrow f_N N_0 \end{matrix} \Rightarrow X_{\max}^A ' = X_{\max}^A + X_0 (\ln(f_\kappa) - \ln(f_N))$$

“changing the shape of energy dependence” → mass-dependent modifications

